

## Appendix: Housework and fiscal expansions

Stefano Gnocchi, Daniela Hauser, and Evi Pappa<sup>1</sup>

---

### Abstract

We build an otherwise-standard business cycle model with housework, calibrated consistently with data on time use, in order to discipline complementarity between consumption and hours worked and relate its strength to the size of fiscal multipliers. Evidence on the substitutability between home and market goods confirms that complementarity is an empirically relevant driver of fiscal multipliers. However, we also find that in a housework model substantial complementarity can be generated without imposing a low wealth effect, which contradicts the microeconomic evidence. Also, explicitly modeling housework matters for assessing the welfare effects of government spending, which are understated by theories that neglect substitutability between home-produced and market goods.

*Keywords:* Government expenditure shocks, home production

*JEL Codes:* E24, E32, E52

---

<sup>1</sup>Gnocchi: Bank of Canada, 234 Laurier Avenue West, ON, K1A 0G0 Ottawa, Canada (e-mail: sgnocchi@bankofcanada.ca); Hauser: Bank of Canada, 234 Laurier Avenue West, ON, K1A 0G0 Ottawa, Canada (e-mail: dhauser@bankofcanada.ca); Pappa: European University Institute, Universitat Autònoma de Barcelona and CEPR; Department of Economics, Villa San Paolo, Via della Piazzuola 43, 50133 Florence, Italy (e-mail: evi.pappa@eui.eu). The views expressed in this paper are those of the authors. No responsibility for them should be attributed to the Bank of Canada. Evi Pappa gratefully acknowledges financial support from the Spanish Ministry of Education and Science through grant ECO2009-09847, the support of the Barcelona GSE Research Network and of the Government of Catalonia.

## 1. The Model

### 1.1. Households' Problem and first-order conditions

In this section we lay out the households' problem and the respective first order conditions. Given initial values of the capital stock  $K_0$  and assets  $B_0$ , and  
 5 all prices and policies, households maximize their lifetime utility by choosing a state-contingent sequence  $\{C_{m,t}, C_{n,t}, h_{m,t}, h_{n,t}, K_{m,t}, K_{n,t}, K_{t+1}, B_t\}_{t=0}^{\infty}$ , i.e.,

$$\max E_0 \sum_{t=0}^{\infty} \beta^t U(C_t, l_t),$$

subject to

$$C_t = [\alpha_1(C_{m,t})^{b_1} + (1 - \alpha_1)(C_{n,t})^{b_1}]^{\frac{1}{b_1}}, \quad \alpha_1 \in [0, 1] \quad b_1 < 1, \quad (1)$$

$$C_{n,t} = (K_{n,t})^{\alpha_2} (h_{n,t})^{1-\alpha_2}$$

$$l_t = 1 - h_t,$$

10

$$h_t = h_{m,t} + h_{n,t},$$

$$K_t = K_{m,t} + K_{n,t}$$

$$\begin{aligned} E_t \{Q_{t,t+1} B_{t+1}\} + P_t C_{m,t} + P_t \left[ K_{t+1} - (1 - \delta) K_t + \frac{\xi}{2} \left( \frac{K_{t+1}}{K_t} - 1 \right)^2 \right] & (2) \\ \leq B_t + W_t P_t h_{m,t} + r_t^k P_t K_{m,t} + T_t. \end{aligned}$$

where the utility function is specified as in Section 4.2 in the main text:

$$U(C_t, l_t) = \frac{[(C_t)^b (l_t)^{1-b}]^{1-\sigma} - 1}{1 - \sigma}, \quad b \in (0, 1), \quad \sigma \geq 1.$$

Then, the Lagrangian is defined as follows:

$$\begin{aligned}
\mathcal{L} = E_0 \sum_{t=0}^{\infty} \beta^t & \frac{\left[ \alpha_1 (C_{m,t})^{b_1} + (1 - \alpha_1) (C_{n,t})^{b_1} \right]^{\frac{b}{b_1}} (1 - h_{n,t} - h_{m,t})^{1-b}}{1 - \sigma} - 1 \\
& + \mu_t \left[ (K_{n,t})^{\alpha_2} (h_{n,t})^{1-\alpha_2} - C_{n,t} \right] \\
& + \gamma_t [K_t - K_{m,t} - K_{n,t}] \\
& + \frac{\lambda_t}{P_t} \left\{ B_t + W_t P_t h_{m,t} + r_t^k P_t K_{m,t} + T_t - E_t \{ Q_{t,t+1} B_{t+1} \} - P_t C_{m,t} \right. \\
& \left. - P_t \left[ K_{t+1} + (1 - \delta) K_t + \frac{\xi}{2} \left( \frac{K_{t+1}}{K_t} - 1 \right)^2 \right] \right\}
\end{aligned}$$

We divide the budget constraint by  $P_t$ , which is given to households, so that we can interpret  $\lambda_t$  as the marginal utility of wealth directly. By optimality the marginal utility of wealth coincides with the marginal utility of market consumption. The corresponding first-order conditions are:

$$\begin{aligned}
\{C_{m,t}\}: \lambda_t &= U_C(C_t, l_t) \alpha_1 \left( \frac{C_{m,t}}{C_t} \right)^{b_1-1} \\
&= b \alpha_1 (1 - h_{n,t} - h_{m,t})^{(1-b)(1-\sigma)} C_{m,t}^{b_1-1} (C_t)^{b(1-\sigma)-b_1}
\end{aligned} \tag{3}$$

$$\begin{aligned}
\{C_{n,t}\}: \mu_t &= U_C(C_t, l_t) (1 - \alpha_1) \left( \frac{C_{n,t}}{C_t} \right)^{b_1-1} \\
&= b (1 - \alpha_1) (1 - h_{n,t} - h_{m,t})^{(1-b)(1-\sigma)} C_{n,t}^{b_1-1} (C_t)^{b(1-\sigma)-b_1}
\end{aligned} \tag{4}$$

$$\{h_{m,t}\}: \lambda_t W_t = U_l(C_t, l_t) = (1-b)(C_t)^{b(1-\sigma)} (1 - h_{n,t} - h_{m,t})^{(1-b)(1-\sigma)-1} \tag{5}$$

$$\begin{aligned}
\{h_{n,t}\}: U_l(C_t, l_t) &= \mu_t (1 - \alpha_2) \left( \frac{C_{n,t}}{h_{n,t}} \right) \\
(1-b)(C_t)^{b(1-\sigma)} (1 - h_{n,t} - h_{m,t})^{(1-b)(1-\sigma)-1} &= \mu_t (1 - \alpha_2) \left( \frac{C_{n,t}}{h_{n,t}} \right)
\end{aligned} \tag{6}$$

20

$$\{K_{m,t}\}: \gamma_t = \lambda_t r_t^k \tag{7}$$

$$\{K_{n,t}\} : \gamma_t = \mu_t \alpha_2 \left( \frac{C_{n,t}}{K_{n,t}} \right) \quad (8)$$

$$\begin{aligned} \{K_{t+1}\} : \beta E_t \left\{ \frac{\lambda_{t+1}}{\lambda_t} \left[ 1 + \frac{\xi}{K_t} \left( \frac{K_{t+1}}{K_t} - 1 \right) \right]^{-1} \right. \\ \left. \left[ 1 - \delta + \xi \left( \frac{K_{t+2}}{K_{t+1}} - 1 \right) \left( \frac{K_{t+2}}{K_{t+1}^2} \right) \right] \right\} + \beta E_t \{\gamma_{t+1}\} = 1 \end{aligned} \quad (9)$$

$$\{B_{t+1}\} : \lambda_t E_t \{Q_{t,t+1}\} = \beta E_t \left\{ \frac{\lambda_{t+1}}{\pi_{t+1}} \right\} \quad (10)$$

Equations (3) and (5) correspond to equations (10) and (11) in the main text,  
 25 respectively. Combining (4) and (6) yields equation (12),

$$\frac{U_l(C_t, l_t)}{(1 - \alpha_1) U_C(C_t, l_t)} \left( \frac{C_{n,t}}{C_t} \right)^{1-b_1} = \frac{(1 - \alpha_2) C_{n,t}}{h_{n,t}}. \quad (11)$$

Similarly, combining (3), (4), (7) and (8) yields equation (13) in the main text

$$\frac{\alpha_1}{1 - \alpha_1} \left[ \frac{C_{m,t}}{C_{n,t}} \right]^{b_1-1} = \frac{\alpha_2 C_{n,t}}{r_t^k K_{n,t}}. \quad (12)$$

Equation (14) results from the first-order conditions with respect to market  
 capital, (7), and with respect to the next-period total capital stock, (9),

$$\begin{aligned} \beta E_t \left\{ \frac{\lambda_{t+1}}{\lambda_t} \left[ 1 + \frac{\xi}{K_t} \left( \frac{K_{t+1}}{K_t} - 1 \right) \right]^{-1} \right. \\ \left. \left[ 1 - \delta + r_{t+1}^k + \xi \left( \frac{K_{t+2}}{K_{t+1}} - 1 \right) \left( \frac{K_{t+2}}{K_{t+1}^2} \right) \right] \right\} = 1. \end{aligned} \quad (13)$$

Finally, by a no-arbitrage argument  $E_t \{Q_{t,t+1}\} = (1 + R_t)^{-1}$ , such that the first-  
 30 order condition with respect to the portfolio of state-contingent assets yields the  
 respective standard Euler equation, equation (15) in the main text

$$\beta E_t \left\{ \frac{\lambda_{t+1}}{\lambda_t} (1 + R_t) \Pi_{t+1}^{-1} \right\} = 1. \quad (14)$$

## 1.2. Firms

In the economy, there are infinitely many monopolistically competitive firms  
 indexed by  $i \in [0, 1]$ . Each firm buys market capital and hours worked on

35 perfectly competitive markets in order to produce a variety  $i$  of the market good, according to the following production function:

$$Y_t(i) = (K_{m,t}(i))^{\alpha_3} (h_{m,t}(i))^{1-\alpha_3}, \quad \alpha_3 \in [0, 1]. \quad (15)$$

Cost minimization yields

$$\alpha_3 RMC_t \left( \frac{Y_t(i)}{K_{m,t}(i)} \right) = r_t^k, \quad (16)$$

$$(1 - \alpha_3) RMC_t \left( \frac{Y_t(i)}{h_{m,t}(i)} \right) = W_t. \quad (17)$$

The real marginal cost,  $RMC_t$ , is constant across firms because of constant returns to scale in production and perfect competition on factor markets. We  
40 follow Calvo [6] and we assume that in any given period each firm resets its price  $P_t(i)$  with a constant probability  $(1 - \theta)$ . At a given price  $P_t(i)$ , production has to satisfy demand:

$$Y_t(i) = \left[ \frac{P_t(i)}{P_t} \right]^{-\varepsilon} Y_t^d. \quad (18)$$

where aggregate demand,  $Y_t^d$ , is taken as given. We assume that production is subsidized by the government, which pays a fraction  $\tau$  of the cost per unit of  
45 production. Maximization of profits

$$E_t \left\{ \sum_{j=0}^{\infty} \theta^j Q_{t,t+j} [P_t(i) Y_{t+j}(i) - P_{t+j} (1 - \tau) RMC_{t+j} Y_{t+j}(i)] \right\} \quad (19)$$

subject to constraint (18) yields the following first-order condition for any firm  $i$  that is allowed to re-optimize in period  $t$ :

$$E_t \left\{ \sum_{j=0}^{\infty} \theta^j Q_{t,t+j} Y_{t+j}(i) \left[ \frac{P_t^*}{P_t} - \frac{\varepsilon(1 - \tau)}{\varepsilon - 1} RMC_{t+j} \Pi_{t,t+j} \right] \right\} = 0. \quad (20)$$

$P_t^*$  is the optimal price,  $Q_{t,t+j}$  denotes the stochastic discount factor in period  $t$  for nominal profits  $j$  periods ahead and it is such that

$$Q_{t,t+j} = \beta^j E_t \left\{ \frac{\lambda_{t+j}}{\lambda_t} \Pi_{t,t+j}^{-1} \right\}, \quad (21)$$

50 while  $\Pi_{t,t+j} \equiv (P_{t+j}/P_t)$ . Calvo pricing implies the following conventional relation between inflation and the relative price charged by re-optimizing firms:

$$\frac{P_t^*}{P_t} = \left( \frac{1 - \theta \Pi_t^{\varepsilon-1}}{1 - \theta} \right)^{\frac{1}{1-\varepsilon}}. \quad (22)$$

The necessary condition for profit maximization (20) can easily be rewritten as

$$\frac{P_t^*}{P_t} = \frac{x_{1,t}}{x_{2,t}}, \quad (23)$$

55 where the auxiliary variables  $x_{1,t}$  and  $x_{2,t}$  are recursively defined by

$$x_{1,t} = [C_{m,t} + I_t + G_t] \left( \frac{\varepsilon(1-\tau)}{\varepsilon-1} \right) RMC_t + \beta \theta E_t \left\{ \frac{\lambda_{t+1}}{\lambda_t} \Pi_{t+1}^\varepsilon x_{1,t+1} \right\}, \quad (24)$$

$$x_{2,t} = [C_{m,t} + I_t + G_t] + \beta \theta E_t \left\{ \frac{\lambda_{t+1}}{\lambda_t} \Pi_{t+1}^{\varepsilon-1} x_{2,t+1} \right\}. \quad (25)$$

### 1.3. Aggregation and Market Clearing

After defining aggregate production

$$Y_t = \left[ \int_0^1 (Y_t(i))^{\frac{\varepsilon-1}{\varepsilon}} di \right]^{\frac{\varepsilon}{\varepsilon-1}}, \quad (26)$$

the clearing of the goods market implies

$$Y_t = C_{m,t} + I_t + G_t. \quad (27)$$

Define the market capital-labor ratio,  $k_t \equiv (K_{m,t}(i)) / (h_{m,t}(i))$ . By equations  
60 (16) and (17), the ratio is constant across firms and satisfies

$$k_t = \frac{\alpha_3 W_t}{(1 - \alpha_3) r_t}. \quad (28)$$

By the clearing of the labor market,

$$h_{m,t} = \int_0^1 h_{m,t}(i) di. \quad (29)$$

Integrating equation (15) over all firms  $i$  yields

$$Y_t = \Delta_t^{-1} k_t^{\alpha_3} h_{m,t}, \quad (30)$$

where  $\Delta_t$  denotes relative price dispersion

$$\Delta_t \equiv \int_0^1 \left( \frac{P_t(i)}{P_t} \right)^{-\varepsilon} di, \quad (31)$$

and evolves according to

$$\Delta_t = (1 - \theta) \left( \frac{P_t^*}{P_t} \right)^{-\varepsilon} + \theta \Pi_t^\varepsilon \Delta_{t-1}. \quad (32)$$

65 It is well known that  $\log(\Delta_t)$  is a second-order term and can thus be neglected when the model is approximated to the first order around the non-stochastic steady state. By the clearing of the capital rental market,

$$K_{m,t} = \int_0^1 K_{m,t}(i) di, \quad (33)$$

which implies

$$K_{m,t} = k_t h_{m,t}. \quad (34)$$

Finally, by using (34) into (30), one can obtain the aggregate production function  
70 tion

$$Y_t = \Delta_t^{-1} (K_{m,t})^{\alpha_3} (h_{m,t})^{1-\alpha_3}, \quad (35)$$

as well as the aggregate counterparts of equations (16) and (17):

$$\alpha_3 RMC_t \left( \frac{\Delta_t Y_t}{K_{m,t}} \right) = r_t, \quad (36)$$

$$(1 - \alpha_3) RMC_t \left( \frac{\Delta_t Y_t}{h_{m,t}} \right) = W_t. \quad (37)$$

#### 1.4. Equilibrium Definition

In this section we define the equilibrium for a housework model with a KPR utility function, as specified in Section 4.2 of the main text. The equilibrium of  
75 the model is a set of state-contingent plans for variables  $C_t$ ,  $C_{m,t}$ ,  $C_{n,t}$ ,  $K_{m,t}$ ,  $K_{n,t}$ ,  $K_t$ ,  $h_{m,t}$ ,  $h_{n,t}$ ,  $I_t$ ,  $\lambda_t$ ,  $Y_t$ ,  $\Pi_t$ ,  $\Delta_t$ ,  $\frac{P_t^*}{P_t}$ ,  $x_{1,t}$ ,  $x_{2,t}$ ,  $RMC_t$ ,  $R_t$ ,  $W_t$  and  $r_t^k$  that satisfy the following system of equations

$$C_t = [\alpha_1 (C_{m,t})^{b_1} + (1 - \alpha_1) (C_{n,t})^{b_1}]^{\frac{1}{b_1}} \quad (38)$$

$$C_{n,t} = (K_{n,t})^{\alpha_2} (h_{n,t})^{1-\alpha_2} \quad (39)$$

$$K_t = K_{m,t} + K_{n,t} \quad (40)$$

$$K_{t+1} = (1-\delta)K_t + I_t - \frac{\xi}{2} \left( \frac{K_{t+1}}{K_t} - 1 \right)^2 \quad (41)$$

$$\left( \frac{\alpha_1}{1-\alpha_1} \right) \left( \frac{C_{m,t}}{C_{n,t}} \right)^{b_1-1} = \left( \frac{1-\alpha_2}{W_t} \right) \left( \frac{C_{n,t}}{h_{n,t}} \right) \quad (42)$$

$$\left( \frac{\alpha_1}{1-\alpha_1} \right) \left( \frac{C_{m,t}}{C_{n,t}} \right)^{b_1-1} = \left( \frac{\alpha_2}{r_t^k} \right) \left( \frac{C_{n,t}}{K_{n,t}} \right) \quad (43)$$

$$W_t(1-h_{n,t}-h_{m,t}) = \left( \frac{1-b}{b\alpha_1} \right) C_{m,t}^{1-b_1} C_t^{b_1} \quad (44)$$

$$\beta E_t \left\{ \frac{\lambda_{t+1}}{\lambda_t} \left[ 1 + \frac{\xi}{K_t} \left( \frac{K_{t+1}}{K_t} - 1 \right) \right]^{-1} \right. \\ \left. \left[ 1 - \delta + r_{t+1}^k + \xi \left( \frac{K_{t+2}}{K_{t+1}} - 1 \right) \left( \frac{K_{t+2}}{K_{t+1}^2} \right) \right] \right\} = 1, \quad (45)$$

$$\beta E_t \left\{ \frac{\lambda_{t+1}}{\lambda_t} (1 + R_t) \Pi_{t+1}^{-1} \right\} = 1 \quad (46)$$

$$\lambda_t = b\alpha_1(1-h_{n,t}-h_{m,t})^{(1-b)(1-\sigma)} C_{m,t}^{b_1-1} (C_t)^{b(1-\sigma)-b_1} \quad (47)$$

$$\frac{P_t^*}{P_t} = \left( \frac{1-\theta \Pi_t^{\varepsilon-1}}{1-\theta} \right)^{\frac{1}{1-\varepsilon}} \quad (48)$$

$$\frac{P_t^*}{P_t} = \frac{x_{1,t}}{x_{2,t}} \quad (49)$$

$$x_{1,t} = [C_{m,t} + I_t + G_t] \left( \frac{\varepsilon(1-\tau)}{\varepsilon-1} \right) RMC_t + \beta \theta E_t \left\{ \frac{\lambda_{t+1}}{\lambda_t} \Pi_{t+1}^{\varepsilon} x_{1,t+1} \right\}$$



$$x_{2,t} = [C_{m,t} + I_t + G_t] + \beta\theta E_t \left\{ \frac{\lambda_{t+1}}{\lambda_t} \Pi_{t+1}^{\varepsilon-1} x_{2,t+1} \right\} \quad (50)$$

$$Y_t = C_{m,t} + I_t + G_t \quad (51)$$

$$Y_t = \Delta_t^{-1} (K_{m,t})^{\alpha_3} (h_{m,t})^{1-\alpha_3} \quad (52)$$

$$\alpha_3 RMC_t \left( \frac{\Delta_t Y_t}{K_{m,t}} \right) = r_t^k \quad (53)$$

$$(1 - \alpha_3) RMC_t \left( \frac{\Delta_t Y_t}{h_{m,t}} \right) = W_t \quad (54)$$

$$\Delta_t = (1 - \theta) \left( \frac{P_t^*}{P_t} \right)^{-\varepsilon} + \theta \Pi_t^\varepsilon \Delta_{t-1} \quad (55)$$

for all  $t$ , for given government expenditure. To close the equilibrium definition, we further need a specification for monetary policy and a law of motion for  
80 government expenditure.

### 1.5. Frisch System

Following Frisch [10], we define the Frisch system of our housework model with a KPR utility function, as specified in Section 4.2 of the main text. Six equations define the Frisch system:

$$f1 = b\alpha_1(1 - h_{n,t} - h_{m,t})^{(1-b)(1-\sigma)} C_{m,t}^{b_1-1} C_t^{b(1-\sigma)-b_1} - \lambda_t \quad (56)$$

$$f2 = (1 - b)C_t^{b(1-\sigma)}(1 - h_{n,t} - h_{m,t})^{(1-b)(1-\sigma)-1} - \lambda_t W_t \quad (57)$$

$$f3 = (1 - h_{n,t} - h_{m,t})b(1 - \alpha_1)(1 - \alpha_2) \frac{C_{n,t}^{b_1}}{h_{n,t}} - (1 - b)C_t^{b_1} \quad (58)$$

$$f4 = b(1 - \alpha_1)\alpha_2(1 - h_{n,t} - h_{m,t})^{(1-b)(1-\sigma)} C_t^{b(1-\sigma)-b_1} \frac{C_{n,t}^{b_1}}{K_{n,t}} - r_t^k \lambda_t \quad (59)$$

$$f5 = [\alpha_1(C_{m,t})^{b_1} + (1 - \alpha_1)(C_{n,t})^{b_1}]^{\frac{1}{b_1}} - C_t \quad (60)$$

$$f6 = (K_{n,t})^{\alpha_2} (h_{n,t})^{1-\alpha_2} - C_{n,t} \quad (61)$$

85 where the choice variables are

$$y_t = \{C_{m,t}, C_{n,t}, C_t, h_{m,t}, h_{n,t}, K_{n,t}\}, \quad (62)$$

whereas  $x_t = \{\lambda_t, W_t, r_t^k\}$  are taken as given. Equation  $f1$  coincides with (3) and defines the marginal utility of market consumption and  $f2$  is the first-order optimality condition with respect to hours worked on the market (equation (5)). Combining the first-order conditions with respect to home goods and hours  
 90 worked in the home sector, (6) and (4), results in  $f3$ . Equivalently, combining the first-order conditions with respect to capital in both sectors (equation (7) and (8)) and further with respect to home goods (4) yields  $f4$ . To close the system we also need the total consumption aggregator ( $f5$ ) and the home-production technology ( $f6$ ).

95 Define  $f = [f1; f2; f3; f4; f5; f6]$  and the matrix of unknown derivatives we are interested in

$$Z_{y,x} = \begin{pmatrix} \frac{\partial C_{m,t}}{\partial \lambda_t} & \frac{\partial C_{m,t}}{\partial W_t} & \frac{\partial C_{m,t}}{\partial r_t^k} \\ \frac{\partial C_{n,t}}{\partial \lambda_t} & \frac{\partial C_{n,t}}{\partial W_t} & \frac{\partial C_{n,t}}{\partial r_t^k} \\ \frac{\partial C_t}{\partial \lambda_t} & \frac{\partial C_t}{\partial W_t} & \frac{\partial C_t}{\partial r_t^k} \\ \frac{\partial h_{m,t}}{\partial \lambda_t} & \frac{\partial h_{m,t}}{\partial W_t} & \frac{\partial h_{m,t}}{\partial r_t^k} \\ \frac{\partial h_{n,t}}{\partial \lambda_t} & \frac{\partial h_{n,t}}{\partial W_t} & \frac{\partial h_{n,t}}{\partial r_t^k} \\ \frac{\partial K_{n,t}}{\partial \lambda_t} & \frac{\partial K_{n,t}}{\partial W_t} & \frac{\partial K_{n,t}}{\partial r_t^k} \end{pmatrix} \quad (63)$$

We then solve the following system for matrix  $Z_{y,x}$

$$\begin{matrix} J_y & Z_{y,x} & + & J_x & = & 0, \\ 6*6 & 6*3 & & 6*3 & & \end{matrix} \quad (64)$$

where  $J_y$  is the Jacobian matrix of function  $f$  with respect to the control variables, and  $J_x$  is the Jacobian matrix of function  $f$  with respect to the state  
 100 variables.

## 2. Simplified model without capital and $G = 0$

### 2.1. Algebra of complementarity

Assume  $\alpha_2 = \alpha_3 = 0$  and  $K_n = K_m = G = 0$ , where variables without time subscript denote a steady state. Hence,  $C_n = h_n$  and the household's optimality

105 condition (11) becomes

$$\frac{U_l(C_t, l_t)}{(1 - \alpha_1)U_C(C_t, l_t)} \left( \frac{C_{n,t}}{C_t} \right)^{1-b_1} = 1, \quad (65)$$

which, combined with the definition of  $\lambda$ , (3), can be rewritten as

$$\frac{U_l(C_t, l_t)}{\lambda_t} \frac{\alpha_1}{1 - \alpha_1} \left( \frac{C_{m,t}}{C_{n,t}} \right)^{b_1-1} = 1. \quad (66)$$

The system of equations (3), (5) and (66), together with feasibility constraints (1), fully describes households' intra-temporal optimality. At a zero-inflation steady state  $\Pi = 1$  and  $\Delta = 1$ , by firms' optimality and by the clearing of all  
110 markets  $W = 1$  and  $C_m = h_m$ , which imply, together with equations (1), (3), (5) and (66), all evaluated at the steady state, relations

$$\lambda = U_l(C, l), \quad U_l(C, l) = U_C(C, l)(1 - \alpha_1) \left( \frac{C_n}{C} \right)^{b_1-1}, \quad (67)$$

$$U_l(C, l) = U_C(C, l)\alpha_1 \left( \frac{C_m}{C} \right)^{b_1-1}, \quad \alpha_1 \left( \frac{C_m}{C} \right)^{b_1} = \frac{h_m}{h},$$

$$(1 - \alpha_1) \left( \frac{C_n}{C} \right)^{b_1} = \frac{h_n}{h}, \quad U_l(C, l) = U_C(C, l) \frac{C}{h}.$$

Log-linearization of (3), (5) and (66), respectively, around the steady state yields

$$\widehat{\lambda}_t = (\nu - \gamma)\widehat{C}_t + \frac{\nu l}{h}\widehat{l}_t + (1 - b_1) \left( \widehat{C}_t - \widehat{C}_{m,t} \right) \quad (68)$$

$$\widehat{W}_t = \nu\widehat{C}_t + \frac{(\nu - \varphi)l}{h}\widehat{l}_t - \widehat{\lambda}_t$$

$$\widehat{\lambda}_t = \nu\widehat{C}_t + \frac{(\nu - \varphi)l}{h}\widehat{l}_t + (1 - b_1) \left( \widehat{C}_{n,t} - \widehat{C}_{m,t} \right)$$

where  $\widehat{\cdot}$  denote log-deviations from the steady state and parameters are defined  
115 as follows:

$$\begin{aligned} \gamma &\equiv -\frac{U_{C,C}C}{U_C} + \frac{U_{C,l}C}{U_l}; \\ \varphi &\equiv -\frac{U_{l,l}h}{U_l} + \frac{U_{C,l}h}{U_C}; \\ \nu &\equiv \frac{U_{C,l}h}{U_C}. \end{aligned} \quad (69)$$

Definitions (69) imply the following relations

$$\frac{U_{C,C}C}{U_C} = \nu - \gamma, \quad \frac{U_{l,l}h}{U_l} = \nu - \varphi, \quad \frac{U_{C,l}C}{U_l} = \nu, \quad (70)$$

where the last equality follows from the definition of  $\nu$  and relations (67). Moreover, log-linearizing (1) yields

$$\widehat{C}_t = \frac{h_m}{h} \widehat{C}_{m,t} + \frac{h_n}{h} \widehat{C}_{n,t}, \quad \widehat{l}_t = -\frac{h_m}{1-h} \widehat{h}_{m,t} - \frac{h_n}{1-h} \widehat{h}_{n,t}, \quad \widehat{C}_{n,t} = \widehat{h}_{n,t}. \quad (71)$$

Relations (68) and (71) determine  $\widehat{C}_{m,t}$ ,  $\widehat{C}_{n,t}$ ,  $\widehat{h}_{m,t}$ ,  $\widehat{h}_{n,t}$ ,  $\widehat{C}_t$  and  $\widehat{l}_t$ , given  $\widehat{\lambda}_t$  and  $\widehat{W}_t$ . Solving for  $\widehat{C}_{m,t}$  and  $\widehat{h}_{m,t}$  yields equations (28) in the main text and the associated coefficients (29). In addition, solving for  $\widehat{C}_t$  and  $\widehat{l}_t$ , one can find

$$\eta_{l,\lambda} \equiv \left. \frac{\partial \widehat{l}_t}{\partial \widehat{\lambda}_t} \right|_{\widehat{W}_t} = \frac{\gamma}{\varphi(\nu - \gamma) + \nu\gamma} \frac{h}{l}, \quad \eta_{C,\lambda} \equiv \left. \frac{\partial \widehat{C}_t}{\partial \widehat{\lambda}_t} \right|_{\widehat{W}_t} = \frac{\varphi}{\varphi(\nu - \gamma) + \nu\gamma}. \quad (72)$$

We derive restrictions on parameters  $\varphi$ ,  $\gamma$  and  $\nu$  such that  $\eta_{l,\lambda}$  and  $\eta_{C,\lambda}$  are both non-positive, so that consumption and leisure increase with wealth for any given price  $W$ , and they are thus non-inferior. To this purpose, we use equations (72). The proof draws on Bilbiie [2]. Concavity of the utility function requires  $U_{CC} \leq 0$ ,  $U_{ll} \leq 0$ ,  $U_{CC}U_{ll} - U_{Cl}^2 \geq 0$ , which hold if and only if (i)  $\gamma \geq \nu$ , (ii)  $\varphi \geq \nu$ , (iii)  $\gamma\varphi \geq \nu(\varphi + \gamma)$ , respectively. By (72) and concavity requirements,  $\eta_{l,\lambda}$  and  $\eta_{C,\lambda}$  are both non-positive if and only if  $\gamma \geq 0$  and  $\varphi \geq 0$ . In fact, if one of the two parameters is negative, either a non-inferiority condition is violated or the last condition for concavity is violated. But if  $\gamma$  and  $\varphi$  are positive, it is also the case that  $\gamma \geq \gamma\varphi/(\gamma + \varphi)$  and  $\varphi \geq \gamma\varphi/(\gamma + \varphi)$ . Hence, the last condition for concavity, (iii), implies the first two, (i)-(ii). Therefore,  $\gamma \geq 0$ ,  $\varphi \geq 0$  and  $\nu \leq \gamma\varphi/(\gamma + \varphi)$  are necessary and sufficient conditions for concavity of preferences and joint non-inferiority of consumption and leisure. Finally notice that, by equations (28) in the main text and the associated coefficients (29), market consumption is non-inferior if and only if total consumption is non-inferior.

2.2. *Substitutability between consumption and leisure versus housework: an equivalence result*

140 Let  $\eta_{c_m,\lambda}$ ,  $\eta_{h_m,\lambda}$ ,  $\eta_{c_m,w}$  and  $\eta_{h_m,w}$  be the elasticities generated by the model for any given  $h_n$  and  $b_1$ . Then, a model with  $h_n = 0$  can be calibrated such that all its elasticities are equalized to  $\eta_{c_m,\lambda}$ ,  $\eta_{h_m,\lambda}$ ,  $\eta_{c_m,w}$  and  $\eta_{h_m,w}$  by choosing values of parameters  $\gamma$ ,  $\varphi$  and  $\nu$ .

**Proof** For  $h_n = 0$  the Frisch elasticities reported in Section 3.1 of the paper  
145 state

$$\eta_{c_m,\lambda} = -\frac{\varphi}{\varphi(\nu - \gamma) + \nu\gamma} \quad (73)$$

$$\eta_{h_m,\lambda} = \eta_{c_m,\lambda} \frac{\gamma}{\varphi} \quad (74)$$

$$\eta_{c_m,w} = \frac{\nu}{\varphi(\nu - \gamma) + \nu\gamma} \quad (75)$$

$$\eta_{h_m,w} = \eta_{c_m,w} + \eta_{h_m,\lambda} \quad (76)$$

From (74) we get

$$\varphi = \gamma \frac{\eta_{c_m,\lambda}}{\eta_{h_m,\lambda}} \quad (77)$$

which, combined with (73) yields the following expression

$$\nu = \frac{\gamma\eta_{c_m,\lambda} - 1}{\eta_{c_m,\lambda}\eta_{h_m,\lambda}} \quad (78)$$

Further combining (78) with (75) and (77) yields  $\gamma$  as a function of Frisch elasticities, only

$$\gamma = \frac{\eta_{h_m,\lambda}}{\eta_{c_m,\lambda}\eta_{h_m,\lambda} + \eta_{c_m,\lambda}\eta_{c_m,w} + \eta_{h_m,\lambda}\eta_{c_m,w}} \geq 0 \quad (79)$$

150 Equivalently, we can solve for  $\nu$  and  $\varphi$

$$\nu = \frac{\eta_{c_m,\lambda}}{\eta_{c_m,\lambda} + \eta_{h_m,\lambda}} \frac{\eta_{h_m,\lambda}}{\eta_{c_m,\lambda}\eta_{h_m,\lambda} + \eta_{c_m,\lambda}\eta_{c_m,w} + \eta_{h_m,\lambda}\eta_{c_m,w}} - \frac{1}{\eta_{c_m,\lambda}\eta_{h_m,\lambda}} \quad (80)$$

$$\varphi = \frac{\eta_{c_m,\lambda}}{\eta_{c_m,\lambda}\eta_{h_m,\lambda} + \eta_{c_m,\lambda}\eta_{c_m,w} + \eta_{h_m,\lambda}\eta_{c_m,w}} \geq 0 \quad (81)$$

Equality of the Frisch labor-supply elasticity between the model with and without the home sector follows from (76). Moreover, given  $\gamma \geq 0$  and  $\varphi \geq 0$ , for

non-inferiority of preferences we further need to show that  $\nu \leq \frac{\gamma\varphi}{\gamma+\varphi}$ , where

$$\frac{\gamma\varphi}{\gamma+\varphi} = \frac{\eta_{c_m,\lambda}\eta_{h_m,\lambda}}{(\eta_{c_m,\lambda} + \eta_{h_m,\lambda})(\eta_{c_m,\lambda}\eta_{h_m,\lambda} + \eta_{c_m,\lambda}\eta_{c_m,w} + \eta_{h_m,\lambda}\eta_{c_m,w})} \quad (82)$$

The necessary condition for non-inferiority reduces to

$$-\frac{1}{\eta_{c_m,\lambda}\eta_{h_m,\lambda}} < 0 \quad (83)$$

155 which, given  $\eta_{h_m,\lambda} > 0$  and  $\eta_{c_m,\lambda} > 0$  always holds. ■

From the canonical form discussed in Section 3.2 in the main text, it follows immediately that two models with the same elasticities  $\eta_{c_m,\lambda}$ ,  $\eta_{h_m,\lambda}$ ,  $\eta_{c_m,w}$  and  $\eta_{h_m,w}$  also generate the same dynamics for all market variables.

Figure 1 compares the utility parameters of a model with no housework and  
 160 arbitrary preferences  $U(C_t, l_t)$ , calibrated to deliver the same Frisch elasticities  
 as in the housework model for any level of complementarity,  $\eta_{C_m,w}$ . To begin  
 with, the parameterization of our model implies  $\gamma = 1$ ,  $\varphi = h/(1-h) = 1.08$   
 and  $\nu = h(1-\sigma) = -0.52$ , while  $b_1$  can be chosen to achieve any desired level of  
 complementarity. The top-left panel shows the elasticity of substitution between  
 165 home and market goods,  $1/(1-b_1)$ , as a function of complementarity. For any  
 level of complementarity, one can then use equations (29) in the main text to  
 recover all the Frisch elasticities implied by the housework model, while expres-  
 sions (B.15)-(B.17) yield parameters  $\gamma$ ,  $\varphi$  and  $\nu$  in the alternative model with  
 $h_n = 0$ . As extensively discussed by Bilbiie [2],  $\nu < 0$  measures substitutability  
 170 between consumption of market goods and leisure and, for given parameters  $\gamma$   
 and  $\varphi$ , fiscal multipliers increase with  $-\nu$ . In fact, substitutability between con-  
 sumption and leisure boosts complementarity between consumption and hours  
 worked. The bottom-right panel shows that for any level of complementarity  
 substitutability between consumption and leisure is always larger in the model  
 175 without housework, and more so the larger is complementarity. The intuition  
 is that when households are not allowed to substitute market work with house-  
 work, substitutability between consumption and leisure needs to be magnified  
 to obtain the same level of complementarity.

Discriminating across the two models by relying on the behavior of market  
180 variables is impossible, precisely because of the equivalence result: the model  
with  $h_n = 0$  is at least as plausible as ours, irrespective of parameter values.  
Quantifying the relative importance of the two substitution margins requires  
evidence on leisure and housework. Unfortunately, evidence on their Frisch  
elasticities is scant at best, leaving little guidance on the choice of utility pa-  
185 rameters, in addition to what can be inferred from market variables. Never-  
theless, data from the American Time Use Survey (ATUS) clearly suggest that  
substitutability of market work with housework is not only quantitatively rel-  
evant, but even stronger than substitutability with leisure: at business cycle  
frequencies the elasticity of substitution between housework and market work  
190 is roughly 0.5 and the one of leisure is around 0.15 (Aguiar et al. [1]). Neglect-  
ing the housework sector overstates substitutability between consumption and  
leisure.

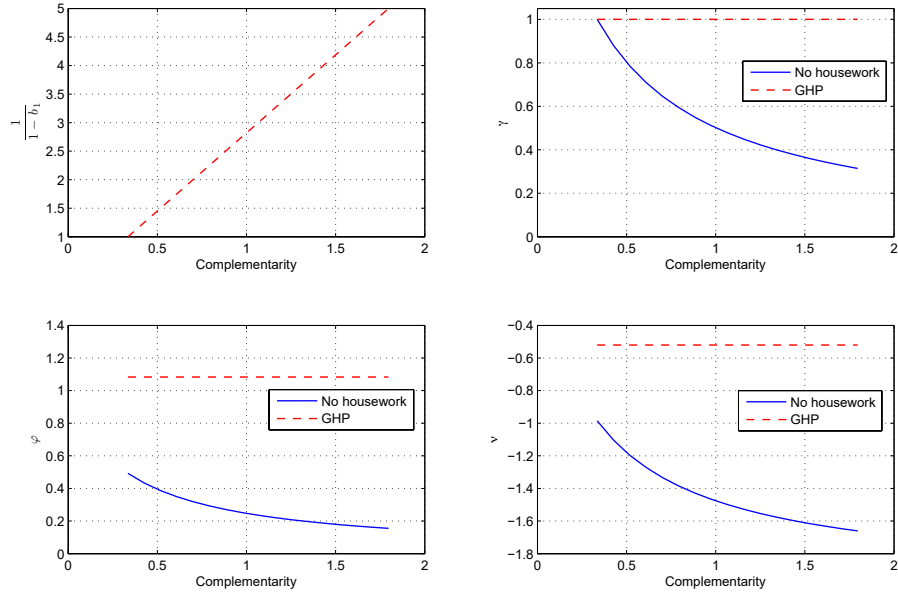


Figure 1: The top-left panel plots the value of the elasticity of substitution between home and market goods,  $1/(1 - b_1)$ , required to achieve a given level of complementarity between market consumption and hours worked in the housework model. The remaining panels plot parameters  $\gamma$ ,  $\varphi$ , and  $\nu$  for a model without housework calibrated to replicate the Frisch elasticities of the housework model (GHP) for given complementarity. For the sake of comparison, we also report the parameter values of the housework model.



### 2.3. Housework versus JR preferences

Consider the utility specification

$$U(C_t, l_t, X_{t-1}) = \frac{[C_t - \psi(1-l_t)^{\bar{\nu}} C_t^{\bar{\gamma}} X_{t-1}^{1-\bar{\gamma}}]^{1-\bar{\sigma}}}{1-\bar{\sigma}}, \quad X_t = C_t^{\bar{\gamma}} X_{t-1}^{1-\bar{\gamma}}, \quad X_{-1} = 1,$$

and assume  $h_{n,t} = 0$ , so that  $C_t = C_{m,t}$  and  $l_t = 1 - h_{m,t}$ . The marginal utility  
 195 of consumption is defined as

$$\lambda_t = U_C(C_t, l_t, X_{t-1}) \implies \lambda_t = [C_t - \psi h_t^{\bar{\nu}} C_t^{\bar{\gamma}} X_{t-1}^{1-\bar{\gamma}}]^{-\bar{\sigma}} \left(1 - \psi \bar{\gamma} h_t^{\bar{\nu}} C_t^{\bar{\gamma}-1} X_{t-1}^{1-\bar{\gamma}}\right), \quad (84)$$

and the solution to the households' problem needs to satisfy

$$\lambda_t W_t = U_l(C_t, l_t, X_{t-1}) \implies W_t = \frac{\bar{\nu} \psi h_t^{\bar{\nu}-1} C_t^{\bar{\gamma}} X_{t-1}^{1-\bar{\gamma}}}{1 - \psi \bar{\gamma} h_t^{\bar{\nu}} C_t^{\bar{\gamma}-1} X_{t-1}^{1-\bar{\gamma}}}, \quad (85)$$

so that equations (84) and (85) replace (3) and (5), respectively, while equation  
 (66) vanishes because of the assumption  $h_n = 0$ . As in the housework model  
 analyzed above, we keep assumptions  $K_m/Y = K_n/Y = G/Y = 0$ . Then,  
 200 log-linear relations (68) collapse to

$$\hat{\lambda}_t = (\nu - \gamma) \hat{C}_{m,t} - \nu \hat{h}_{m,t} + \frac{U_{C,X} X}{U_C} \hat{X}_{t-1} \quad (86)$$

$$\hat{W}_t = \nu \hat{C}_{m,t} - (\nu - \varphi) \hat{h}_{m,t} - \hat{\lambda}_t + \frac{U_{l,X} X}{U_l} \hat{X}_{t-1}$$

where  $\varphi$ ,  $\gamma$ , and  $\nu$ , defined as in (69), map into utility parameters as follows,

$$\varphi = \bar{\nu} + \bar{\gamma} - 1, \quad \gamma = \frac{\bar{\gamma}}{\bar{\nu}} (\bar{\nu} + \bar{\gamma} - 1), \quad \nu = \bar{\gamma} - \frac{\bar{\sigma} \bar{\nu}}{\bar{\nu} + \bar{\gamma} - 1},$$

and

$$\frac{U_{C,X} X}{U_C} = \frac{\bar{\sigma}(1-\bar{\gamma})}{\bar{\nu} + \bar{\gamma} - 1} - \frac{\bar{\gamma}(1-\bar{\gamma})}{\nu}, \quad \frac{U_{l,X} X}{U_l} = \frac{\bar{\sigma}(1-\bar{\gamma})}{\bar{\nu} + \bar{\gamma} - 1} - (1-\bar{\gamma}).$$

Solving for  $C_m$  and  $h_m$  yields equation (31) in the text with coefficients

$$\eta_{Cm,x} = -\eta_{Cm,W} \frac{1-\bar{\gamma}}{\bar{\nu}}, \quad \eta_{hm,x} = -(\eta_{hm,W} + 1) \frac{1-\bar{\gamma}}{\bar{\nu}}, \quad (87)$$

that are zero if and only if  $\bar{\gamma} = 0$ .

Given  $(1 - b_1)^{-1} \in [1, 5]$ , we choose parameters  $\bar{\nu}$ ,  $\bar{\sigma}$  and  $\bar{\gamma}$  in the JR model  
 in order to make the market consumption multiplier, the Frisch elasticity of  
 labor supply and the intertemporal elasticity of substitution equal across the  
 205 two models. Parameter  $\psi$  is calibrated to match hours worked on the market.  
 For  $(1 - b_1)^{-1} \in [1, 5]$ , figure 2 plots the following variables in both models after  
 an exogenous increase in government expenditure normalized to one percentage  
 point of steady-state GDP: fiscal multipliers, percentage deviations of leisure  
 210 from the steady state, Frisch elasticities  $\eta_{Cm,W}$  and  $\eta_{hm,\lambda}$ , and parameter  $\bar{\gamma}$ .  
 We find some interesting facts. First, matching the market consumption multi-  
 pplier also implies the same responses of output and hours worked. In addition,  
 for  $(1 - b_1)^{-1}$  between 1 and 2.25, values close to the microeconomic estimates,  
 complementarity and wealth effects are also identical across models, but they  
 215 diverge for large substitutability. In this respect, evidence on time use seems to  
 suggest values of  $\bar{\gamma}$  closer to KPR rather than GHH preferences. Finally, irre-  
 spective of substitutability, in the model with home production, an increase in  
 consumption expenditure is always associated with a fall in total consumption,  
 as compared to the JR model.

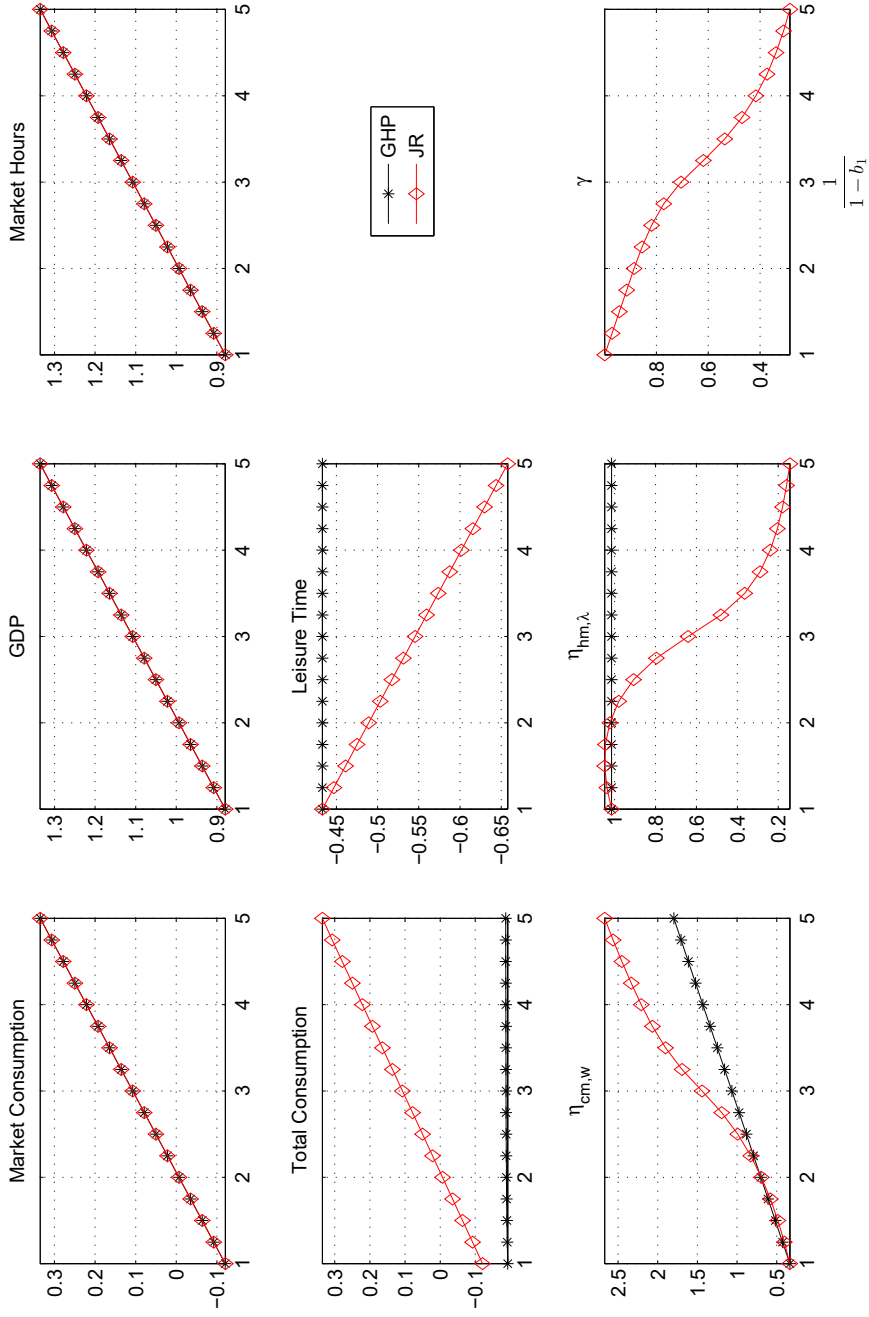


Figure 2: Comparison of fiscal multipliers, the percentage deviations of leisure from the steady state, and the two Frisch elasticities,  $\eta_{cm,w}$  and  $\eta_{hm,\lambda}$ , for different values of the elasticity of substitution between home and market goods,  $(1 - b_1)^{-1}$ , for the household model where  $K_m/Y = K_n/Y = G/Y = 0$ , labeled as GHP, and a baseline model with Jaimovich-Rebelo preferences (labeled as JR Preferences). Parameter  $\gamma$  in the JR model is calibrated to match the consumption multiplier in the GHP model.

Combining equations (28) in the main text immediately gives equation (32) and

$$\widehat{\lambda}_t = \frac{\eta_{Cm,W}}{\eta_{Cm,\lambda}} \widehat{W}_t - \frac{1}{\eta_{Cm,\lambda}} \widehat{C}_{m,t}, \quad (88)$$

while a first-order approximation of equation (15) yields

$$\widehat{\lambda}_t = E_t \widehat{\lambda}_{t+1} - E_t \pi_{t+1} + r_t + \log(\beta). \quad (89)$$

Equation (33) follows from combining (88) and (89). Using  $\widehat{Y}_t = \widehat{C}_{m,t} + \widehat{g}_t$  into (28) and (33) to substitute for  $\widehat{C}_{m,t}$  implies<sup>2</sup>

$$\begin{aligned} \widehat{W}_t &= \kappa \widehat{Y}_t - \kappa \frac{\eta_{hm,\lambda}}{\eta_{Cm,\lambda} + \eta_{hm,\lambda}} \widehat{g}_t, \\ \widehat{Y}_t &= E_t \widehat{Y}_{t+1} - \eta_{Cm,\lambda} (r_t - E_t \pi_{t+1} + \log(\beta)) - \eta_{Cm,W} (E_t \widehat{W}_{t+1} - \widehat{W}_t) \\ &\quad - (E_t \widehat{g}_{t+1} - \widehat{g}_t), \end{aligned} \quad (90)$$

where  $\kappa$  is defined as in equation (34), while from firms' optimality conditions,  $\widehat{RMC}_t = \widehat{W}_t$ . At the flexible-price equilibrium  $\widehat{RMC}_t = 0$  and the first equation in (90) imply the expression for  $y_t^n$  displayed in the text, which, substituted for  $\widehat{Y}_t$  in the second equation yields  $r_t^n$ . A conventional Phillips curve is obtained by log-linearizing firms' optimality condition (20),

$$\pi_t = \beta E_t \pi_{t+1} + \frac{(1-\theta)(1-\theta\beta)}{\theta} \widehat{RMC}_t$$

Using the fact  $\widehat{RMC}_t = 0$  at the flexible-price equilibrium, together with equations (90), the definitions of natural output, the natural interest rate and the output gap yields equations (34). We finally prove the statement in footnote 10. For simplicity define

$$\bar{\kappa} = \kappa \frac{(1-\theta)(1-\theta\beta)}{\theta}.$$

Let  $r_t^*$ ,  $\pi_t^*$  and  $y_t^*$  satisfy both the IS and the Phillips curve (34). Then, the locally unique solution to the system formed by equations (34) and the interest-rate rule  $r_t = r_t^* + \phi_\pi (\pi_t - \pi_t^*)$ , is  $r_t^*$ ,  $\pi_t^*$  and  $y_t^*$  for any  $\phi_\pi > 1$ . If indeed  $r_t^*$ ,

<sup>2</sup>Recall that  $G/Y = 0$ ,  $C/Y = 1$  and  $\widehat{g}_t = \frac{G_t}{Y_t}$ .

$\pi_t^*$  and  $y_t^*$  satisfy both the IS and the Phillips curve (34), the system formed by  
 230 equations (34) and the interest-rate rule can be written as

$$\begin{bmatrix} y_t - y_t^* \\ \pi_t - \pi_t^* \end{bmatrix} = \Omega \mathbf{A} E_t \begin{bmatrix} y_{t+1} - y_{t+1}^* \\ \pi_{t+1} - \pi_{t+1}^* \end{bmatrix} \quad (91)$$

where

$$\Omega = (\sigma + \bar{\kappa} \phi_\pi)^{-1} \quad (92)$$

$$\mathbf{A} = \begin{bmatrix} \sigma & 1 - \phi_\pi \beta \\ \sigma \bar{\kappa} & \bar{\kappa} + \beta \sigma \end{bmatrix} \quad (93)$$

The system has a unique solution if and only if the eigenvalues of matrix  $\mathbf{A}$  are both inside the unit circle. As Bullard and Mitra [5] show, this is the case if and only if  $\phi_\pi > 1$ . Hence,  $\phi_\pi > 1$  guarantees that  $y_t = y_t^*$  and  $\pi_t = \pi_t^*$  is the unique solution. Set

$$\begin{aligned} \pi_t^* &= \phi_g \hat{g}_t, \\ y_t^* &= \frac{\phi_g (1 - \beta \rho_g) \theta}{\kappa (1 - \theta) (1 - \theta \beta)} \hat{g}_t. \end{aligned}$$

and let  $r_t^*$  be derived by substituting  $\pi_t^*$  and  $y_t^*$  in the IS equation. It must then be the case that the locally unique solution to equations (34) and  $r_t =$   
 235  $r_t^* + \phi_\pi (\pi_t - \pi_t^*)$  is  $r_t^*$ ,  $\pi_t^*$  and  $y_t^*$ .

### 2.5. Welfare: consumption versus expenditure

In this section we study the role of houswork for the impact of government expenditure shocks on welfare. We follow the lines of [3] and use the nonlinear utility function together with the models' equilibrium conditions. Having  
 240 households' preferences defined over consumption and leisure, where

$$C_t = \left[ \alpha_1 C_{m,t}^{b_1} + (1 - \alpha_1) C_{n,t}^{b_1} \right]^{\frac{1}{b_1}}, \quad (94)$$

$$l_t = 1 - h_{m,t} - h_{n,t}, \quad (95)$$

$$C_{n,t} = h_{n,t}, \quad (96)$$

the derivative of welfare with respect to  $G_t$  states as

$$\begin{aligned} \frac{dU}{dG} &= \underbrace{U_c \alpha_1 \left( \frac{C_{m,t}}{C_t} \right)^{b_1-1} \frac{dC_m}{dG}}_A + \underbrace{U_c (1 - \alpha_1) \left( \frac{C_{n,t}}{C_t} \right)^{b_1-1} \frac{dh_n}{dG}}_B \\ &+ \underbrace{U_l \frac{dl}{dh_n} \frac{dh_n}{dG}}_C + \underbrace{U_l \frac{dl}{dh_m} \frac{dh_m}{dG}}_D \end{aligned}$$

with  $\frac{dl}{dh_n} = \frac{dl}{dh_m} = -1$ . From households' optimality conditions we have

$$\frac{U_l(C_t, l_t)}{U_c(C_t, l_t)} = W_t \alpha_1 \left( \frac{C_{m,t}}{C_t} \right)^{b_1-1} \quad (97)$$

$$\frac{U_l(C_t, l_t)}{U_c(C_t, l_t)} = (1 - \alpha_1) \left( \frac{C_{n,t}}{C_t} \right)^{b_1-1} \quad (98)$$

such that terms B and C cancel out and we are left with terms A and D, only.

$$\begin{aligned} \frac{dU}{dG} &= U_c \alpha_1 \left( \frac{C_{m,t}}{C_t} \right)^{b_1-1} \frac{dC_m}{dG} - U_l \frac{dh_m}{dG} \\ &= U_c \alpha_1 \left( \frac{C_{m,t}}{C_t} \right)^{b_1-1} \frac{dC_m}{dG} - W_t U_c \alpha_1 \left( \frac{C_{m,t}}{C_t} \right)^{b_1-1} \frac{dh_m}{dG} \\ &= U_c \alpha_1 \left( \frac{C_{m,t}}{C_t} \right)^{b_1-1} \left[ \frac{dC_m}{dG} - W_t \frac{dh_m}{dG} \right] \end{aligned} \quad (99)$$

The goods' market clearing condition and the resource constraint, respectively,

245 read

$$Y_t = C_{m,t} + G_t \quad (100)$$

$$Y_t = h_{m,t} \Delta_t \quad (101)$$

Combining (100) and (101) then yields

$$h_{m,t} = \Delta_t C_{m,t} + \Delta_t G_t \quad (102)$$

such that

$$\frac{dh_m}{dG} = \frac{dC_m}{dG} \Delta_t + \frac{d\Delta}{dG} C_{m,t} + \frac{d\Delta}{dG} G_t + \Delta_t \quad (103)$$

Finally, combining (99) with (103) yields

$$\begin{aligned}
\frac{dU}{dG} &= U_c \alpha_1 \left( \frac{C_{m,t}}{C_t} \right)^{b_1-1} \left[ \frac{dC_m}{dG} - W_t \left( \frac{dC_m}{dG} \Delta_t + \frac{d\Delta}{dG} C_{m,t} + \frac{d\Delta}{dG} G_t + \Delta_t \right) \right] \\
&= U_c \alpha_1 \left( \frac{C_{m,t}}{C_t} \right)^{b_1-1} W_t \Delta_t \left[ \left( \frac{1}{W_t \Delta_t} - 1 \right) \frac{dC_m}{dG} - \frac{C_{m,t}}{\Delta_t} \frac{d\Delta}{dG} - \frac{G_t}{\Delta_t} \frac{d\Delta}{dG} - 1 \right] \\
&= \lambda_t W_t \Delta_t \left[ \left( \frac{1}{W_t \Delta_t} - 1 \right) \frac{dC_m}{dG} - \frac{C_{m,t}}{\Delta_t} \frac{d\Delta}{dG} - \frac{G_t}{\Delta_t} \frac{d\Delta}{dG} - 1 \right] \quad (104)
\end{aligned}$$

### 3. Robustness: Modeling Assumptions

#### 250 3.1. Distortionary Taxation and CES Production Functions

In this section, we show that our findings continue to hold in the case of distortionary taxation on capital and labor, and in the more general case of constant elasticity of substitution (CES) production functions both in the home and the market sector

$$C_{n,t} = \left[ \alpha_2 (K_{n,t})^{b_2} + (1 - \alpha_2) (h_{n,t})^{b_2} \right]^{\frac{1}{b_2}}, \quad (105)$$

$$Y_t = \left[ \alpha_3 (K_{m,t})^{b_3} + (1 - \alpha_3) (h_{m,t})^{b_3} \right]^{\frac{1}{b_3}}, \quad (106)$$

Assuming the presence of distortionary taxes on capital and labor, which we assume not to respond to the shock since we focus on deficit spending, the household's budget constraint becomes

$$\begin{aligned}
&E_t \{Q_{t,t+1} B_{t+1}\} + P_t (C_{m,t} + I_t) \\
&\leq B_t + (1 - \tau_h) W_t P_t h_{m,t} + (1 - \tau_k) r_t^k P_t K_{m,t} + \delta \tau_k P_t K_{m,t} + T_t. \quad (107)
\end{aligned}$$

255 Accordingly, the household's intratemporal conditions, (42) - (44), and the Euler equation for the optimal intertemporal allocation of the capital stock, (45), are replaced by

$$\left( \frac{\alpha_1}{1 - \alpha_1} \right) \left( \frac{C_{m,t}}{C_{n,t}} \right)^{b_1-1} = \left( \frac{1 - \alpha_2}{W_t (1 - \tau_h)} \right) \left( \frac{C_{n,t}}{h_{n,t}} \right)^{1-b_2} \quad (108)$$

$$\left( \frac{\alpha_1}{1 - \alpha_1} \right) \left( \frac{C_{m,t}}{C_{n,t}} \right)^{b_1-1} = \left( \frac{\alpha_2}{(1 - \tau_k) r_t^k + \delta \tau_k} \right) \left( \frac{C_{n,t}}{K_{n,t}} \right)^{1-b_2} \quad (109)$$

$$W_t (1 - \tau_h) (1 - h_{n,t} - h_{m,t}) = \left( \frac{1 - b}{b \alpha_1} \right) C_{m,t}^{1-b_1} C_t^{b_1} \quad (110)$$

$$\beta E_t \left\{ \frac{\lambda_{t+1}}{\lambda_t} \left[ 1 + \frac{\xi}{K_t} \left( \frac{K_{t+1}}{K_t} - 1 \right) \right]^{-1} \right. \\ \left. \left[ 1 - \delta + \xi \left( \frac{K_{t+2}}{K_{t+1}} - 1 \right) \left( \frac{K_{t+2}}{K_{t+1}^2} \right) + (1 - \tau_k) r_{t+1}^k + \delta \tau_k \right] \right\} = 1 \quad (111)$$

The firms' optimality conditions, (53) and (54), become

$$\alpha_3 RMC_t \left( \frac{K_{m,t}(i)}{Y_t(i)} \right)^{b_3-1} = r_t^k \quad (112)$$

$$(1 - \alpha_3) RMC_t \left( \frac{h_{m,t}(i)}{Y_t(i)} \right)^{b_3-1} = W_t. \quad (113)$$

260 with (52) being replaced by

$$Y_t = \Delta_t^{-1} \left[ \alpha_3 (K_{m,t})^{b_3} + (1 - \alpha_3) (h_{m,t})^{b_3} \right]^{\frac{1}{b_3}} \quad (114)$$

For the definition of the equilibrium with distortionary taxation and CES production functions we further replace (39) by (105). All remaining equilibrium conditions, as defined in Appendix 1.4, remain unaffected. We set tax rates according to the base case in McGrattan, Rogerson and Wright [11], i.e.,  $\tau_k = 0.55$  265 and  $\tau_h = 0.24$ , and set  $b_2 = 0.269$  and  $b_3 = 0.054$  according to the estimates in McGrattan et al. [11]. Figure 3 shows that the relative performance of our model, labeled as ‘‘GHP,’’ compared to a counterfactual model, labeled as ‘‘No Home Sector,’’ where hours worked and capital in the home sector are set to zero, is unaffected by the presence of distortionary taxes and by the assumption 270 of CES production functions in both sectors.

### 3.2. External Habits in Consumption

In this section we analyze the implications of external habit formation. Households' period utility function now reads

$$U(\tilde{C}_t, h_{n,t}, h_{m,t}) = \frac{\left[ \left( \tilde{C}_t \right)^b (1 - h_{n,t} - h_{m,t})^{1-b} \right]^{1-\sigma} - 1}{1 - \sigma} \quad (115)$$

where

$$\tilde{C}_t \equiv C_t - hC_{t-1}^A \quad (116)$$



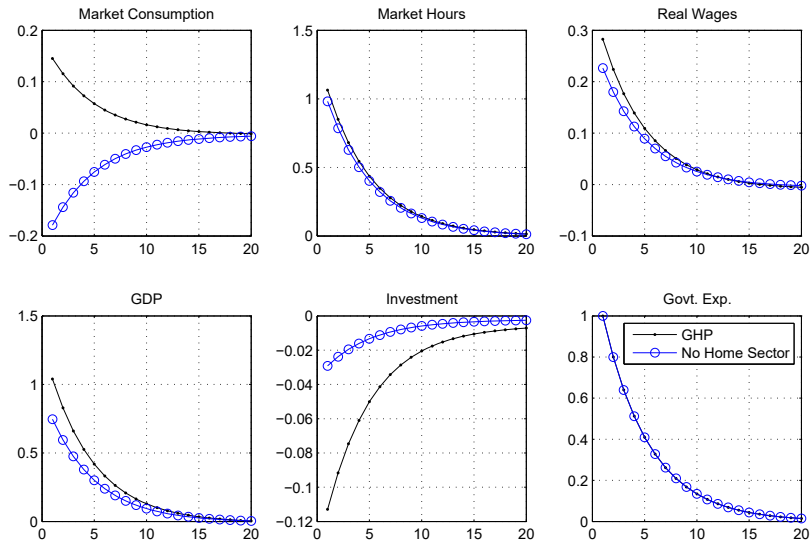


Figure 3: Impulse responses with distortionary taxation,  $\tau_k = 0.55$  and  $\tau_h = 0.24$ , and CES production functions both in the market ( $b_2 = 0.269$ ) and the home sector ( $b_3 = 0.054$ ). All remaining parameters are calibrated as in Table 1 in the main text.

275 with  $h > 0$  being the habit persistence parameter, and  $C_{t-1}^A$  representing past, aggregate consumption, which is taken as given by the household. The corresponding Lagrangian is now given by

$$\begin{aligned} \mathcal{L} = E_0 \sum_{t=0}^{\infty} \beta^t & \frac{\left[ \left[ \alpha_1 (C_{m,t})^{b_1} + (1 - \alpha_1) (C_{n,t})^{b_1} \right]^{\frac{1}{b_1}} - h C_{t-1}^A \right]^b (1 - h_{n,t} - h_{m,t})^{1-b}}{1 - \sigma}^{1-\sigma} - 1 \\ & + \mu_t \left[ (K_{n,t})^{\alpha_2} (h_{n,t})^{1-\alpha_2} - C_{n,t} \right] \\ & + \gamma_t [K_t - K_{m,t} - K_{n,t}] \\ & + \frac{\lambda_t}{P_t} \left\{ B_t + W_t P_t h_{m,t} + r_t^k P_t K_{m,t} + T_t - E_t \{ Q_{t,t+1} B_{t+1} \} - P_t C_{m,t} \right. \\ & \left. - P_t \left[ K_{t+1} + (1 - \delta) K_t + \frac{\xi}{2} \left( \frac{K_{t+1}}{K_t} - 1 \right)^2 \right] \right\} \end{aligned}$$

The corresponding first-order conditions are:

$$\{C_{m,t}\} : \lambda_t = b \alpha_1 (1 - h_{n,t} - h_{m,t})^{(1-b)(1-\sigma)} \tilde{C}_t^{b(1-\sigma)-1} \left( \frac{C_{m,t}}{C_t} \right)^{b_1-1} \quad (117)$$

$$\{C_{n,t}\} : \mu_t = b(1 - \alpha_1) (1 - h_{n,t} - h_{m,t})^{(1-b)(1-\sigma)} \tilde{C}_t^{b(1-\sigma)-1} \left( \frac{C_{n,t}}{C_t} \right)^{b_1-1} \quad (118)$$

$$\{h_{m,t}\} : \lambda_t W_t = (1 - b) \tilde{C}_t^{b(1-\sigma)} (1 - h_{n,t} - h_{m,t})^{(1-b)(1-\sigma)-1} \quad (119)$$

$$\{h_{n,t}\} : \mu_t (1 - \alpha_2) \left( \frac{C_{n,t}}{h_{n,t}} \right) = (1 - b) \tilde{C}_t^{b(1-\sigma)} (1 - h_{n,t} - h_{m,t})^{(1-b)(1-\sigma)-1} \quad (120)$$

280 The remaining first-order conditions, (7) - (10), remain unaffected when assuming external habit persistence in households' utility function. Combining these new first-order conditions as in Appendix 1.1 yields the same equilibrium conditions as for our baseline model, except for the expression defining the marginal utility of wealth (47) and the optimality condition solving for the consumption-leisure tradeoff (44)

$$W_t (1 - h_{n,t} - h_{m,t}) = \left( \frac{1 - b}{b \alpha_1} \right) \tilde{C}_t \left( \frac{C_{m,t}}{C_t} \right)^{1-b_1} \quad (121)$$

285 The equilibrium with external habit formation is thus defined as in Appendix 1.4, except for (44) and (47), which are replaced by (121) and (117), respectively, and with  $\tilde{C}_t \equiv C_t - hC_{t-1}$ , given that in equilibrium  $C_{t-1} = C_{t-1}^A$ . In the vein of Appendix 1.5 the corresponding Frisch system states as:

$$\begin{aligned}
f1 &= b\alpha_1(1 - h_{n,t} - h_{m,t})^{(1-b)(1-\sigma)}(C_t - hC_{t-1})^{b(1-\sigma)-1} \left(\frac{C_{m,t}}{C_t}\right)^{b_1-1} - \lambda_t \\
f2 &= (1-b)(C_t - hC_{t-1})^{b(1-\sigma)}(1 - h_{n,t} - h_{m,t})^{(1-b)(1-\sigma)-1} - \lambda_t W_t \\
f3 &= (1 - h_{n,t} - h_{m,t})b(1 - \alpha_1)(1 - \alpha_2) \frac{C_{n,t}^{b_1}}{h_{n,t}} - (1-b)C_t^{b_1-1}(C_t - hC_{t-1}) \\
f4 &= b(1 - \alpha_1)\alpha_2(1 - h_{n,t} - h_{m,t})^{(1-b)(1-\sigma)}(C_t - hC_{t-1})^{b(1-\sigma)-1} C_t^{1-b_1} \frac{C_{n,t}^{b_1}}{K_{n,t}} - r_t^k \lambda_t \\
f5 &= [\alpha_1(C_{m,t})^{b_1} + (1 - \alpha_1)(C_{n,t})^{b_1}]^{\frac{1}{b_1}} - C_t \\
f6 &= (K_{n,t})^{\alpha_2} (h_{n,t})^{1-\alpha_2} - C_{n,t}
\end{aligned}$$

where  $y_t = \{C_{m,t}, C_{n,t}, C_t, h_{m,t}, h_{n,t}, K_{n,t}\}$  are the choice variables, whereas  
290  $x_t = \{\lambda_t, W_t, r_t^K, C_{t-1}\}$  are taken as given. As for the baseline housework model, we define  $f = [f1; f2; f3; f4; f5; f6]$  and the matrix of unknown derivatives we are interested in

$$Z_{y,x} = \begin{pmatrix} \frac{\partial C_{m,t}}{\partial \lambda_t} & \frac{\partial C_{m,t}}{\partial W_t} & \frac{\partial C_{m,t}}{\partial r_t^k} & \frac{\partial C_{m,t}}{\partial C_{t-1}} \\ \frac{\partial C_{n,t}}{\partial \lambda_t} & \frac{\partial C_{n,t}}{\partial W_t} & \frac{\partial C_{n,t}}{\partial r_t^k} & \frac{\partial C_{n,t}}{\partial C_{t-1}} \\ \frac{\partial C_t}{\partial \lambda_t} & \frac{\partial C_t}{\partial W_t} & \frac{\partial C_t}{\partial r_t^k} & \frac{\partial C_t}{\partial C_{t-1}} \\ \frac{\partial h_{m,t}}{\partial \lambda_t} & \frac{\partial h_{m,t}}{\partial W_t} & \frac{\partial h_{m,t}}{\partial r_t^k} & \frac{\partial h_{m,t}}{\partial C_{t-1}} \\ \frac{\partial h_{n,t}}{\partial \lambda_t} & \frac{\partial h_{n,t}}{\partial W_t} & \frac{\partial h_{n,t}}{\partial r_t^k} & \frac{\partial h_{n,t}}{\partial C_{t-1}} \\ \frac{\partial K_{n,t}}{\partial \lambda_t} & \frac{\partial K_{n,t}}{\partial W_t} & \frac{\partial K_{n,t}}{\partial r_t^k} & \frac{\partial K_{n,t}}{\partial C_{t-1}} \end{pmatrix} \quad (122)$$

We then solve the following system for matrix  $Z_{y,x}$

$$\begin{matrix} J_y & Z_{y,x} & + & J_x & = & 0, \\ 6*6 & 6*3 & & 6*3 & & \end{matrix} \quad (123)$$

where  $J_y$  is the Jacobian matrix of function  $f$  with respect to the control variables, and  $J_x$  is the Jacobian matrix of function  $f$  with respect to the state  
295 variables.

### 3.3. Internal Habits in Consumption

While in Appendix 3.2 we analyze external habits, in this section we study the implications of internal habit formation. Households' period utility function is defined as

$$U(\bar{C}_t, h_{n,t}, h_{m,t}) = \frac{\left[ (\bar{C}_t)^b (1 - h_{n,t} - h_{m,t})^{1-b} \right]^{1-\sigma} - 1}{1 - \sigma} \quad (124)$$

where

$$\bar{C}_t \equiv C_t - hC_{t-1} \quad (125)$$

with  $h > 0$  being the habit persistence parameter. Different from the case of external habits, the internal habit stock represents the household's own past consumption,  $C_{t-1}$ . The corresponding Lagrangian is now given by

$$\begin{aligned} \mathcal{L} = E_0 \sum_{t=0}^{\infty} \frac{\beta^t}{(1-\sigma)} & \left\{ \left[ [\alpha_1 (C_{m,t})^{b_1} + (1-\alpha_1)(C_{n,t})^{b_1}]^{\frac{1}{b_1}} - h [\alpha_1 (C_{m,t-1})^{b_1} + (1-\alpha_1)(C_{n,t-1})^{b_1}]^{\frac{1}{b_1}} \right]^b \right. \\ & \left. (1 - h_{n,t} - h_{m,t})^{1-b} \right\}^{1-\sigma} - 1 \\ & + \mu_t \left[ (K_{n,t})^{\alpha_2} (h_{n,t})^{1-\alpha_2} - C_{n,t} \right] \\ & + \gamma_t [K_t - K_{m,t} - K_{n,t}] \\ & + \frac{\lambda_t}{P_t} \left\{ B_t + W_t P_t h_{m,t} + r_t^k P_t K_{m,t} + T_t - E_t \{ Q_{t,t+1} B_{t+1} \} - P_t C_{m,t} \right. \\ & \left. - P_t \left[ K_{t+1} + (1-\delta)K_t + \frac{\xi}{2} \left( \frac{K_{t+1}}{K_t} - 1 \right)^2 \right] \right\} \end{aligned}$$

The only first-order conditions that are different compared to the external-habit model are the first-order conditions with respect to market and non-market consumption ( $C_{m,t}$  and  $C_{n,t}$ , respectively).

$$\{C_{m,t}\} : \lambda_t = b\alpha_1 \left( \frac{C_{m,t}}{C_t} \right)^{b_1-1} \left[ l_t^{(1-b)(1-\sigma)} (\bar{C}_t)^{b(1-\sigma)-1} - \beta h l_{t+1}^{(1-b)(1-\sigma)} (\bar{C}_{t+1})^{b(1-\sigma)-1} \right] \quad (126)$$

where  $l_t = 1 - h_{n,t} - h_{m,t}$ . Different to the baseline model and the case of external habit formation, when the stock of habits is internal the marginal utility  
 310 of wealth ( $\lambda_t$ ) is no longer equal to the marginal utility of market consumption ( $U_{C_{m,t}}$ ). Moreover, the marginal utility of wealth becomes a dynamic equation, depending on expected marginal utility of market consumption ( $U_{C_{m,t+1}}$ ) and on expected consumption levels.

$$\{C_{n,t}\} : \mu_t = b(1 - \alpha_1) \left( \frac{C_{n,t}}{C_t} \right)^{b_1 - 1} \left[ l_t^{(1-b)(1-\sigma)} (\overline{C}_t)^{b(1-\sigma) - 1} - \beta h l_{t+1}^{(1-b)(1-\sigma)} (\overline{C}_{t+1})^{b(1-\sigma) - 1} \right] \quad (127)$$

We can then combine the first-order conditions as in our baseline model (see Ap-  
 315 pendix 1.1). The resulting equilibrium equations coincide with the ones for our baseline model (and with the ones for the model with external habits), except for the expression for marginal utility of wealth and the optimality condition solving for the consumption-leisure tradeoff.

$$W_t(1 - h_{n,t} - h_{m,t}) = \left( \frac{1 - b}{b\alpha_1} \right) \overline{C}_t \left( \frac{C_{m,t}}{C_t} \right)^{1 - b_1} \left[ 1 - \beta h \left( \frac{l_{t+1}}{l_t} \right)^{(1-b)(1-\sigma)} \left( \frac{\overline{C}_{t+1}}{\overline{C}_t} \right)^{b(1-\sigma) - 1} \right]^{-1} \quad (128)$$

Equivalent to the case of external habits, the equilibrium with internal habit  
 320 formation is thus defined as in Appendix 1.4, except for (44) and (47), which are replaced by (128) and (126), respectively, and with  $\overline{C}_t \equiv C_t - hC_{t-1}$ . The

corresponding Frisch system states as:

$$\begin{aligned}
f1 &= b\alpha_1 \left( \frac{C_{m,t}}{C_t} \right)^{b_1-1} \left[ l_t^{(1-b)(1-\sigma)} (C_t - hC_{t-1})^{b(1-\sigma)-1} - \beta h l_{t+1}^{(1-b)(1-\sigma)} (C_{t+1} - hC_t)^{b(1-\sigma)-1} \right] \\
&\quad - \lambda_t \\
f2 &= (1-b)(C_t - hC_{t-1})^{b(1-\sigma)} l_t^{(1-b)(1-\sigma)-1} - \lambda_t W_t \\
f3 &= \left[ l_t^{(1-b)(1-\sigma)} (C_t - hC_{t-1})^{b(1-\sigma)-1} - \beta h l_{t+1}^{(1-b)(1-\sigma)} (C_{t+1} - hC_t)^{b(1-\sigma)-1} \right] \\
&\quad b(1-\alpha_1)(1-\alpha_2) \frac{C_{n,t}^{b_1}}{h_{n,t}} - (1-b)C_t^{b_1-1} (C_t - hC_{t-1})^{b(1-\sigma)} l_t^{(1-b)(1-\sigma)-1} \\
f4 &= \left[ l_t^{(1-b)(1-\sigma)} (C_t - hC_{t-1})^{b(1-\sigma)-1} - \beta h l_{t+1}^{(1-b)(1-\sigma)} (C_{t+1} - hC_t)^{b(1-\sigma)-1} \right] \\
&\quad b(1-\alpha_1)\alpha_2 \frac{C_{n,t}^{b_1}}{K_{n,t}} C_t^{1-b_1} - r_t^k \lambda_t \\
f5 &= \left[ \alpha_1 (C_{m,t})^{b_1} + (1-\alpha_1)(C_{n,t})^{b_1} \right]^{\frac{1}{b_1}} - C_t \\
f6 &= (K_{n,t})^{\alpha_2} (h_{n,t})^{1-\alpha_2} - C_{n,t} \\
f7 &= l_t - (1 - h_{n,t} - h_{m,t})
\end{aligned}$$

where  $y_t = \{C_{m,t}, C_{n,t}, C_t, h_{m,t}, h_{n,t}, K_{n,t}, l_t\}$  are the choice variables, whereas  $x_t = \{\lambda_t, W_t, r_t^K, K_t, C_{t-1}\}$  are taken as given. As for the baseline housework model, we define  $f = [f1; f2; f3; f4; f5; f6]$  and the matrix of unknown derivatives we are interested in

$$Z_{y,x} = \begin{pmatrix} \frac{\partial C_{m,t}}{\partial \lambda_t} & \frac{\partial C_{m,t}}{\partial W_t} & \frac{\partial C_{m,t}}{\partial r_t^k} & \frac{\partial C_{m,t}}{\partial C_{t-1}} \\ \frac{\partial C_{n,t}}{\partial \lambda_t} & \frac{\partial C_{n,t}}{\partial W_t} & \frac{\partial C_{n,t}}{\partial r_t^k} & \frac{\partial C_{n,t}}{\partial C_{t-1}} \\ \frac{\partial C_t}{\partial \lambda_t} & \frac{\partial C_t}{\partial W_t} & \frac{\partial C_t}{\partial r_t^k} & \frac{\partial C_t}{\partial C_{t-1}} \\ \frac{\partial h_{m,t}}{\partial \lambda_t} & \frac{\partial h_{m,t}}{\partial W_t} & \frac{\partial h_{m,t}}{\partial r_t^k} & \frac{\partial h_{m,t}}{\partial C_{t-1}} \\ \frac{\partial h_{n,t}}{\partial \lambda_t} & \frac{\partial h_{n,t}}{\partial W_t} & \frac{\partial h_{n,t}}{\partial r_t^k} & \frac{\partial h_{n,t}}{\partial C_{t-1}} \\ \frac{\partial K_{n,t}}{\partial \lambda_t} & \frac{\partial K_{n,t}}{\partial W_t} & \frac{\partial K_{n,t}}{\partial r_t^k} & \frac{\partial K_{n,t}}{\partial C_{t-1}} \\ \frac{\partial l_t}{\partial \lambda_t} & \frac{\partial l_t}{\partial W_t} & \frac{\partial l_t}{\partial r_t^k} & \frac{\partial l_t}{\partial C_{t-1}} \end{pmatrix} \quad (129)$$

We then solve the following system for matrix  $Z_{y,x}$

$$\begin{matrix} J_y & Z_{y,x} & + & J_x & = & 0, \\ 6*6 & 6*3 & & 6*3 & & \end{matrix} \quad (130)$$

where  $J_y$  is the Jacobian matrix of function  $f$  with respect to the control variables, and  $J_x$  is the Jacobian matrix of function  $f$  with respect to the state

330 variables.

### 3.4. Real Wage Rigidity

We consider real wage rigidities as in Blanchard and Galí [4]. Hence, we assume that real wages respond sluggishly to labor market conditions, as a result of some unmodelled frictions in labor markets. Specifically, we assume

$$\begin{aligned} w_t &= \omega w_{t-1} + (1 - \omega) mrs_t \\ w_t &= \omega w_{t-1} + (1 - \omega) \ln \left[ \left( \frac{1 - b}{b\alpha_1} \right) \left( \frac{C_{m,t}^{1-b_1} C_t^{b_1}}{(1 - h_{n,t} - h_{m,t})} \right) \right] \end{aligned} \quad (131)$$

335 where  $w_t = \ln(W_t)$  represents the natural logarithm of the real wage and  $mrs_t = -\frac{U_{h_{m,t}}}{U_{c_{m,t}}}$  the logarithm of the marginal rate of substitution between hours worked on the market and market consumption. The equilibrium with real wage rigidities is thus defined as in Appendix 1.4, except for (44) which is replaced by (131).

## 340 4. Robustness: Monetary Policy Rules

In this section, we assess the robustness of our findings to two additional monetary policy rules for which we repeat the exercise presented in Section 4.4 of the paper, following Canova and Paustian [7]. In particular, we consider the following monetary policy rules.

- 345 • **Taylor Rule with Output (in deviation from steady state) and Interest Rate Smoother (Rule 1):**

$$(1 + R_t) = (1 + R_{t-1})^{\rho_m} \left( \beta^{-1} \Pi_t^{\Phi_\pi} \left( \frac{Y_t}{Y} \right)^{\Phi_Y} \right)^{1 - \rho_m} \quad (132)$$

Among others, this rule has been considered by Del Negro and Schorfheide [8], Rabanal and Rubio-Ramírez [12], Del Negro, Schorfheide, Smets and Wouters [9], and Canova and Paustian [7].

- 350 • **Simple Taylor Rule with Interest Rate Smoother (Rule 2):**

$$(1 + R_t) = (1 + R_{t-1})^{\rho_m} \left( \beta^{-1} \Pi_t^{\Phi_\pi} \right)^{1 - \rho_m} \quad (133)$$

We take 50,000 draws from uniform distributions of the following parameters, with their respective bounds:  $\theta \in [0.2, 0.9]$ ,  $\sigma \in [1, 4]$ ,  $\xi \in [0, 500]$ ,  $\rho_m \in [0, 0.9]$ ,  $\Phi_\pi \in [1.05, 2.5]$ ,  $\rho_g \in [0, 0.95]$  and  $\Phi_Y \in [0, 0.1]$  for Rule 1. All the other parameters are chosen as in Table 1 in the main text. As it becomes clear from 355 figure 4, the two monetary policy rules do not differ significantly from our main specification.



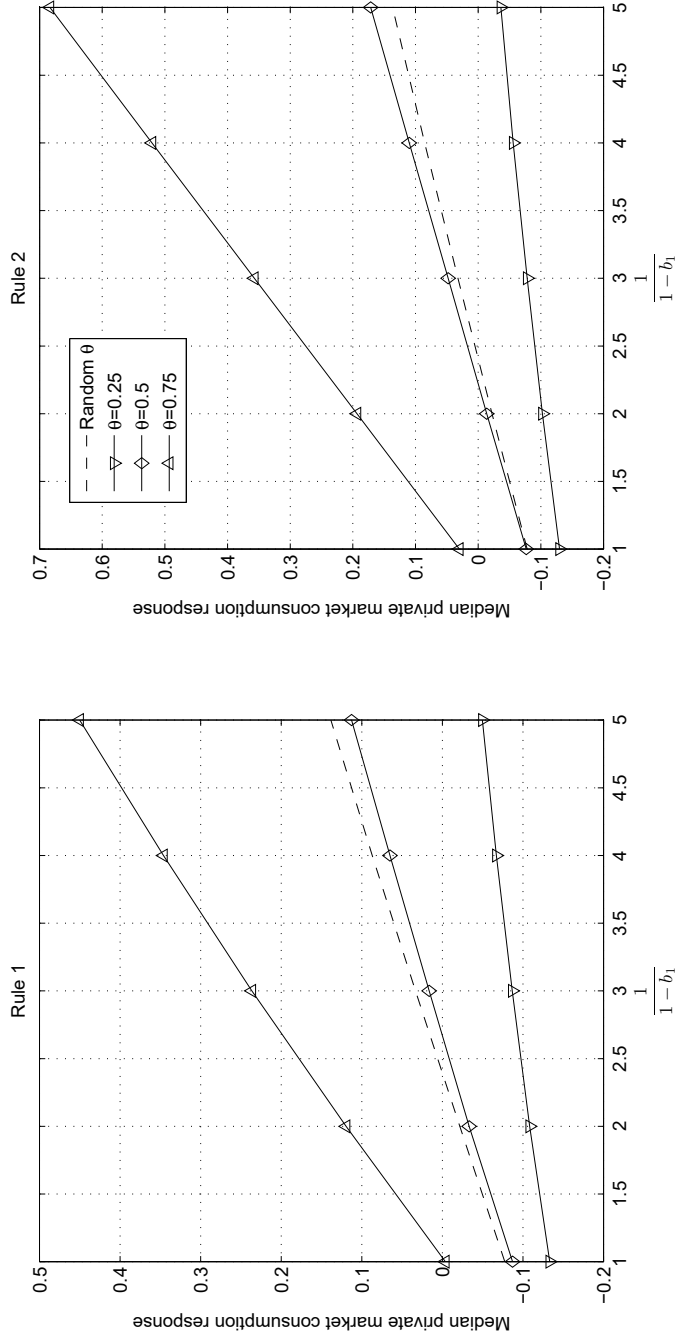


Figure 4: Robustness analysis on the monetary policy rule. Median responses to a  $G$  shock for 50,000 draws from uniform distributions of the following parameters, with their respective bounds, as summarized in Table 1 in the paper:  $\theta \in [0.2, 0.9]$ ,  $\sigma \in [1, 4]$ ,  $\xi \in [0, 0.9]$ ,  $\Phi_\pi \in [0, 0.9]$ ,  $\Phi_\pi \in [1.05, 2.5]$ ,  $\rho_g \in [0, 0.95]$  and  $\Phi_Y \in [0, 0.1]$  for Rule 1. All the other parameters are chosen as in Table 1 in the main text.

## References

- [1] **Aguiar, Mark, Erik Hurst, and Loukas Karabarbounis**, “Time Use During the Great Recession,” *The American Economic Review*, 2013, *103* (5), 1664–1696.
- [2] **Bilbiie, Florin**, “Nonseparable Preferences, Frisch Labor Supply, and the Consumption Multiplier of Government Spending: One Solution to a Fiscal Policy Puzzle,” *Journal of Money, Credit and Banking*, 2011, *43* (1), 221–251.
- [3] — , **Tommaso Monacelli, and Roberto Perotti**, “Is Government Spending at the Zero Lower Bound Desirable?,” 2014, (20687).
- [4] **Blanchard, Olivier and Jordi Galí**, “Real wage rigidities and the New Keynesian model,” *Journal of Money, Credit and Banking*, 2007, *39* (1), 35–65.
- [5] **Bullard, James and Kaushik Mitra**, “Learning About Monetary Policy Rules,” *Journal of Monetary Economics*, 2002, *49*, 1105–1129.
- [6] **Calvo, Guillermo**, “Staggered Prices in a Utility Maximizing Framework,” *Journal of Monetary Economics*, 1983, *12* (3), 383–398.
- [7] **Canova, Fabio and Matthias Paustian**, “Business Cycle Measurement with Some Theory,” *Journal of Monetary Economics*, 2011, *58* (4), 345–361.
- [8] **Del Negro, Marco and Frank Schorfheide**, “Priors from General Equilibrium Models for VARS,” *International Economic Review*, 2004, *45* (2), 643–673.
- [9] — , — , **Frank Smets, and Rafael Wouters**, “On the Fit of New Keynesian Models,” *Journal of Business and Economic Statistics*, 2007, *25* (2), 123–143.

- [10] **Frisch, Ragnar**, “A Complete Scheme for Computing All Direct and Cross Demand Elasticities in a Model with Many Sectors,” *Econometrica*, 1959, 27, 177–196.
- 385
- [11] **McGrattan, Ellen, Richard Rogerson, and Randall Wright**, “An Equilibrium Model of the Business Cycle with Household Production and Fiscal Policy,” *International Economic Review*, 1997, 38, 267–290.
- [12] **Rabanal, Pau and Juan Rubio-Ramírez**, “Comparing New Keynesian Models of the Business Cycle: A Bayesian Approach,” *Journal of Monetary Economics*, 2005, 52 (6), 1151–1166.
- 390