

This is a postprint version of the following published document:

Rodríguez-Sánchez, M. R., Leray, C., Toutant, A., Ferriere, A. & Olalde, G. (2019). Development of a new method to estimate the incident solar flux on central receivers from deteriorated heliostats. *Renewable Energy*, vol. 130, pp. 182–190.

DOI: [10.1016/j.renene.2018.06.056](https://doi.org/10.1016/j.renene.2018.06.056)

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**1 Development of a new method to estimate the incident solar flux on central receivers from**  
**2 deteriorated heliostats**

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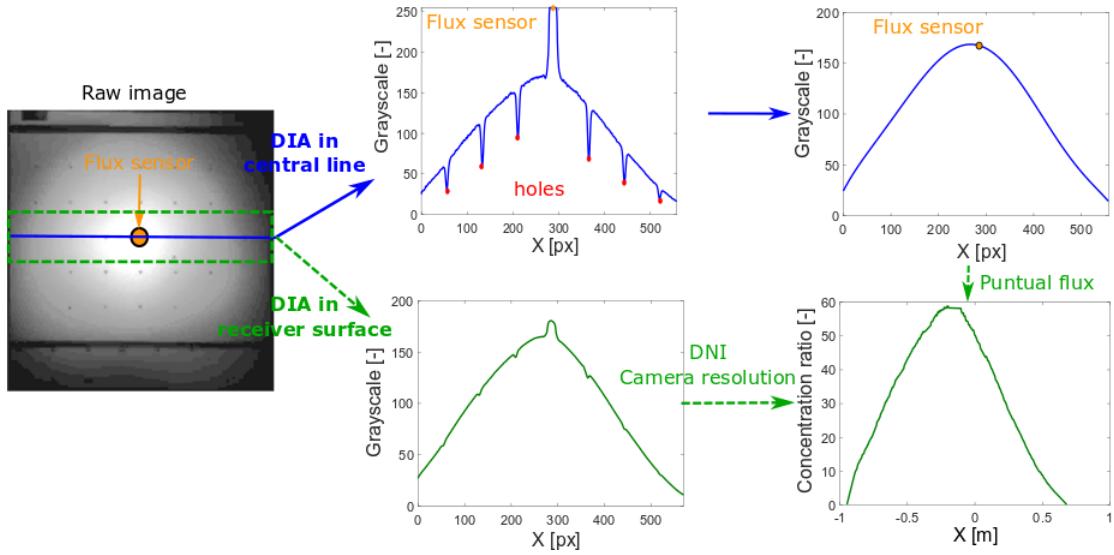
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## 13 Graphical abstract



15 Abstract

16 This work proposes a new empirical direct methodology to estimate both the solar flux  
17 distribution and intensity on the surface of central receivers. In solar power tower plants with  
18 deteriorated heliostats, the numerical simulations to estimate the incident solar flux are not  
19 precise. Hence the thermal behaviour of the receivers cannot be determined. In those cases,  
20 direct measurement or semi-empirical methodologies are required to characterize the radiant  
21 power on the receiver.

1 The new methodology proposed, named “*Superposition method*”, consists in the hourly  
2 characterization of the reflected solar beam of each individual heliostat by means of a  
3 pyrheliometer, a passive screen, a flux sensor, a camera and digital image analysis. According to  
4 the aiming strategy used during receiver operation, each individual solar flux distribution and  
5 intensity can be gathered to obtain the total incident radiant power on the solar receiver. This  
6 non-real-time method has the advantage of reproducing any solar flux distribution on the  
7 receiver at present and past time.

8 **Keywords**

9 Solar power tower; Heliostat; Incident solar flux; Digital image analysis.

10 **1. Introduction**

11 Concentrated Solar Power (CSP) is one of the most promising clean energy technologies in the  
12 modern society. While solar energy offers the highest renewable energy potential to our planet,  
13 CSP can provide dispatchable power in a technically and economically viable way by means of  
14 thermal energy storage and/or hybridization (European energy research alliance, 2014).  
15 However, the knowledge of this kind of plant has to be improved to operate them in a safely  
16 way.

17 One of the main problems of this kind of plants is associated with the measurement of the  
18 incident radiant power on the receiver, without perturbing the power plant operation. The  
19 accurate evaluation of the incident solar flux is very important to manage the plant and to  
20 determine its performance. If the radiant power per unit area is not high enough the thermal  
21 load capacity decreases and the cost of the electricity increases; while if the radiant power per  
22 unit area is too high or is bad distributed it can damage the receiver.

23 Numerous numerical tools have been developed to estimate the incident solar flux during the  
24 receiver operation (N.C. Cruz et al., 2017). They can be divided into two main categories (Garcia  
25 et al., 2008): Montecarlo Ray Tracing and convolution methods. The first one consists in a  
26 statistical approach that traces a bundle of random rays from the sun, and it is characterized by  
27 a high computational cost. Codes as MIRVAL (Leary and Hankins, 1979), SolTrace (Wendelin,  
28 2003), Tonatiuh (Blanco et al., 2005), Stral (Belhomme et al., 2009) and Solfast (Roccia et al.,  
29 2012) belong to this category. The second category is an approximation methodology based on  
30 mathematical superposition and convolution of error cones, characterized by a low  
31 computational cost, being some of the most popular codes HFLCAL (Schwarzbözl et al., 2009),  
32 DELSOL3 (Kistler, 1986), UNIZAR and CAMPO (Collado, 2010; Collado and Guallar, 2012), SPTflux

1 (Sánchez-González and Santana, 2015), PSO (Piroozmand and Boroushaki, 2016) and ParHel (N.  
2 C. Cruz et al., 2017).

3 Previous methodologies can be deficient when the heliostats are not well aligned, when they  
4 are imperfect or when some of their parameters are unknown. In these cases the validation of  
5 numerical models is a crucial step (Rodríguez-Sánchez et al., 2015). Several are the authors that  
6 have used experimental methodologies to validate the results of their numerical simulations:  
7 either by correcting the reflectivity of the heliostats (Fernández-Reche, 2006), the tracking  
8 errors (Chiesi et al., 2017; Wei et al., 2011) or the canting errors (Sánchez-González et al., 2017).  
9 When validation of numerical models is not possible, it is preferable to use experimental  
10 methodologies. (Röger et al., 2014) classified the limited experimental methodologies in 5  
11 groups, which has been summarized in Table 1:

- 12 i) Indirect methods that use a white diffuse moving bar target placed in front of the  
13 receiver surface and a digital camera that record the flux brightness distribution,  
14 which is calibrated with a radiometer. This measurement principle was used since  
15 the end of the 1970s worldwide in different central receiver projects, e.g., Beam  
16 Characterization System (BCS) of Sandia (Strachan and Houser, 1993), Flux Analysing  
17 System of EIR (Vontobel et al., 1982), heliostat and receiver measurement system  
18 (HERMES I+II, ProHERMES) of the German Aerospace Center (DLR) (Kroger-Vodde  
19 and Hollander, 1999), and CSIRO (Imenes et al., 2006). This method is able to  
20 characterize the flux distribution of all the heliostats aiming the receiver at once.  
21 Being its main issue the degradation of the radiometer painting.
- 22 ii) Direct methods based on the previous procedure that use flux sensors mounting in  
23 the moving bar. MDF method (Ballestrín and Monterreal, 2004) was the most  
24 renowned system of this type, which reported an accuracy of about 6%. However,  
25 it still had problems with the overheating and the degradation of the white  
26 Lambertian surface of the moving bar.
- 27 iii) Indirect methods that utilize a digital camera directly on the receiver surface. In this  
28 case, the intensities reflected by the images at the receiver surface are calibrated to  
29 obtain the incident solar flux on the receiver. The most popular method, named  
30 PHLUX method, was employed by (Ho and Khalsa, 2012). The uncertainties of this  
31 method are significantly, up to 20-40%.
- 32 iv) Indirect methods that use a stationary stripe-shaped target and sweeping the focus  
33 over a fixed target located close to the receiver. The stripe-shaped images, collected  
34 with a digital camera, are then merged to gain a composite flux image. (Pacheco et

al., 1994) applied this method by splitting up the heliostats in groups, instead of moving the whole focus at once. Depending on the accuracy of the heliostat tracking, the number of heliostats involved, the spatial shift and the time gap the uncertainty of the flux density distribution reached was in the range from 3.6% to 9.1%.

v) The last direct methods consist in distribute stationary water cooled flux gauges in the aperture plane or on the receiver surface. The problem of this methodology is the moderate spatial resolution and the short lifetime of the flux gauges on high temperature receiver zones, limited to 6 months.

Table 1 – Summary of the experimental methods to characterize the flux distribution on the receiver surface described in the literature

Method	Acquisition devices	Strength	Weakness	Example
I Indirect	Diffuse moving bar target Digital camera Radiometer	High spatial resolution Short measurement time High reliability	Radiometer and target degradation Mechanical problems of the target	BCS EIR HERMES FATMES OBELIX
II Direct	Diffuse moving bar target Digital camera Gardon flux gauges	Good spatial resolution Low interpolation errors Better precision than method I (~6%)	Overheating Target degradation No applicable in external receivers	MDF
III Indirect	Digital cameras Receiver surface	Simply Cheap	High uncertainties ~20-40% Spectral dependence of the receiver	PHLUX
IV Indirect	Stripe-shaped target close to the receiver Digital camera Flux sensor	No mechanical parts	Time gap between heliostats characterization Accuracy function of the number of heliostats	-
V Direct	Flux gauges Cooling system	No moving parts Low uncertainties	Low spatial resolution High cost Short gauges lifetime (~6 months)	-

The issue is that nowadays, none of these procedures have been introduced in commercial power plants, since they are not fully developed to measure the solar flux distribution intercepted by the huge receiver surface area with an acceptable spatial resolution. Note also that indirect methods need hypothesis to carry out the estimation of the solar flux distributions that can introduce further uncertainties. For example, the Power-On method proposed by (Pacheco, 2002) to calculate the total incident power on the receiver neglects the influence of the power load in the heat losses, while PROHERMES (Kroger-Vodde and Hollander, 1999) and

1 MDF (Ballestrín and Monterreal, 2004) estimates the solar flux distribution on the aperture of  
2 the cavity, assuming that it is equal to the flux distribution on the receiver surface.

3 The main goal of this work is to develop an empirical direct methodology to estimate the  
4 incident radiant power per unit area on a solar absorber. The experimental method proposed,  
5 named “*Superposition method*”, lies in the application of the superposition method on  
6 luminosity images of the reflected beam of the heliostats, using digital image analysis (DIA) and  
7 the measurement of a punctual flux sensor. Although this procedure is well known in numerical  
8 procedures, it has not been applied experimentally.

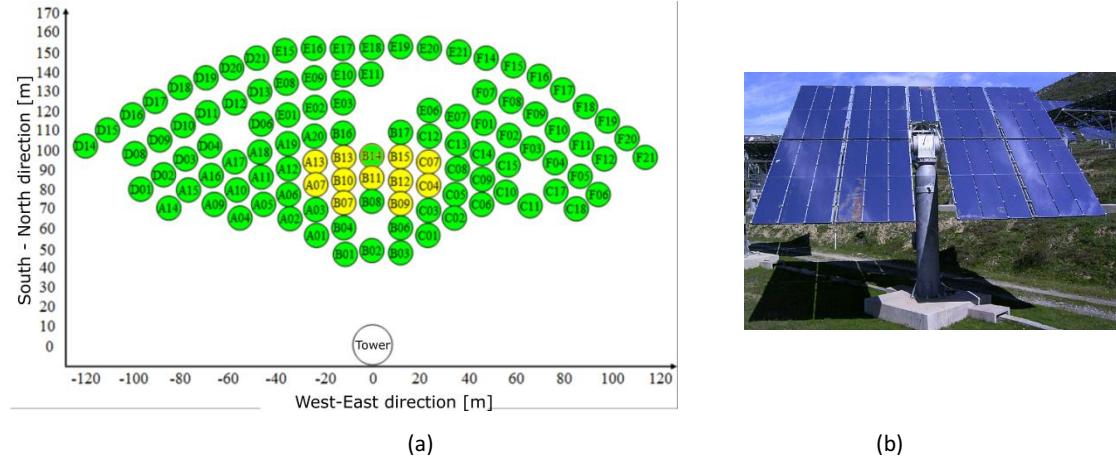
9 The method proposed can be considered a combination of the fourth and second methods  
10 described previously with several updates. The main novelty introduced is that it is a non-real-  
11 time method thanks to the creation of an hourly library of the different heliostats. Which is  
12 independent of the DNI and the day, using as storage variables the solar time and the  
13 concentration ratio. With this library, any combination of the available images can be used to  
14 reproduce a solar flux distribution on the receiver at present and past time.

15 This method could be applied when the numerical simulations are not able to accurately predict  
16 the incident radiant power due to the heliostat detriment. This study starts with a description  
17 of the plant and the receiver prototype in which it is applied. Secondly, the methodology  
18 developed for the estimation of the radiant power on the receiver has been explained. Finally,  
19 this new methodology has been verified and validated with several experiments carried out in  
20 Themis solar power tower.

21 **2. Themis power plant**

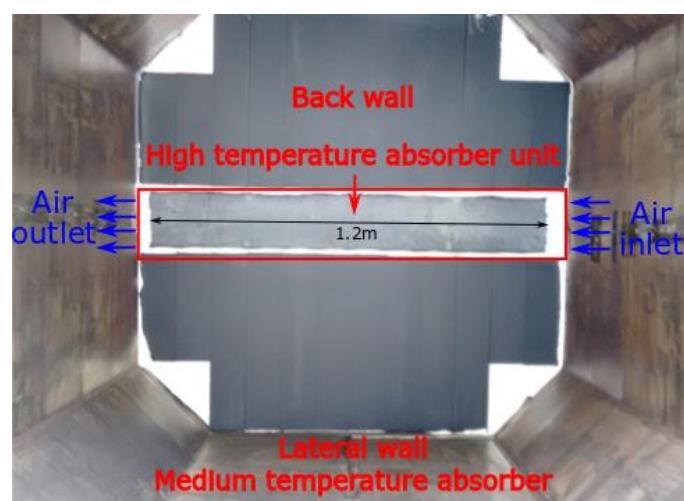
22 To carry out this study a prototype solar absorber assembled in Themis solar power tower has  
23 been characterized. Themis solar plant consists of a northern solar field layout compound of 107  
24 heliostats, see Figure 1.a. Each heliostat has an effective surface of 53.70 m<sup>2</sup> composed of 9  
25 spherical mirror elements installed onto a parabolic supporting structure: eight main modules  
26 of 3.62 m x 1.794 m and one central module of 2.46 m x 0.828 m, see Figure 1.b. Each module is  
27 individually oriented such as its axis matches the normal to the parabola. In practice, all the  
28 modules of each heliostat possess the same focal length, which is close to the distance to the  
29 receiver aperture. The size, the curvature, the position and the orientation of these facets and  
30 the focal length of the supporting structure are known from the design specifications of each  
31 individual heliostat, whose initial error ranging was comprised between 0.5 and 2 mrad (Salomé  
32 et al., 2013). Then, the control of the heliostat field should provide the desired intensity and

1 solar flux distribution at the focal volume. However, over the years the heliostats have been  
 2 deteriorated and some of their facets are missed or broken, therefore nowadays they do not  
 3 fulfil their initial specifications.



4  
 5 Figure 1–(a) Representation of the heliostat field layout of Themis. (b) Frontal part of a Themis heliostat (Salomé et  
 6 al., 2012).  
 7

8 Themis tower is 100 m height and it is equipped with several experimental areas (CNRS-  
 9 PROMES, 2013). The receiver prototype consists of a silicon carbide high temperature absorber  
 10 plate of 1200 mm length, 167 mm width and 28 mm of total thickness (Capeillère et al., 2014).  
 11 The plate is located at the back wall of a parallelepiped cavity inclined 35.9° with respect to the  
 12 vertical axis. The cavity has a square aperture area of 1.2 m length and its depth is 1 m. The four  
 13 lateral walls work as medium temperature absorbers, which preheats the pressurized air that  
 14 feeds the receiver. The air enters in the high temperature absorber by the right side and exits  
 15 by the left (see Figure 2.a). As the high temperature absorber is small, to avoid overheating only  
 16 11 of the 107 heliostats in the field have been used, they have been highlighted in yellow in  
 17 Figure 1.a.  
 18



19 Figure 2–Overview of a ceramic cavity receiver prototype developed by PROMES laboratory installed in Themis.

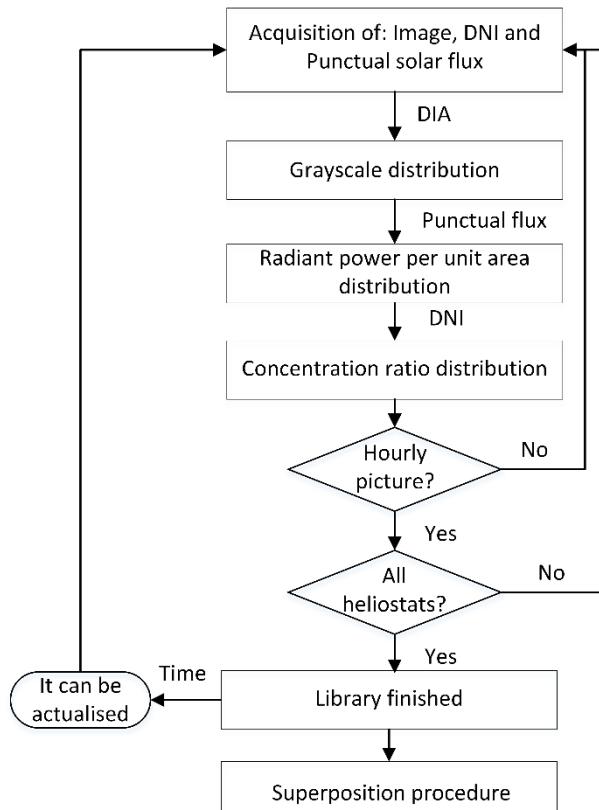
1     **3. Superposition method**

2     Experimentations on the prototype receiver were carried out at Themis from April 2015 to May  
3     2016. In those experiments different operational conditions were tested. A mass flowmeter and  
4     several thermocouples allowed to calculate the heat power absorbed by the heat transfer fluid.  
5     The estimated incident flux on the receiver, by means of a modified HFCAL simulation (Capeillère  
6     et al., 2014), resulted to be so high, giving a derisory thermal efficiency of the receiver that did  
7     not agree with the numerical study. Therefore, a new methodology to estimate the incident  
8     radianc power per unit area is required.

9     A new experimental methodology named “Superposition method” has been developed to  
10    determine the incident solar flux on the receiver surface for any hour, day and aiming strategy.  
11    The methodology proposed consists in two main phases. In the first phase, images of the  
12    reflected beam of each individual heliostat have been taken and processed to obtain the  
13    concentration ratio distribution of each heliostat on the receiver surface. In this first phase, a  
14    library of images and concentration ratio distributions of the different heliostats have been  
15    created. In the second phase the procedure to superpose the concentration ratio distributions  
16    of different heliostats have been explained. This procedure allows to reproduce the incident  
17    radianc power per unit area on the receiver surface for any hour, day and aiming strategy.

18       **3.1. Image processing**

19    Figure 3 shows the schematic of the process described in the following subsections.



1

2

Figure 3– Schematic of the image processing

3       **3.1.1. Image acquisition**

4     This first phase consists on the characterization of the reflected beam of each heliostat. To do  
 5     that, a passive screen of 1.4 m length and 1 m height is used. It is located 2.5 m under the cavity  
 6     and with the same inclination angle. This screen is a solar flux qualification system coated with  
 7     a white Lambertian paint. The homogeneity of its surface make it ideal to characterize the  
 8     luminosity of the reflected beam of the heliostats. However, this screen is not refrigerated and  
 9     only one heliostat can be focused on it at once.

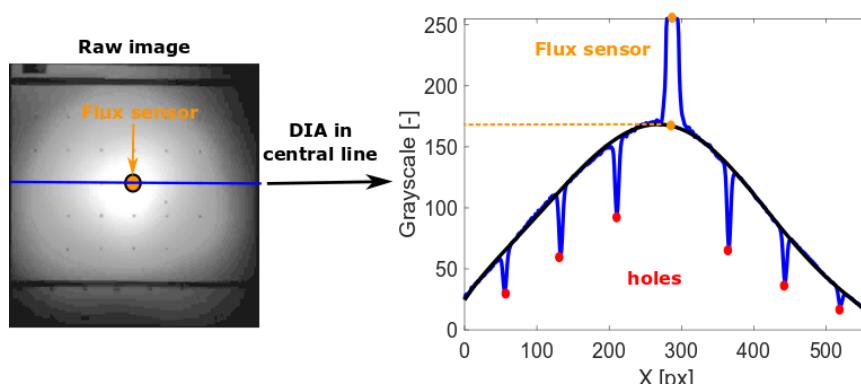
10    On the ground, in the middle of the solar field, a high resolution CCD camera with adapted filters  
 11    takes pictures of the beam which is reflected onto the passive screen. The camera is a Theta  
 12    system SIS1-s28, with a resolution of 2.597 mm per pixel. Besides, the passive target was  
 13    equipped in its central position with a Vatell flux sensor type TG9000-25, that allows to measure  
 14    punctual solar flux intensities. The sensitive sensor consists in a disk of 4.76 mm diameter,  
 15    equipped of a sapphire window that ensures a pure radiative measurement eliminating  
 16    convection effects with an accuracy of  $\pm 3\%$ . Theoretically, this central point of the screen should  
 17    correspond to the peak flux of the heliostat beam. The data acquired by the flux sensor is read  
 18    at the same instant of time in which the picture is taken and the direct normal irradiation (DNI)

1 is acquired. To collect the meteorological data a meteorological station placed at the roof of  
2 Themis tower is employed. The station is equipped with a pyrheliometer that measures the DNI  
3 every passing minute with a precision of  $\pm 1 \text{ W/m}^2$ .

4           **3.1.2. Digital Image Analysis (DIA)**

5 The raw images taken by the CCD camera are treated with a DIA using the free software  
6 “*ImageJ*”. This process allows to obtain the luminosity of the reflected beam of the images. For  
7 each picture two different surfaces are selected to characterize the average luminosity in the  
8 horizontal axis. The raw image of Figures 4 and 5 represents the reflected beam of heliostat B10  
9 the 30/03/2016 at 11:22h (civil time).

10 Firstly, the luminosity has been characterized in the central line of the target (blue solid line in  
11 raw image of Figure 4), which crosses the flux sensor. The luminosity is obtained in grayscale  
12 level; whose range goes from 0 to 255. Analysing this central line and not only the central point  
13 where the flux sensor is located is mandatory, since the sensor has different reflectivity than the  
14 passive screen and then a peak appears in the luminosity signal (yellow point). It is important to  
15 note also that there are other atypical values (red points) due to the perforations that the  
16 passive screen has every 20 cm, as can be seen in the raw image. These defects in the luminosity  
17 have been solved with the average between the closest points (black solid line in Figure 4). Once  
18 the signal has been treated, it is possible to link the flux measurement with a greyscale value  
19 (yellow dashed line in Figure 4).

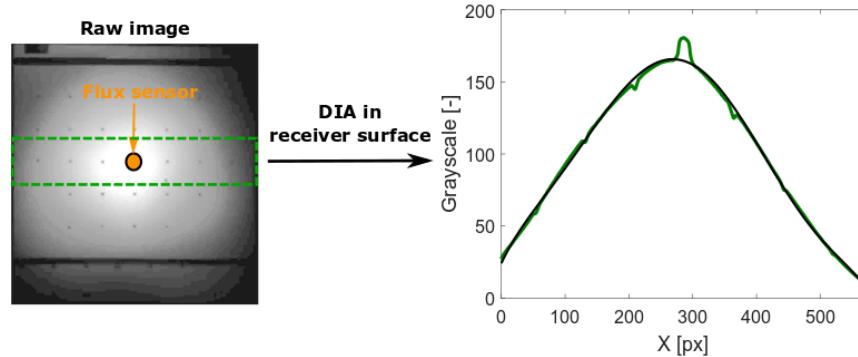


20

21 Figure 4 –Raw image of the reflected beam of heliostat B10 the 30/03/2016 at 11:22 h. Post-processed information:  
22 luminosity in the central line of the target.

23 Secondly, the luminosity has been characterized in a rectangular section of the target (green  
24 dashed line in raw image of Figure 5). This section corresponds to the equivalent area of the high  
25 temperature absorber. The average luminosity of that section has been converted to the  
26 grayscale level. In this case, the anomalous points still appear, but they are much lower as it

1 corresponds to a lower area in the region scrutinized. Nevertheless, they have been corrected  
 2 (black solid line) as in Figure 4. Then, it is possible to use the prior relationship between the  
 3 grayscale and the flux intensity.



4  
 5 Figure 5 –Raw image of the reflected beam of heliostat B10 the 30/03/2016 at 11:22 h. Post-processed information:  
 6 average luminosity in an area equivalent to the one of the high temperature absorber.

### 7 3.1.3. Data conversion

8 In this step it is required to convert the pixels to meters and the grayscale level to flux intensity.  
 9 For the first transformation, the resolution of the camera has been used. Besides, the position  
 10 of the flux sensor (maximum peak) has been selected as the origin of coordinates. For the second  
 11 transformation, a lineal relationship has been assumed between the grayscale level and the flux  
 12 intensity. The relationship, seen in Figure 4, has been used to transform the grayscale signal of  
 13 Figure 5 to flux intensity, as is plotted in Figure 6.

14 The flux intensity depends on the DNI, thus it is preferable to work with concentration ratio,  
 15 which is defined as the instantaneous flux intensity over the corresponding DNI. Solid green line  
 16 of Figure 6 illustrates the concentration ratio distribution on the central area of the target for  
 17 heliostat B10 at the same day an hour than Figures 4 and 5. In those figures it can be observed  
 18 that the grayscale level does not reach the 0 value. The reflected beam spot is larger than the  
 19 target size, thus heliostat B10 has spillage losses and the concentration distribution obtained  
 20 from the image is incomplete. An extrapolation at the beginning and end of the signal has been  
 21 applied to reach the null concentration ratio (solid black line in Figure 6).

22 It must be highlighted that the reflected beam is not a perfect ellipse, which reveals some  
 23 canting and alignment errors of this heliostat. Moreover, the maximum value is slightly displaced  
 24 to the left with respect to the flux sensor position ( $x = 0\text{m}$ ), which reflects also a tracking defect  
 25 of heliostat B10.

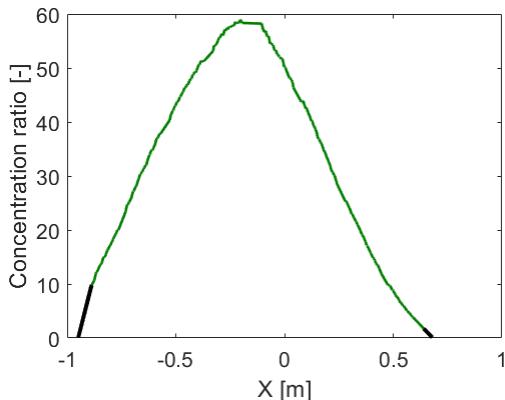


Figure 6 – Concentration ratio distribution of the heliostat B10 in the central section of the passive screen the  
30/03/2016 at 11:22 h.

### 3.1.4. Library creation

5 The concentration ratio distribution of each heliostat varies along the year, thus only one picture  
6 of each heliostat is not enough to characterize its behaviour. This variation is more pronounced  
7 in non-aligned heliostats than in heliostats at perfect conditions. Figure 7 portrays an example  
8 of this variation. It shows several isoflux images, obtained from the raw images (Salomé et al.,  
9 2013), of the reflected beam of heliostat B10 along a sunny day. It can be observed that at 10 h  
10 the heliostat seems to be on perfect conditions, however at first hours in the morning its shape  
11 is irregular and in the afternoon there are two focus points (maximums) instead of one.

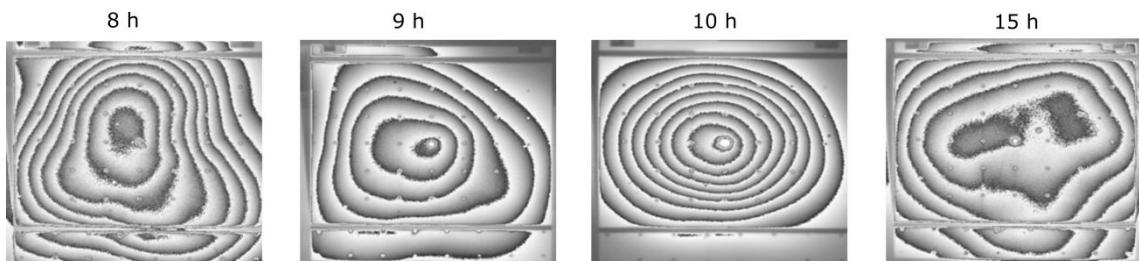


Figure 7 – Isoflux images of the reflected beam of heliostat B10 at different hours of a sunny day.

To solve this problem a library of images of each heliostat has to be created. Figure 8.a represents the concentration ratio distribution of heliostat B10 for two different days at the same solar hour, while Figure 8.b depicts the concentration ratio distribution of the same heliostat at different hours of a sunny day. In Figure 8 it can be seen that the annual concentration ratio distribution remains almost constant when the solar hour is fixed, however it varies considerably with the time variation. Therefore, it can be assumed that the library is independent on the day but not on the solar hour.

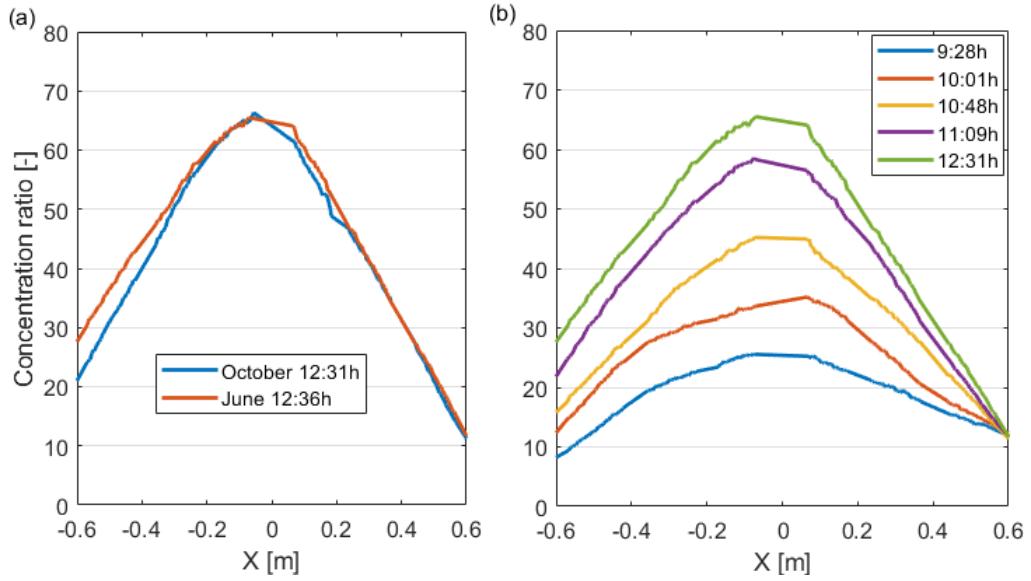


Figure 8 – Distribution of the average concentration ratio for heliostat B10 at (a) two different days at the same hour, and at (b) the same day at different hours.

To complete the library is recommendable to have more than one image per hour of each heliostat. It permits to do reliable weighted averages between several concentration ratio distributions of a heliostat to obtain its approximate behaviour at any time. Besides, it is recommendable to take these photos at different days along the year to reduce the errors in the characterization of the heliostat, as it minimises the effect of the reflectivity variation caused by the weather conditions or the cleaning of the heliostat.

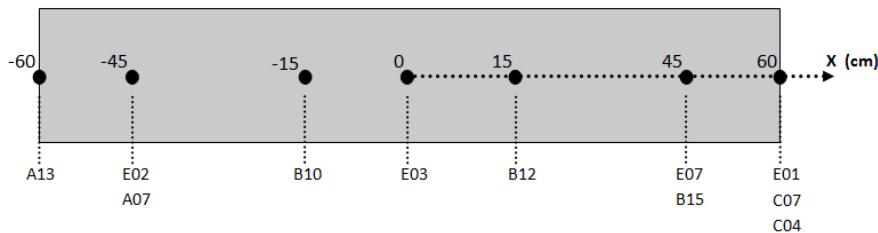
### 3.2. Superposition procedure

In the second phase the average concentration ratio distribution of the individual heliostats has to be gathered in order to obtain the incident thermal power on the receiver.

Firstly, the solar hour of the analysis has to be fixed, since it is required to obtain the most adequate concentration ratio distributions from the library. For each heliostat a weighted average between concentration ratio distributions closer in time has to be done, the resultant of this operation is used in the next steps. Based on the amount of data available three images, for each heliostat, were chosen enough to minimise the uncertainties due to time gap, atmospheric conditions and season (day of the year) with a reasonable increment of the computational cost. However, the number of averaged images could be reduced if not enough data are available or increased if there are too many available pictures close to the hour of study.

Secondly, the aiming strategy has to be selected. In the prototype receiver, 11 heliostats aimed to 7 different points in the same horizontal line, as shown in Figure 9. The origin of coordinates corresponds to the central position of the high temperature absorber. Therefore, the resultant

concentration ratio of each heliostat has to be displaced in the horizontal position the corresponding distance given by Figure 9. As the passive screen and the high temperature absorber are relatively close, the variations on the reflected beam when the heliostats aim to the target or to the high temperature absorber can be neglected. (J.E. Pacheco et al., 1994) examined the effect of focus variation due to spatial shift and time gap during experiments carried out in an external receiver. They determined that this error is greater for heliostats in the rows closer to the tower and lower for the heliostats at the edges. This error increases with the separation between the receiver and the target and the modification of the interception plane. However, they pointed that this error is relatively small (around 2%) compared to other errors as: variation of the atmospheric conditions, camera linearity and variations in the white target properties.



12

13

Figure 9 – Aiming strategy used on the solar receiver prototype

Figure 10 (bottom) represents the resultant concentration ratio of each individual heliostat once the aiming strategy has been applied. The horizontal axis represents the length of the high temperature absorber (1.2 m). It can be observed that the selected aiming strategy has important spillage losses, especially in the inlet of the absorber (right side). Figure 10 (top) portrays the sum of the individual concentration ratio presented in Figure 10 (bottom). The incident solar flux on the high temperature absorber is calculated multiplying the total concentration ratio by the instantaneous DNI at the desired moment.

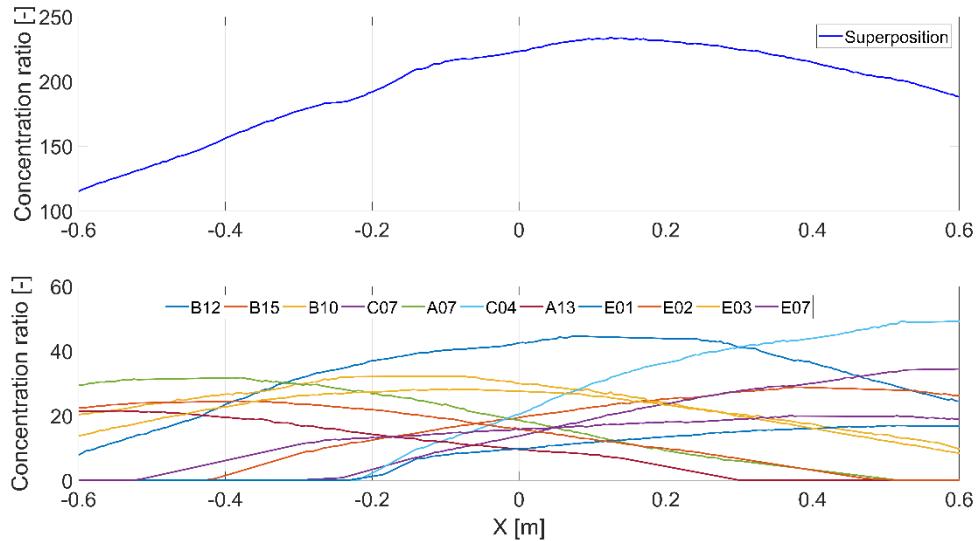


Figure 10 – Resultant concentration ratio of the 11 heliostats focused to different horizontal positions (see Figure 9).  
Bottom: Individual concentration ratio distributions. Top: Superposed concentration ratio distribution.

#### 4. Verification of the method

To verify the main assumptions made in Superposition method a set of experiments were carried out after dismantling the high temperature absorber. A rigid insulation panel of compacted  $\text{Al}_2\text{O}_3$  fibbers  $1 \text{ m} \times 0.2 \text{ m} \times 0.05 \text{ m}$  has been assembled in the absorber position. As it has a homogeneous colour, it can be used as a passive target in the back of the cavity. A Vatell flux sensor was installed in the centre of the insulation panel to measure the punctual incident flux, see Figure 11.



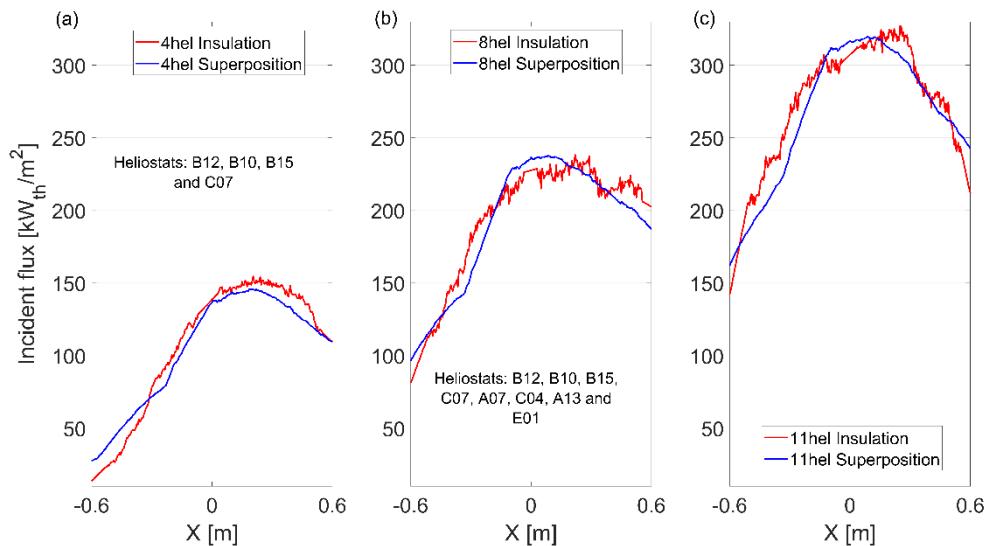
Figure 11 – Assemble of the rigid insulation panel with the flux sensor in the middle.

Images of the back of the cavity were taken with the CCD camera when different number of heliostats were focused on the insulation panel. Independently on the number of heliostats used, each working heliostat focus to its respective point indicated in Figure 9. To the raw images of the reflected beams on the insulation panel the same DIA than in the passive screen images

1 has been applied. In this case, the grayscale level takes into account the effect (shadows) of the  
2 cavity lateral walls.

3 In Figure 12 the incident flux distributions obtained in the insulation panel, when 4, 8 and 11  
4 heliostats were focused to the back of the cavity, have been compared with the results of the  
5 Superposition method at the same hour. It is observed that with the three aiming strategies the  
6 solar flux distribution obtained in the insulation panel agrees well with the method proposed.  
7 The radiant power per unit area is slightly underestimated with the Superposition method  
8 (about 2.5%) and the differences are constant with the number of heliostats focused. These  
9 small differences can be attributed to: the effect of the lateral walls of the cavity, which is only  
10 considered in the insulation panel; the variation of the aiming position (passive screen or back  
11 of the cavity), and a possible wrong estimation of the averaged reflected beam of the individual  
12 heliostats due to the lack of information on the library at certain hours.

13 Due to the technical difficulty of the plant operation further verifications were not possible. With  
14 the available data it can be pointed that, despite the approximations made, Superposition  
15 method is able to obtain a good approximation of the solar flux distribution and intensity that  
16 falls upon the high temperature absorber. Moreover, it has been tested that Superposition  
17 method can be adapted easily to different aiming strategies and hours since the heliostats have  
18 been individually characterized.



20 Figure 12 – Comparison between the solar flux distribution on the insulation panel and the calculated by  
21 Superposition on the central section of the high temperature absorber for the day 19/07/2016, using (a) 4 heliostats  
22 at 14:59 h (b) 8 heliostats at 15:19 h (b) 11 heliostats at 15:44 h.

23 **4.1. Uncertainty considerations**

1 The uncertainty of the proposed Superposition method depends on:

2 - The accuracy of heliostat tracking: which treats to be corrected using the white target  
3 before focusing the heliostats to the receiver.

4 - The number of heliostats involved in the test: although in previous subsection it has  
5 seen that the accuracy is independent of the heliostat number.

6 - The time gap between the heliostat characterization and the tests on the receiver: this  
7 effect has been corrected with the library creation and the solar flux distribution  
8 average.

9 - Variation of the atmospheric conditions and mirrors cleanliness: this effect is also  
10 minimised averaging solar flux distributions of each heliostat.

11 - The spatial shift between the white screen and the receiver and effect of the lateral  
12 walls of the cavity: comparing two consecutive images (time gap lower than a minute)  
13 of the reflected beam of heliostat B12 on the white screen and on the insulation panel,  
14 the differences find between both flux distributions is 2.7%.

15 - Uncertainties of CCD camera and the flux sensor that can be assumed around 3%,  
16 - Painting deterioration of the target an insulation panel: The target is frequently cleaned  
17 and the insulation panel was used during a few number of experiments to avoid that  
18 problems.

19 Therefore, the error of the proposed method is similar to the one obtained by (J.E. Pacheco et  
20 al., 1994) being lower than 10%, which is acceptable for experimental results.

## 21 **5. Validation**

22 In this section the Superposition method has been validated using flux measurements carried  
23 out in the back of the cavity before installing the receiver prototype. A metallic cooled panel was  
24 assembled in the back wall of the cavity (Figure 13.a); it possesses 32 holes distributed by its  
25 entire surface, but only 12 of which are sited on the high temperature absorber location. In these  
26 12 holes, different Vatell cooled flux sensors were installed.

27 Figure 13.b schematizes the cooled panel and portrays the aiming strategy described in Figure  
28 9. Besides, the intensity of the solar flux measured in each of the 12 holes for the 7<sup>th</sup> of January  
29 of 2015 at 16:11 h (civil time) have been shown in the red rectangles. These 12 measures give  
30 the distribution of incident radiant power per unit area on the high temperature absorber  
31 surface (red circles in Figure 14).

32

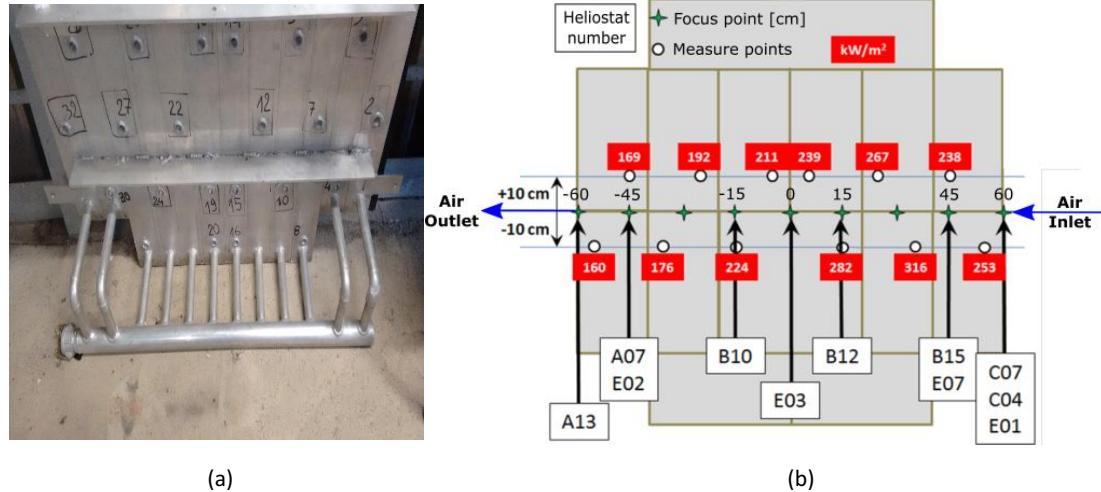


Figure 13–(a) Image of the dismantled cooled panel (b) Schematic of the cooled panel including the focus point of the 11 heliostats (white rectangles and green crosses) and the intensity of each of the 12 solar flux (red rectangles and white points) for the 07/01/2015 at 16:11 h (civil time).

Figure 14 displays the solar flux distribution and intensity on the high temperature absorber position, during the 7<sup>th</sup> of January of 2015 at 14:19 h solar time (16:11 h civil time) measured in the cooled panel and calculated using Superposition method. The distribution of radiant power per unit area is similar in both cases. Therefore, the assumption of proportionality between the grayscale level and the flux intensity is correct.

Integrating both signals it is obtained a total solar flux on the equivalent receiver surface of 253 kW<sub>th</sub>/m<sup>2</sup> for the measurement in the cooled panel and 276.27 kW<sub>th</sub>/m<sup>2</sup> for the Superposition method, which represents a variation of 8.4%. This variation is slightly higher than the obtained in the uncertainty analysis, due to none location of the 12 measurement points are located in the middle height of the receiver, where the flux is expected to be the highest, and thus the cooled panel underestimates the incident flux intensity on the receiver. At the inlet and exit of the high temperature absorber the differences between both signals increase. The flux measured on the cooled panel presents slope variations close to the edges due to the radiative heat exchange with the lateral walls of the cavity; effect that is not considered in the Superposition method. Overall it can be concluded that the Superposition method constitutes a good approximation for the flux density calculation.

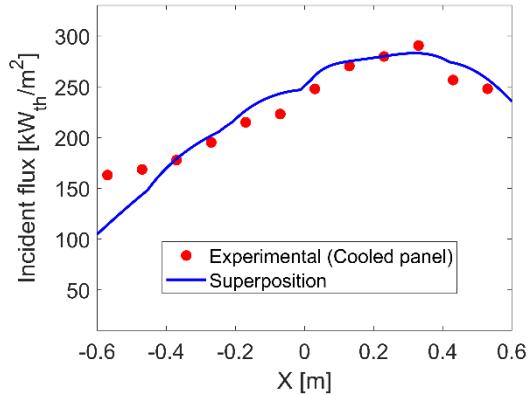


Figure 14 – Comparison between the incident solar flux measured in the cooled panel and the calculated by the Superposition method the 07/01/2015 at 16:11 h.

## 6. Conclusions

In this study, a new empirical direct methodology named “*Superposition method*” has been developed to determine the distribution and intensity of the solar flux that falls upon a central receiver surface. The methodology is especially useful when the heliostats are deteriorated and the numerical simulations are not able to predict the incident solar flux. This methodology has been verified and validated on a high temperature absorber installed in the back of a cavity on Themis solar power tower, whose heliostats are far from the nominal conditions.

“*Superposition method*” characterizes separately each heliostat to gather the individual flux distributions using digital image analysis. The method requires creating an hourly library to characterize each heliostat. Once the library is well defined it is a non-real-time method that allows to predict the solar flux distribution and intensity on the high temperature absorber at any moment with minimum grade of error. Characterizing the heliostats individually permits to test different aiming strategies without excessive effort. Besides, to minimising the error the authors encourage to extend the library always that it was possible, to adapt it to the new conditions of the heliostats.

The strength of the proposed experimental methodology compared to others of the literature is the time independence that allows to estimate solar flux distributions without carrying out extra measurements, the good spatial resolution and the low cost. However, the main issue related to Superposition methodology is the time cost of creating the proposed library for large solar fields. As the heliostats are characterized individually, the heliostats could be defocused of the receiver during operation without perturbing the solar plant operation, being the available time the only problem of the proposed methodology for its implantation in commercial power

1 plants. Nonetheless, it is useful in demonstration solar power towers as Themis or to  
2 characterize those heliostats, inside large solar fields, that may present calibration or  
3 geometrical problems.

4 Moreover, the creation of the library can be a good starting point to develop further strategies  
5 to control problematic heliostats and to introduce the heliostat deterioration parameters in  
6 numerical models.

## 7 **Acknowledgments**

8 The authors acknowledge the financial support of the research programme of the University  
9 Carlos III de Madrid, which made this study possible through a mobility grant of the first author.  
10 Moreover, the research work leading to this article received funding from the European Union  
11 Seventh Framework Program (FP7/2014-2018) under grant agreement n°. 609837 (Scientific and  
12 Technological Alliance for Guaranteeing the European Excellence in Concentrating Solar Thermal  
13 Energy, STAGE-STE). This work was also supported by the Spanish government under the project  
14 ENE2015-69486-R (MINECO/FEDER, UE).

## 15 **References**

- 16 Ballestrín, J., Monterreal, R., 2004. Hybrid heat flux measurement system for solar central  
17 receiver evaluation. *Energy* 29, 915–924. [https://doi.org/10.1016/S0360-5442\(03\)00196-8](https://doi.org/10.1016/S0360-5442(03)00196-8)
- 19 Belhomme, B., Pitz-Paal, R., Schwarzbözl, P., Ulmer, S., 2009. A New Fast Ray Tracing Tool for  
20 High-Precision Simulation of Heliostat Fields. *J. Sol. Energy Eng.* 131, 31002.  
21 <https://doi.org/10.1115/1.3139139>
- 22 Blanco, M.J., Amieva, J.M., Mancilla, A., 2005. THE TONATIUH SOFTWARE DEVELOPMENT  
23 PROJECT: AN OPEN SOURCE APPROACH TO THE SIMULATION OF SOLAR CONCENTRATING  
24 SYSTEMS, in: ASME International Mechanical Engineering Congress and Exposition.  
25 Orlando, Florida, USA, pp. 1–8.
- 26 Capeillère, J., Toutant, a., Olalde, G., Boubault, a., 2014. Thermomechanical behavior of a  
27 plate ceramic solar receiver irradiated by concentrated sunlight. *Sol. Energy* 110, 174–  
28 187. <https://doi.org/10.1016/j.solener.2014.08.039>
- 29 Chiesi, M., Scarselli, E.F., Guerrieri, R., 2017. Run-time detection and correction of heliostat  
30 tracking errors. *Renew. Energy* 105, 702–711.  
31 <https://doi.org/10.1016/J.RENENE.2016.12.093>
- 32 CNRS-PROMES, 2013. PROMES facilities: Themis [WWW Document]. URL  
33 <http://www.promes.cnrs.fr/index.php?page=themis> (accessed 2.25.18).
- 34 Collado, F.J., 2010. One-point fitting of the flux density produced by a heliostat. *Sol. Energy* 84,  
35 673–684. <https://doi.org/10.1016/j.solener.2010.01.019>

- 1 Collado, F.J., Guallar, J., 2012. Campo: Generation of regular heliostat fields. *Renew. Energy* 46,  
2 49–59. <https://doi.org/10.1016/j.renene.2012.03.011>
- 3 Cruz, N.C., Redondo, J.L., Berenguel, M., Álvarez, J.D., Becerra-Teron, A., Ortigosa, P.M., 2017.  
4 High performance computing for the heliostat field layout evaluation. *J. Supercomput.*  
5 73, 259–276. <https://doi.org/10.1007/s11227-016-1698-7>
- 6 Cruz, N.C., Redondo, J.L., Berenguel, M., Álvarez, J.D., Ortigosa, P.M., 2017. Review of software  
7 for optical analyzing and optimizing heliostat fields. *Renew. Sustain. Energy Rev.* 72,  
8 1001–1018. <https://doi.org/10.1016/J.RSER.2017.01.032>
- 9 European energy research alliance, 2014. STAGE-STE project [WWW Document].  
10 <http://www.stage-ste.eu/>. URL <http://www.stage-ste.eu/> (accessed 4.4.16).
- 11 Fernández-Reche, J., 2006. Reflectance measurement in solar tower heliostats fields. *Sol.*  
12 *Energy* 80, 779–786. <https://doi.org/10.1016/J.SOLENER.2005.06.006>
- 13 Garcia, P., Ferriere, A., Bezian, J.-J., 2008. Codes for solar flux calculation dedicated to central  
14 receiver system applications: A comparative review. *Sol. Energy* 82, 189–197.  
15 <https://doi.org/10.1016/j.solener.2007.08.004>
- 16 Ho, C.K., Khalsa, S.S., 2012. A Photographic Flux Mapping Method for Concentrating Solar  
17 Collectors and Receivers. *J. Sol. Energy Eng.* 134, 41004.  
18 <https://doi.org/10.1115/1.4006892>
- 19 Imenes, A., Hinkley, J., Benito, R., Bolling, R., Schramek, P., Ulmer, S., 2006. Ray tracing and flux  
20 mapping as a design and research tool at the national solar energy centre, in: ANZSES  
21 Conference. Canberra, pp. S06-81.
- 22 Kistler, B.L., 1986. A User's Manual for DELSOL3: A Computer Code for Calculating the Optical  
23 Performance and Optimal System Design for Solar Thermal Central Receiver Plants.  
24 Albuquerque.
- 25 Kroger-Vodde, a., Hollander, a., 1999. CCD flux measurement system PROHERMES. *J. Phys. IV*  
26 Fr. 9, 649–654.
- 27 Leary, P.L., Hankins, J.D., 1979. User's guide for MIRVAL: a computer code for comparing  
28 designs of heliostat-receiver optics for central receiver solar power plants.
- 29 Pacheco, J.E., 2002. Final Test and Evaluation Results from the Solar Two Project. Albuquerque,  
30 SAND2002-0120.
- 31 Pacheco, J.E., Houser, R.M., Neumann, A., 1994. Concepts to measure flux and temperature for  
32 external central receivers.pdf, in: Joint Solar Engineering Conference. pp. 595–603.
- 33 Piroozmand, P., Boroushaki, M., 2016. A computational method for optimal design of the  
34 multi-tower heliostat field considering heliostats interactions. *Energy* 106, 240–252.  
35 <https://doi.org/10.1016/J.ENERGY.2016.03.049>
- 36 Roccia, J.P., Piaud, B., Coustet, C., Caliot, C., Guillot, E., Flamant, G., Delatorre, J., 2012.  
37 SOLFAST, a ray-tracing monte-carlo software for solar concentrating facilities. *J. Phys.*  
38 Conf. Ser. 369. <https://doi.org/10.1088/1742-6596/369/1/012029>
- 39 Rodríguez-Sánchez, M.R., Sánchez-González, A., Santana, D., 2015. Revised receiver efficiency  
40 of molten-salt power towers. *Renew. Sustain. Energy Rev.* 52, 1331–1339.

- 1           <https://doi.org/10.1016/j.rser.2015.08.004>
- 2       Röger, M., Herrmann, P., Ulmer, S., Ebert, M., Prahl, C., Göhring, F., 2014. Techniques to  
3       Measure Solar Flux Density Distribution on Large-Scale Receivers. *J. Sol. Energy Eng.* 136,  
4       31013. <https://doi.org/10.1115/1.4027261>
- 5       Salomé, A., Chhel, F., Flamant, G., Ferrière, A., Thiery, F., 2013. Control of the flux distribution  
6       on a solar tower receiver using an optimized aiming point strategy: Application to THEMIS  
7       solar tower. *Sol. Energy* 94, 352–366. <https://doi.org/10.1016/j.solener.2013.02.025>
- 8       Salomé, A., Flamant, G., Ferrière, A., Thiery, F., 2012. Optimized Aim Point Strategy for Central  
9       Receiver : Application To Themis. *SolarPACES*.
- 10      Sánchez-González, A., Caliot, C., Ferrière, A., Santana, D., 2017. Determination of heliostat  
11      canting errors via deterministic optimization. *Sol. Energy* 150, 136–146.  
12      <https://doi.org/10.1016/j.solener.2017.04.039>
- 13      Sánchez-González, A., Santana, D., 2015. Solar flux distribution on central receivers: a  
14      projection method from analytic function. *Renew. Energy* 74, 576–587.
- 15      Schwarzbözl, P., Pitz-Paal, R., Schmitz, M., 2009. Visual HFLCAL - A Software Tool for Layout  
16      and Optimisation of Heliostat Fields, in: *SolarPACES*. SolarPACES, Berlin, Germany.
- 17      Strachan, J., Houser, R., 1993. Testing and evaluation of large-area heliostats for solar thermal  
18      applications, Solar Thermal Test Department, Sandia National Laboratories. Albuquerque,  
19      SAND92-1381.
- 20      Vontobel, G., Schelders, C., Real, M., 1982. Concentrated solar-flux measurements at the IEA-  
21      SSPS solar-central-receiver power plant, Tabernas - Almeria (Spain). Wuerenlingen  
22      (Switzerland).
- 23      Wei, X., Lu, Z., Yu, W., Zhang, H., Wang, Z., 2011. Tracking and ray tracing equations for the  
24      target-aligned heliostat for solar tower power plants. *Renew. Energy* 36, 2687–2693.  
25      <https://doi.org/10.1016/j.renene.2011.02.022>
- 26      Wendelin, T., 2003. SolTRACE: A New Optical Modeling Tool for Concentrating Solar Optics.  
27      *Sol. Energy* 253–260. <https://doi.org/10.1115/ISEC2003-44090>
- 28