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Experimental analysis of an attenuation method for Hydrodynamic Ram effects

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Abstract

The hydrodynamic ram (HRAM) phenomenon occurs when an object with a high-kinetic energy impacts against a fluid-filled structure, which could induce important damages. An attenuation technique would be of great interest for structures which could be subjected to impact. In this work, honeycomb panels are used to fill the entire space inside the structure in such a way that they are able to alleviate the loading onto it. Experimental tests were carried out varying aluminium honeycomb cells orientation, to determine the configuration that mitigates more efficiently the effects of HRAM comparing the results with a non-protected structure. The experimental tests were analysed using a high speed video camera, strain gauges, residual displacement of the structure walls and the deformation of the honeycomb panels. It is shown that for all the configurations, the honeycomb is able to reduce the plastic deformation of the structure. The honeycomb allows to reduce the cavity expansion in the fluid, which is the most dangerous phenomenon in the studied cases. The best configuration is able to diminish up to a 54% the residual expanded volume in the structure walls, and hence considerably

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attenuating the HRAM effect on the structure.

Keywords: Hydrodynamic Ram, Attenuation method, Fluid-structure interaction, Fluid-filled tank, High Velocity Impact, Experimental test

1. Introduction

The Hydrodynamic Ram (HRAM) phenomenon occurs when an object with high kinetic energy penetrates a fluid-filled container. The object, while traveling through the fluid, transfers part of its energy to it, and consequently to the surrounding structure. Hence the walls of a fluid-filled structure, subjected to an impact load, have to withstand higher energy levels than the same structure without fluid. Therefore it is important to take into account the presence of fluid inside a structure because it is the responsible for increasing the risk of a catastrophic failure [1]. Thus, the HRAM phenomenon is considered one of the most important factors in aircraft vulnerability [2, 3]. Fuel tanks can be impacted by different kind of fragments and in different situations. Different impactors such as hail [6, 7], bird [8] or tyre fragments [9] could impact fuel tanks with enough kinetic energy to generate the HRAM phenomenon causing a catastrophic failure, as happened in the accident of the Concorde [10]. Also, the accidental explosion of an engine can generate a number of fragments that impact at high velocity against the wing fuel tanks [5] producing the HRAM effects as happened in Qantas A-380 accident [4]. The commercial aircraft industry is greatly concerned about this type of Uncontained Engine Rotor Failure (UERF) events. But the HRAM phenomenon is not an unique issue in the aerospace industry, also it is important and should be taken into account in the industrial sector, where a structure containing fluid (vessel, tanker truck, etc.) can be hit at high velocity [11, 12, 13]. This case can

22 be particularly dangerous if the fluid inside the container is a hazardous material.

23

24 The first researches concerning the HRAM were carried out by military agen-
25 cies in the 70s. It's not until the 90's when academic institutions had studied this
26 phenomenon, applied to commercial aircraft. The HRAM has been analysed ex-
27 perimentally [1, 14, 15], numerically [16, 17, 18, 19] and with analytical models
28 [20]. An extensive review regarding the studies performed can be found in the
29 experimental and numerical works of D. Varas et al. [1, 16]. Additionally to these
30 works, the authors of the present research have published several articles concern-
31 ing the study of this phenomenon in metallic and composite tubes filled with water
32 [17, 21, 22, 23].

33

34 Previous studies have shown that the HRAM phenomenon consists of four
35 main stages: shock, drag, cavity and exit [1, 16, 15, 17]. Each stage contributes to
36 the structural damage through a different mechanism and to a different extent. In
37 addition, depending on the particular circumstances (dimensions of the structure,
38 material and kinetic energy of the object that impacts...), the importance of each
39 stage varies. Shock phase is usually described as one of the main cause of failure
40 for large containers [14] or in the case of low-strength impactors. However when
41 the size of the cavity is similar to the size of the tube, cavity stage becomes the
42 main cause of deformation and failure of the tank.

43

44 The conclusions obtained from the previous works are the basis to propose
45 improvements in the vulnerability of fluid-filled tanks subjected to the HRAM
46 phenomenon. It has to be remarked that the works in which HRAM attenuation

47 methods have been proposed are very scarce. In 1983 A. Copland [24] evaluated
48 the ability of different inerting agents to attenuate HRAM in armoured vehicles.
49 Two different containers were impacted by 12.7 mm AP bullets and 11.9 mm
50 steel spheres. The results indicate that the destructive effects of HRAM may be
51 enhanced by the addition of the inerting agent called “Explosafe” to liquid con-
52 taining cells, while the addition of the foam studied delayed the pressure pulse
53 and reduced its value contributing to attenuate the effects of HRAM. Other pas-
54 sive fuel tank inerting systems can be found in the work of S. McCormick et al.
55 [25] where a review about both fuel tank fillers and systems which surround the
56 fuel tanks is presented. The work is focused on the capability of different systems
57 to suppress fire in and from ground combat vehicles fuel tanks. D. Townsend et
58 al. [26] used two different techniques in order to reduce the shock pressure waves
59 which are generated in HRAM: thin air-filled baffles introduced inside the fuel
60 tank and bubbling air through the fluid. These two techniques consist in intro-
61 ducing low impedance solutions and hence disrupt or disperse the shock wave
62 produced in the fluid by the projectile impact. The mitigation effect for both tech-
63 niques reaches approximately a 50 % of reduction in the pressure wave in some
64 region of the fuel tank, and therefore it decreases the damage induced in the struc-
65 ture. Another work that proposed an attenuation technique is the one developed by
66 Peter J. Disimile et al. [27]. In this case, it has been also analysed the mitigation
67 of shock waves using wedged bars placed inside the water filled tank. These ele-
68 ments are specially designed to reduce the shock pressure wave by the destructive
69 interference between the original pressure wave and its reflections. It is shown
70 that the proposed technique allows reducing the pressure measured in the sensors
71 inside the fuel tank up to a 60 %. These two works successfully reduced the shock

72 pressure wave and therefore the damage induced in the structure. However, as it
73 was said previously, depending on the studied impact conditions and the structure
74 characteristics in which the HRAM is generated, the shock pressure wave may not
75 be the most damaging stage.

76

77 The cavity expansion can be considered as the major cause of deformation
78 and failure in the tanks in which the size of the cavity generated inside the tank
79 is similar to the size of the mentioned tank [22, 23]. These cases could occur in
80 high velocity impacts of metallic fragments against small range aircrafts or fight-
81 ers. Therefore, in this work it is proposed an attenuation method focused in the
82 reduction of the cavity expansion, instead of the reduction of pressure waves. In
83 this case, a honeycomb structure is placed inside the fluid filled tank, so that when
84 the cavity grows inside the tank, the honeycomb structure gets deformed plas-
85 tically, absorbing part of the energy transferred into the fluid. It is well known
86 the high energy absorption to density ratio of honeycomb or lattices structures
87 [28, 29, 30, 31, 32], consequently, it is expected that the structure protected with
88 honeycomb will be subjected to a less damaging loading case. As it is well known
89 honeycomb low density will not counteract with the effort in reducing the weight
90 on aircraft structures. The different orientation possibilities, in which the honey-
91 comb structure can be placed inside the tank, are analysed in order to obtain the
92 best configuration to attenuate the HRAM effects on the structure when it is im-
93 pacted perpendicularly.

94

95 **2. Experimental description of the problem**

96 *2.1. Experimental set-up*

97 In this work, an experimental set-up has been used to carry out the tests in
98 which the performance of the HRAM attenuation method proposed is analysed.
99 Fig. 1 shows a sketch of the experimental devices used to accomplish and register
100 adequately the tests. All the experimental tests were done at the University Carlos
101 III of Madrid Impact Laboratory.

102

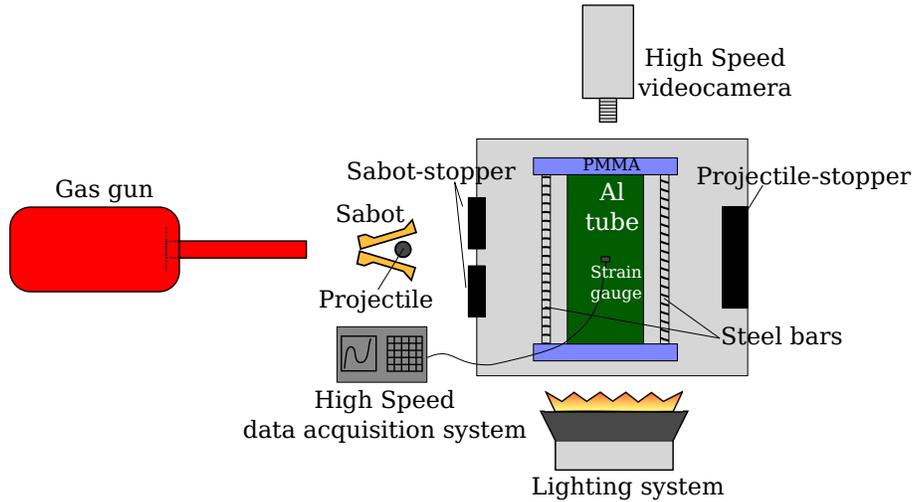


Figure 1: Sketch of the experimental set-up used

103 The structure analysed is a 6063-T5 aluminium tube ($150\text{ mm} \times 150\text{ mm} \times$
104 750 mm and 3 mm thickness) that has been filled with fluid to study the HRAM
105 effects. According to the recommendations of the Advisory Group for Aerospace
106 Research and Development (AGARD) [2, 3] no fuel was used in any of the experi-
107 mental tests due to the risk of fire; replacing it with water. The tubes are closed by
108 two PMMA windows (30 mm thick) allowing the recording of the impact process.

109 Four steel bars joint the PMMA and the tube without pre-stressing it; therefore it
110 is needed to use a sealant in the contact between the tube and the PMMA to assure
111 the water tightness of the tube. This set-up is based firstly in the work of Nishida
112 et al. [33], and then modified by D. Varas et al. [1].

113

114 The projectile used was a tempered steel sphere (12.5 mm diameter and 8 g of
115 mass and at least ~ 60 HRC). Its geometry helps to the repeatability of the test and
116 due to its high strength no deformation can be seen after the test, so the energy ab-
117 sorbed by the projectile can be neglected. The projectile was launched at 900 m/s
118 by a one-stage light gas gun, manufactured by Thiot Ingenierie. The gas gun uses
119 helium that is pressurize up to 270 bar to accelerate the projectile. The barrel is
120 4.5 m long and its calibre is 25 mm; due to the diameter differences between barrel
121 and projectile the use of a sabot is needed. The sabot is designed to be opened in
122 two valves. A steel structure stops the valves of the sabot preventing its impact
123 against the tube, and allows the impact of the projectile in the tank. After the pro-
124 jectile perforates the whole tube, a thick metal plate is used to stop it, preventing
125 also the possible rebounds.

126

127 As it can be seen in Fig. 1 the impact process has been recorded by means of a
128 high speed camera Photron Ultima APX-RS. Based on previous tests performed,
129 a frame rate of 36000 fps was used, which is enough to observe adequately both
130 the projectile entry and perforation of the tube. As it was already said two PMMA
131 windows (closing the tube) were used to allow the recording of the impact process
132 inside the fluid, nevertheless it is worth to mention that two of the honeycombs
133 configurations used to attenuate the HRAM effects impeded viewing the inside of

134 the tube. However, the video is used to register the impact velocity and the cav-
135 ity evolution when no honeycomb is added. This kind of tests, in which impacts
136 at high velocity occurs, requires a proper lighting system; moreover taking into
137 account the shutter used of $1\mu s$. In this case an Arrisun 12 Plus lamphead with a
138 1200 W Hydrargyrum Medium-arc Iodide (HMI) lamp was used.

139

140 The aluminium tubes were instrumented with six strain gauges. Two of them
141 were located in the entry wall, near and far from the impact point (G1 and G2
142 respectively). Another two were placed in the exit wall at the same position as
143 the entry ones (G3 and G4, near and far from the impact point respectively) and
144 the last two gauges were located in the center of the lower and upper wall (G5
145 and G6) (see Fig. 2). A high speed acquisition system Dewetron DEWE-800 was
146 employed to register all the strain gauges data, using a sample rate of 1 MHz , as
147 well as to synchronise the data with the video recording.

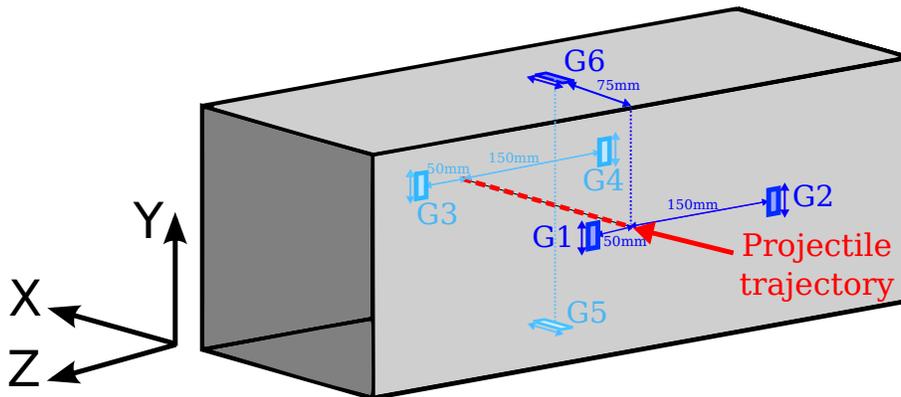


Figure 2: Sketch of the gauges locations

148 *2.2. Description of the HRAM attenuation method*

149 As it is said previously, this work proposes a method to attenuate the effects of
150 the HRAM phenomenon and hence reduce the vulnerability of fluid-filled struc-
151 tures. The work is focused on fluid-filled structures in which, due to its dimen-
152 sions, the most damaging process of the HRAM is the cavity expansion as was
153 observed in previous works [1, 16]. Therefore the method proposed should be
154 able to reduce the cavity formed in order to diminish its load onto the walls struc-
155 ture, and hence the damaging effects. The solution tested and studied consists in
156 placing a honeycomb structure inside the tube. It is expected that the honeycomb
157 panels could reduce the cavity expansion, dissipating through deformation the en-
158 ergy transferred by the fluid and hence alleviating the structure loading.

159
160 The honeycomb structures used consist of 5052 aluminium 50 mm thickness
161 panels, with a cell size of 6.35 mm and a nominal foil thickness of 63.5 μm . The
162 honeycomb geometrical parameters have been selected to maximize its resistance
163 but assuring a low density and a correct filling and circulation of the water inside
164 it. There are three possible configurations of the honeycomb structure depending
165 on how the cells are oriented inside the tube, Fig. 3. In the first configuration,
166 denoted as C-1, the honeycomb cells are placed perpendicularly to the impact di-
167 rection (X axis) and oriented to the largest dimension of the tube (Z axis). Since
168 the honeycomb panel thickness used is 50 mm, 15 panels of 150 mm \times 150 mm are
169 needed to fill the whole tube. In the second configuration, C-2, the honeycomb
170 cells are oriented in the same direction as the projectile trajectory (X axis), being
171 needed only three panels of 750 mm \times 150 mm. In the third case, C-3, honeycomb
172 cells are placed perpendicularly to the projectile trajectory (as in the case C-1),

173 but now they are oriented to the **third dimension of the tube (Y axis)**, therefore
174 three panels of $750\text{ mm} \times 150\text{ mm}$ are required, as happened in C-2. The three
175 configurations have been tested and analysed in order to decide which one is able
176 to produce the best attenuation effects on the walls structure, comparing it with a
177 non-protected case. To this end, an impact test on a filled tube without the hon-
178 eycomb structure inside was also performed. **Results presented concern to one**
179 **impact test for each configuration. Variability for cavity evolution, deformation**
180 **and strain data has been considered negligible attending to the repeatability on**
181 **previous tests done for aluminium tubes subjected to HRAM events [1].**

182
183 **It has to be mentioned that the weight added by the proposed solution has been**
184 **taken into account. Due to the very low density of honeycomb (83.2 kg/m^3), the**
185 **attenuation structure only represents a 6.8% of the aluminium tube-fluid system.**
186 **In addition the honeycomb could be implemented only in some zones that, due**
187 **to its position, are statistically more likely to be subjected to different kind of im-**
188 **pacts avoiding a catastrophic failure. Therefore the added mass would not be a**
189 **great disadvantage.**

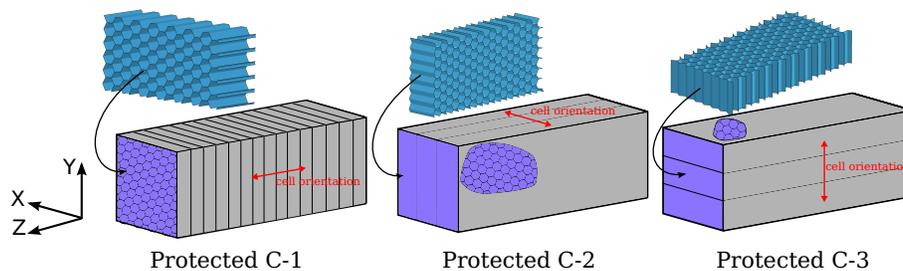


Figure 3: Sketch of the protected configurations

191 **3. Results**

192 In this section the results of the non-protected aluminium tube and the three
193 different protected tubes configurations are presented. Firstly, the images obtained
194 by the high speed camera are studied in order to obtain some qualitative compar-
195 ison of the HRAM phenomenon between the non-protected and protected tubes.
196 Then the residual deformation and the strain gauge data of the aluminium tube
197 walls are used to compare the HRAM attenuation effect of each configuration.

198

199 *3.1. High speed video sequence*

200 Some selected frames obtained from the high speed camera for the impact in
201 the non-protected tube and the C-1 protected tube are shown in Fig. 4. As it
202 was already mentioned, the honeycomb cells orientation in the other two config-
203 urations (C-2 and C-3) impedes viewing the inside of the tube and therefore the
204 images have not been presented. However, the video sequence images of Fig. 4
205 can be used to qualitatively compare both cases in the first instants and observe if
206 some remarkable change in the impact process happens in the protected case.

207

208 Fig. 4 shows how the cavity is formed in the wake of the projectile once it
209 penetrates the entry wall. This is very clearly observed in the non-protected case,
210 whereas in the case with the honeycomb protection, the cavity can be seen as a
211 kind of non-defined shadow. The projectile impact generates a pressure wave that
212 travels through the fluid, which is only visible in the non-protected case because
213 the presence of honeycomb impedes to visualize it. $111 \mu s$ after the impact, the
214 projectile is travelling through the fluid while the cavity continues growing. This

215 is observed in the protected case attending the growing of the non-defined shadow
216 mentioned before. As the cavity increases its size, the fluid pushes the tube walls
217 producing the deformation and the most damaging process in the tube [1, 18, 23].
218 Approximately 1 *ms* after the impact the cavity reaches its maximum size, in-
219 ducing the maximum loading state on the tube walls. That instant can be clearly
220 identified in the images of the non-protected case, whereas in the protected case
221 cannot be seen.

222

223 Taking into account the information obtained by the images, it can be con-
224 cluded that the HRAM process does not change qualitatively by the introduction
225 of the honeycomb protection. However, it is expected that certain phenomena, as
226 cavity expansion, may be affected by it. Due to the fact that the cavity size quan-
227 tification cannot be made by means of the video images (honeycomb cells impede
228 to have an accurate vision), the HRAM attenuation effect comparison between all
229 the considered cases will be made using the residual deformation and the strain
230 gauge data of the tube walls .

231 3.2. *Tube walls residual deformation*

232 In order to obtain the residual deformation of all the tube walls, it has been
233 used a laser extensometer MEL M27L/50 (Range =50 *mm*, Resolution=0.2 *mm*).
234 After the impact, the laser has been attached to an automatic positioning system
235 that is able to sweep the surface of a tube wall. The distance between the laser
236 and each point of the wall is obtained by the laser and registered in a high speed
237 acquisition system (Dewetron DEWE-600) at 1 *KHz*. Thanks to this distance, it
238 is possible to derive the deformation in all the points of each tube walls, allowing
239 to obtain a contour of the residual deformation. Fig. 5 presents a contour of the

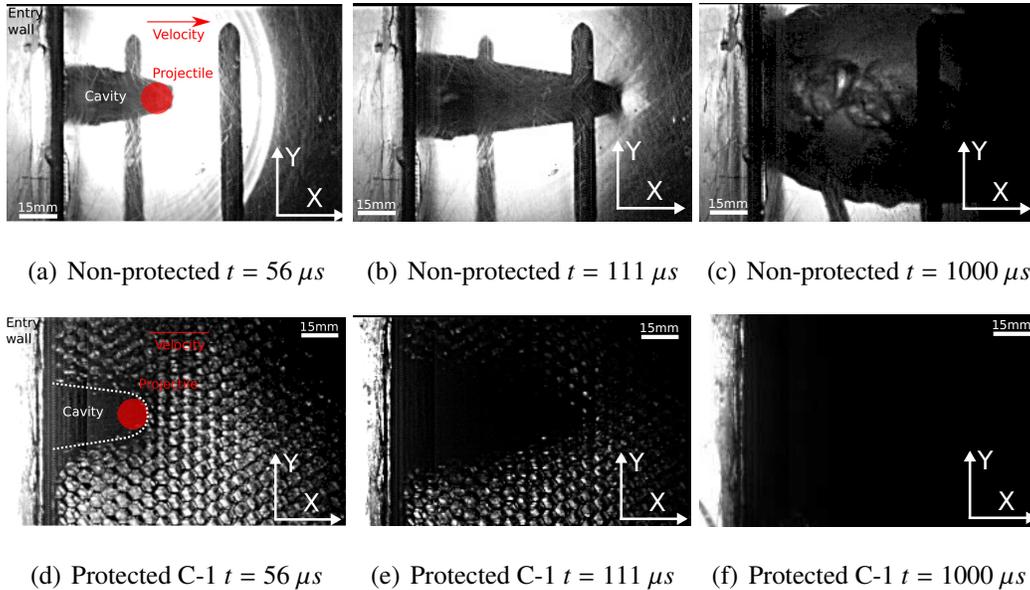


Figure 4: Video images obtained by the high speed camera

240 residual deformation of all the tube walls in the non-protected and protected con-
 241 figurations; the crossed-flags in the figure represent a vertical symmetry line. The
 242 images clearly show how the deformation is expanded from the impact location in
 243 all the cases due to the cavity expansion effect. However it can be seen that both
 244 the maximum residual deformation and the area deformed are not the same in the
 245 non-protected and protected cases.

246

247 The displacements obtained in the non-protected case can be explained taking
 248 into account the effects of the cavity evolution on each tube wall. The upper and
 249 lower wall (the walls which are not impacted by the projectile) have similar defor-
 250 mation results because they are placed symmetrically with respect to the impact
 251 trajectory. The cavity evolves pushing the fluid onto this walls equally. In the
 252 entry wall, the deformation is slightly higher than in the upper and lower wall.

253 The projectile impact produces the failure of the wall and the beginning of the
254 cavity generation, which causes a severe loading around the impact point. It has
255 to be noticed that the final deformation of the entry wall appears in the opposite
256 direction to the projectile velocity. This is explained because the high velocity
257 impact (900 m/s) produces only local deformation around the impact point, while
258 the fluid impulse (which in the entry wall goes in the opposite direction of the
259 projectile) is the governing mechanism that induces the deformation. The exit
260 wall has the highest deformation due to the fact that it is pre-stressed before the
261 impact of the projectile. The projectile, while travels inside the fluid, generates
262 an overpressure ahead which deforms the exit wall before being impacted. Then
263 the impact of the projectile and the cavity expansion continue loading the wall
264 increasing the deformation far from the impact point [16].

265

266 Regarding the protected cases, it can be seen that the permanent deforma-
267 tion suffered by the walls follows the same trends as in the non-protected case.
268 This is due to the fact that the phenomena that produce the loading of each wall,
269 previously explained, are the same in these cases. However, it can be noticed
270 a reduction in the permanent deformation for all configurations and tube walls
271 when comparing to the non-protected case. This is produced by the mitigating
272 effect over the cavity expansion that the honeycomb cells produce. The honey-
273 comb cells are deformed by the expansion of the cavity, partially absorbing the
274 energy transferred into the fluid by the projectile and hence reducing the load over
275 the walls. Nevertheless the reduction achieved is not the same for all the pro-
276 tected cases because of the asymmetrical effect created by the orientation of the
277 honeycomb cells in each configuration.

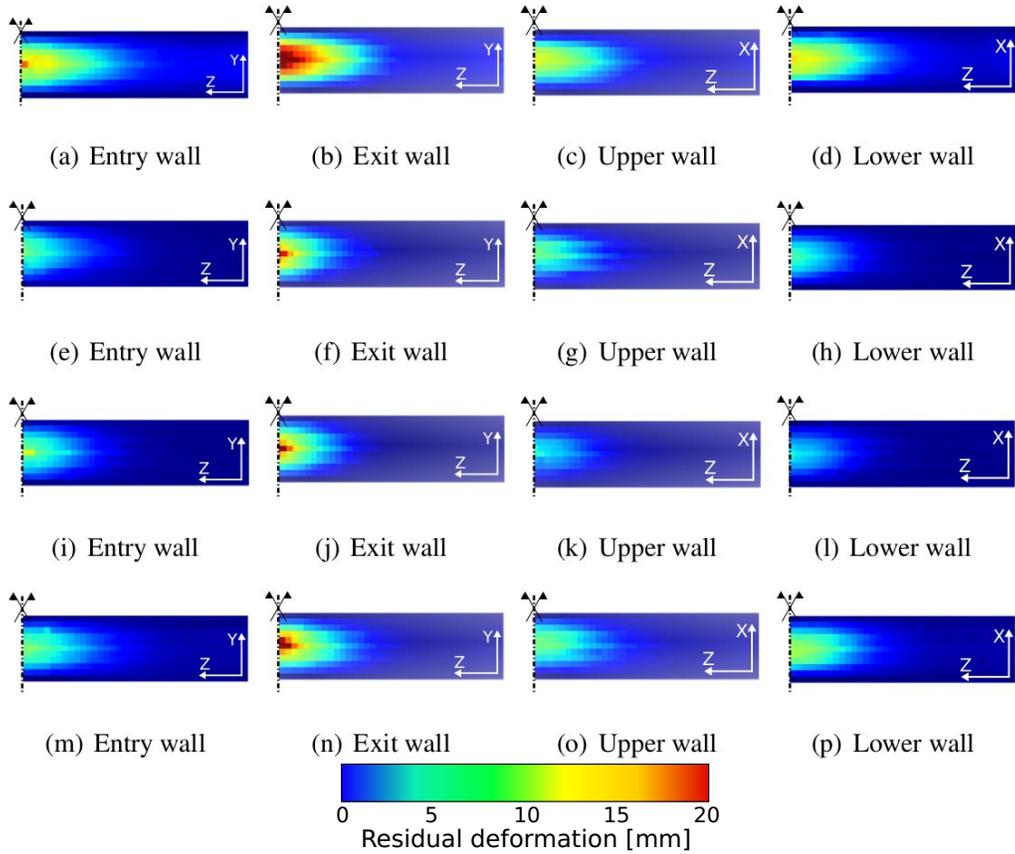


Figure 5: (a)-(d) Non-protected. (e)-(h) Protected C-1. (i)-(l) Protected C-2. (m)-(p) Protected C-3. **Contours of permanent out plane deformation plot on aluminium tube walls.**

278 In order to compare quantitatively the different protected configurations stud-
 279 ied, Fig. 6 shows the permanent out of plane deformation along the middle path
 280 (along axis Z) for all the tube walls (identified in the image with a red line, while
 281 impact position is identified with a red arrow). The maximum displacement in all
 282 the cases occurs in the central point of the tube, as it was expected. The first thing
 283 that can be observed is that, as it was already mentioned, the deformation in all
 284 the protected tubes is smaller than in the non-protected case. The differences are

285 now more evident than in the deformation contours plot showed in Fig. 5. It has to
286 be mentioned that the decrease in the deformation values affects the global shape
287 of the permanent displacement in the walls. Therefore, the honeycomb protection
288 makes the HRAM effect on the walls more located around the impact point. The
289 cavity produced by the projectile in the non-protected case is able to freely expand
290 affecting areas far from the impact point. It can be seen that the non-protected tube
291 shows some permanent deformation on both extreme sides, whereas the protected
292 cases are hardly deformed. This can be important to avoid that the HRAM phe-
293 nomenon affects contiguous structure elements.

294
295 Regarding the honeycomb protected cases, it is observed that in the entry and
296 exit wall (the walls impacted by the projectile) almost no differences appear, al-
297 though in both cases the honeycomb protected case C-2 slightly shows lower
298 deformations in the walls except in the region close to the holes. The upper and
299 lower wall, however, show a clear difference between the protected cases. The
300 major reduction in the permanent deformation is obtained in the honeycomb case
301 C-2. The configuration C-1 and C-3 show the same results in the upper wall but
302 different in the lower wall because the honeycomb modify slightly the projectile
303 trajectory. As the projectile trajectory may be closer to upper wall than lower, this
304 will increases cavity loading on the wall and therefore deformation. Taken into
305 account the average of the deformation values obtained in the upper and lower
306 walls, it can be concluded that the honeycomb configuration C-3 is the worst in
307 terms of deformation reduction.

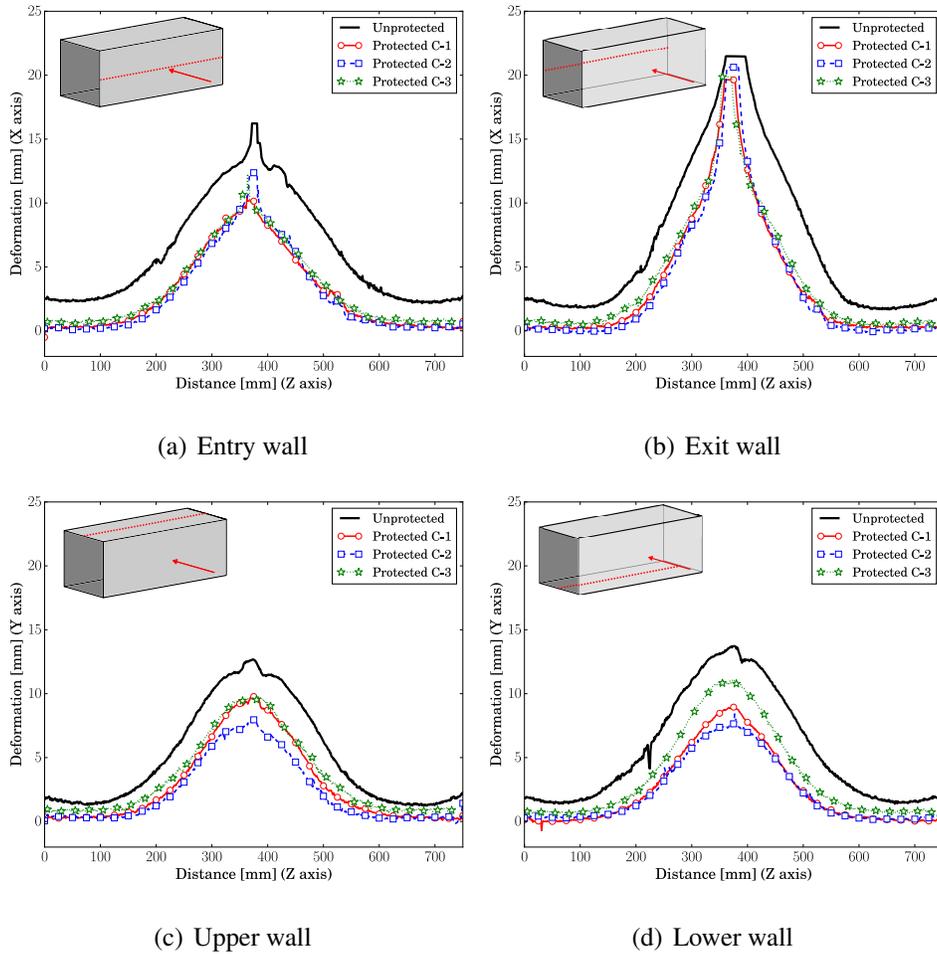


Figure 6: Permanent out of plane deformation in aluminium tube walls

308 *3.3. Strain data in aluminium tube walls*

309 The permanent walls deformation previously studied has shown that the hon-
 310 eycomb protection helps to reduce the HRAM effects. In order to try to understand
 311 how the HRAM phenomenon affects the surrounding walls during the impact pro-
 312 cess, the strain gauges data obtained in the experimental tests have been analysed.
 313 Fig. 7 shows the strain time history in different points of the tube walls, for both

314 non-protected and protected cases. All gauges show that the strain in the non-
315 protected walls is higher than in the protected cases. In the images it is highlighted
316 in red the position of the studied gauge in the tube.

317

318 Fig. 7(a) depicts the strain time history of the gauge located near the impact
319 point in the entry wall (gauge G1). It is observed that until approximately 0.18 ms
320 the curves are similar for all the configurations, whereas from that instant the
321 strain in the protected configurations is lower than in the non-protected case. This
322 behaviour is due to the fact that in those first instants, the honeycomb does not
323 produced any significant change (neither in the velocity of the projectile nor the
324 phenomena generated) as it was already described attending Fig. 4. Nevertheless,
325 when the cavity starts to grow around the impact point, the honeycomb protection
326 reduce its expansion and hence the loading effect on the entry wall. The strain data
327 shows that the configuration C-2 is the one which exhibits the lowest strain fol-
328 lowed by configuration C-3 and finally C-1. The strain time history in this gauge
329 for all the configurations is registered only up to 0.4 ms after the impact because
330 the high shake produced by the impact in this zone leads to the debonding of the
331 gauge.

332

333 Fig. 7(b) shows the strain time history of the gauge located far from the impact
334 point in the entry wall (gauge G2). Unlike the previous gauge data, all the impact
335 process could be registered because in this region (150 mm far from the impact
336 point) the shake is lower, avoiding the debonding of the gauge. As happened
337 before, it can be distinguished a first region in which the differences between
338 the configurations are not clear (until 0.7 ms approximately) and a second region

339 where is clearly observed the reduction in the strain for the protected cases. These
340 two regions are related, as was already explained, to the cavity evolution and its
341 influence on the loading walls effect at different distances from the impact point.
342 In this case, as the gauge G2 is far from the impact point, the effect of the cavity in
343 the strain takes a longer time than in the case of G1. In addition, as the cavity finds
344 more honeycomb cells on its path, the honeycomb protection produces a higher
345 reduction on the strain values than in the case of the gauge G1. It can be observed
346 how the maximum strain value is obtained in the non-protected case at 1.5 *ms*
347 after the impact; close to the instant where the cavity reaches its maximum size
348 (~ 1 *ms*). Therefore, the maximum loading effect on the surrounding structure
349 can be related to the the maximum cavity expansion. Due to the attenuation effect
350 of the honeycomb structure, the strain registered in the protected cases is lower
351 and the maximum is reached sooner. Once the cavity has reached its maximum
352 size it starts to diminish, and the strain value is reduced due to the elastic recovery
353 of the wall. Finally, the data reaches a plateau that corresponds to the plastic
354 deformation of the tube. The protected configuration with the lowest strain values
355 is again C-2.

356

357 Regarding the strain in the exit wall, Fig. 7(c) shows the data obtained by the
358 gauge located far from the impact point (at the same position as gauge G2). It
359 is observed that the strain data is similar to the one registered in G2, previously
360 analysed. It can be seen also that up to ~ 1 *ms* all the cases show similar results.
361 This duration is controlled mainly by the impact to the exit wall and the initiation
362 of the cavity expansion. This observation could lead to think that projectile
363 velocity is not altered significantly by the presence of the honeycomb structure.

364 However, when maximum cavity expansion takes place, the results show again
365 that the protected configurations mitigate the HRAM effects on the tube. The
366 strain time history obtained in the gauge located near the impact point in the exit
367 wall (gauge G3) does not provide useful information because in all the cases the
368 gauge is debonded few microseconds after the projectile hits the mentioned wall.

369

370 Finally, Fig. 7(d) shows the strain time history of the gauge located in the
371 central point of the upper wall (which is not impacted by the projectile). It is
372 observed that the strain values are higher in this point than in the other gauges.
373 This is probably due to the fact that the gauge is located just above the projectile
374 path and in a place where the cavity reaches its maximum size, producing a severe
375 loading on the upper wall. At approximately 0.5 *ms* after the impact the gauge for
376 the non-protected case and for the configuration C-1 are debonded due to the high
377 impulse generated by the cavity. This does not happen in the other configurations,
378 which would corroborate the HRAM mitigating effect of those protected cases.
379 It can be seen that the protected configuration C-2 obtains the major reduction
380 of strain once the cavity is totally expanded (~ 1 *ms*), before than in the non-
381 protected case as was previously explained and showing a lower residual strain,
382 confirming all the previous finding obtained for the permanent deformation.

383 The results shown in Fig. 6 and 7 indicate that the honeycomb protection is
384 able to reduce the deformation of the walls, and therefore the vulnerability of the
385 tubes subjected to the HRAM phenomenon. It has been observed that the best
386 protected configuration in terms of deformation and strain reduction is the con-
387 figuration C-2. In order to analyse the attenuation of the HRAM effects achieved
388 by this configuration, it is obtained a contour map which represents the reduction

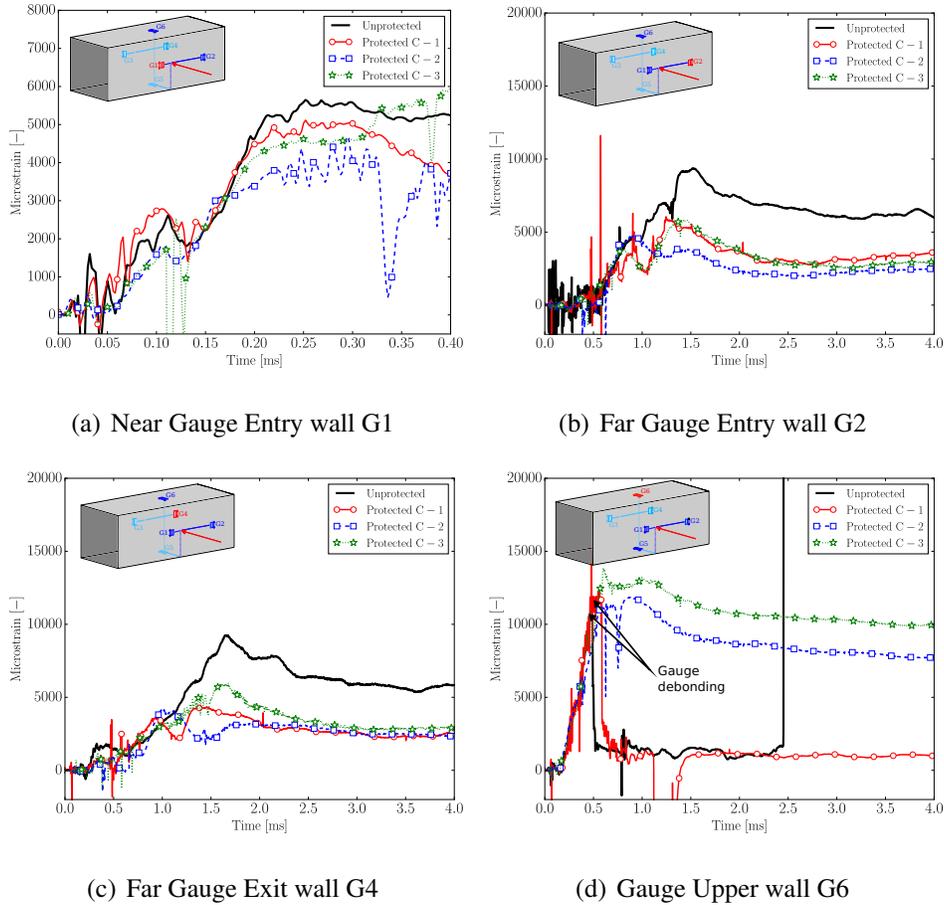


Figure 7: Strain gauge information

389 of permanent deformation in the different tube walls of the protected case C-2,
 390 compared to the non-protected case (Fig. 8). It can be observed that the major
 391 reductions are obtained near the impact point of the exit wall, which is where
 392 the maximum deformation of the tube appears. Nevertheless, taking into account
 393 the reduction of maximum deformation in each wall, it can be concluded that the
 394 higher attenuation is reached in the lower wall, where a reduction of 46% (com-
 395 pared to the non-protected case) is obtained. Therefore it can be concluded that

396 the attenuation effect is more important, in relative terms, where the cavity ex-
 397 pansion is the main loading case. It has to be mentioned that the pictures show
 398 some asymmetrical differences in the results, because as it was explained earlier
 399 the honeycomb could induce slight differences on projectile trajectory.

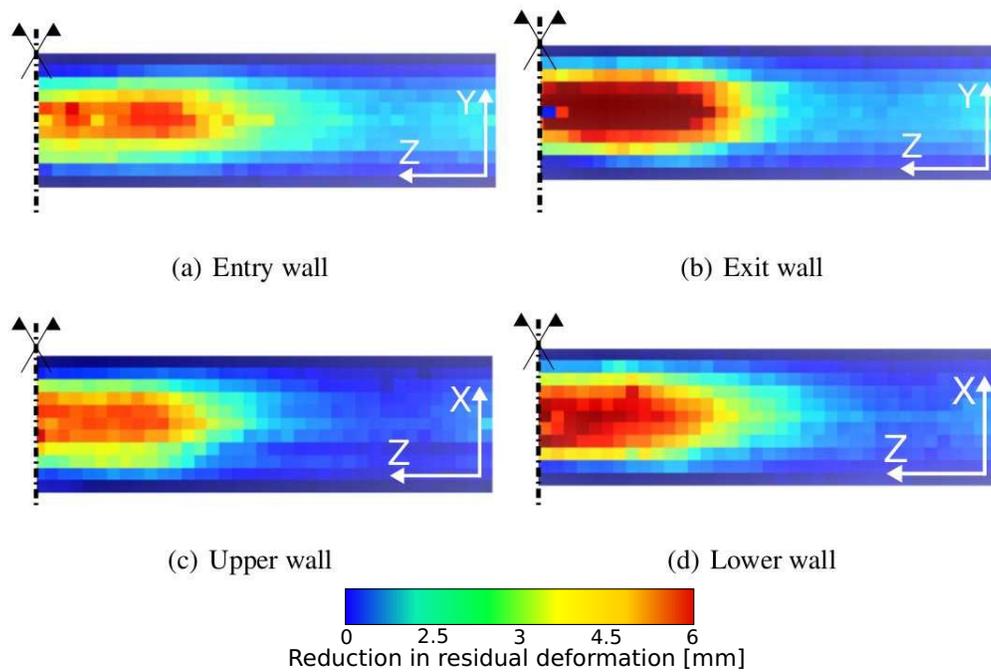


Figure 8: Reduction in the deformation tube walls.

400 4. Analysis of the HRAM attenuation method

401 In light of the results previously shown, it can be concluded that the hon-
 402 eycomb panels reduce the vulnerability of a structure subjected to the HRAM
 403 phenomenon. First of all, it is necessary to clarify if the attenuation produced by
 404 the honeycomb is due to the projectile deceleration generated by the resistance
 405 of the honeycomb to its penetration (lower projectile velocity means lower cavity

406 expansion) or to the resistance of the honeycomb to the expansion of the cavity.
407 To this end a simple analytical model has been implemented to model the de-
408 celeration of the projectile on a protected and non-protected configuration. The
409 deceleration produced by the fluid has been obtained according to the drag of a
410 spherical projectile inside a fluid (more information can be found in [1] where the
411 present approach is validated). The deceleration obtained on the aluminium tube
412 walls and in the honeycomb thin walls has been obtained using the energy balance
413 equation for piercing penetration [34, 35]. The number of honeycomb thin walls
414 has been obtained to model each impact on each honeycomb thin wall. For the
415 model, only the worst case in which the projectile perforates all the cell walls has
416 been taken into account.

417 In Fig. 9 it can be seen the projectile velocity with respect the projectile dis-
418 placement for a non-protected and a protected configuration. It can be seen that
419 velocity differs gradually with the displacement up to a maximum reduction on
420 the final velocity of only ~ 30 m/s in the protected configuration. Moreover in
421 the first instant of the impact, where the velocity is higher and the cavity starts
422 to evolve, velocity differences are negligible. These observations confirm that the
423 projectile velocity is hardly affected by the presence of the honeycomb. Therefore
424 the major role on the HRAM attenuation effects is due to the honeycomb resis-
425 tance to cavity expansion.

426

427 In order to analyse how the honeycomb attenuates the HRAM effects and to
428 understand the differences between the protected configurations tested, regarding
429 the mitigation effect obtained, it is studied the honeycomb structure deformation
430 inside the tube. Finally, an analysis relating the cavity size and the tube wall de-

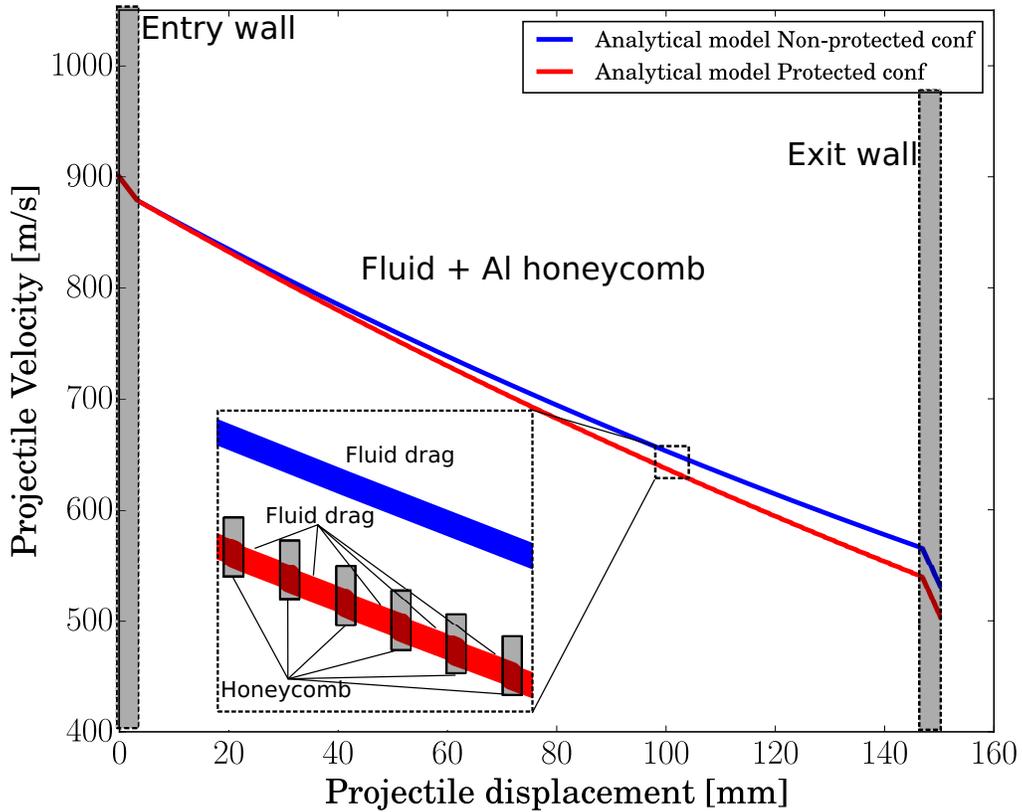


Figure 9: Analytical model for velocity deceleration.

431 formation is performed.

432

433 *4.1. Honeycomb structure deformation*

434 In order to analyse the honeycomb structure deformation produced by the
 435 HRAM loading, the tubes and the honeycomb structure are cut in two halves in
 436 a plane that is perpendicular to the longitudinal direction of the tube (Z axis) and
 437 that contains the projectile path. The cut has been done using a circular saw taking
 438 care of not modifying the damage and deformation produced during the impact.

439 The analysis has been conducted in order to understand the performance of each
440 configuration.

441

442 Fig. 10 shows a normal view and a perspective view of the cut plane for all the
443 protected configurations tested. It is included also the maximum dimension of the
444 deformed honeycomb structure in the different axes. The images of the config-
445 uration C-1 show very clearly how the honeycomb has been deformed along the
446 projectile path. The projectile impacts the tube and perforates all the honeycomb
447 cells in its path. As it is seen in Fig. 9 neither projectile velocity nor the trajectory
448 is affected noticeable by the presence of the honeycomb. As the projectile travels
449 through the tube, the cavity generated on its trajectory evolves and deforms the
450 impacted honeycomb panel that try to avoid its expansion. Due to this loading
451 the impacted honeycomb panel is broken in two parts and its deformation occurs
452 mainly in the lower-upper tube walls direction (Y axis). The fluid is able to flow
453 through the cells oriented in the longitudinal direction of the tube (Z axis), so the
454 damage of those adjacent honeycomb panels is much lower (only honeycomb cell
455 debonding can be observed). It has to be noted that in this configuration 15 honey-
456 comb panels of 50 mm are used to fill the entire space of the tube, being the cells
457 oriented in the longitudinal direction of the tube (Z axis). Therefore due to the
458 absence of connection between the different panels, the deformation produced by
459 the cavity expansion does not reach the adjacent ones. It has to be remarked that
460 the use of other thickness for the panel will probably have influence on the results.

461

462 Regarding the honeycomb structure deformation, it can be said that the main
463 absorbing energy mechanism is the bending of thin honeycomb walls [36, 37, 38],

464 but also some energy is dissipated by the debonding of the honeycomb cells in the
465 adjacent panels. Certainly this energy transferred from the fluid to the honey-
466 comb structure alleviates the tube loading, mitigating the HRAM effects. Finally,
467 the similarity between the shapes of the honeycomb deformation and the cavity,
468 leads to think that the maximum expansion of the cavity is similar to the maxi-
469 mum deformation of the honeycomb panel. This could be a design key to know
470 which solution or configuration could contribute in a better way to improve the
471 vulnerability of a structure, because the smaller the cavity, the lower would be the
472 deformation of the structure.

473

474 It has been previously seen that the protected configuration C-2 shows the best
475 results in terms of reduction of residual displacement. This configuration con-
476 sists of three honeycomb panels with the cells oriented parallel to the projectile
477 trajectory (X axis). Fig. 10 shows that the three honeycomb panels are equally
478 deformed along the projectile path. The projectile impacts the tube and travels
479 through the honeycomb cells while the cavity try to evolve radially deforming the
480 honeycomb cells that are all around it. The cavity is much more restricted in this
481 configuration than in configuration C-1 or C-3, because in the other cases the hon-
482 eycomb cell direction matches with one radial direction of the cavity expansion.
483 **The images show that for this configuration the dominant failure mechanism is cell**
484 **wall buckling, which leads to a higher resistance.** Thus the energy dissipated by
485 the honeycomb occurs in a more efficient way for configuration C-2. This would
486 explain why the better results are obtained with this configuration. Although in
487 this case the cells allow the fluid to flow in the projectile direction, the results
488 obtained in the entry and exit walls are similar to the other protected cases. This

489 could be explained due to the fact that the deformation in these walls is mainly
490 influenced by the projectile impact and the fluid impulse around the impact point,
491 effects that are negligibly affected by the different configurations of the honey-
492 comb.

493

494 Finally, the honeycomb panels deformation for the protected configuration C-
495 3 can also be observed in Fig. 10. This configuration consists of three honeycomb
496 panels with the cells oriented in the lower-upper wall direction of the tube (Y
497 axis). It is observed that the honeycomb deformation appears mainly in the mid-
498 dle panel, which matches with the projectile path. The cavity evolves pushing
499 the honeycomb wall cells towards the longest tube direction (Z axis). The images
500 show that as it occurs in configuration C-1, bending of thin honeycomb wall is
501 the dominant failure mechanism. Due to the orientation of the cells, the fluid can
502 flow in the lower-upper wall direction without generating a significant deforma-
503 tion on the adjacent honeycomb panels, like in the configuration C-1. This could
504 explain the smaller reduction of deformation in the upper and lower walls for the
505 protected configuration C-3. Taking into account the orientation of the cells, it
506 could be thought that the entry and exit walls would be more protected because
507 the cavity expansion is restricted in those directions, nevertheless the residual dis-
508 placement and gauges show very few differences. As it was already explained,
509 the effect of the honeycomb is less noticeable in these walls since the projectile
510 velocity is hardly affected.

511

512 The analysis of the honeycomb deformation performed shows that the pro-
513 tected configuration C-2 achieves the better attenuation results, especially in the

514 upper and lower walls, because the cavity expansion is more restricted due to in
 515 this configuration cell wall buckling is the dominant failure mechanism, increas-
 516 ing honeycomb resistance. It can be concluded that the energy dissipated by the
 517 deformation of the honeycomb produces a reduction in the energy transferred to
 518 the structure, attenuating the HRAM effects and reducing the vulnerability of a
 519 structure subjected to the HRAM phenomenon.

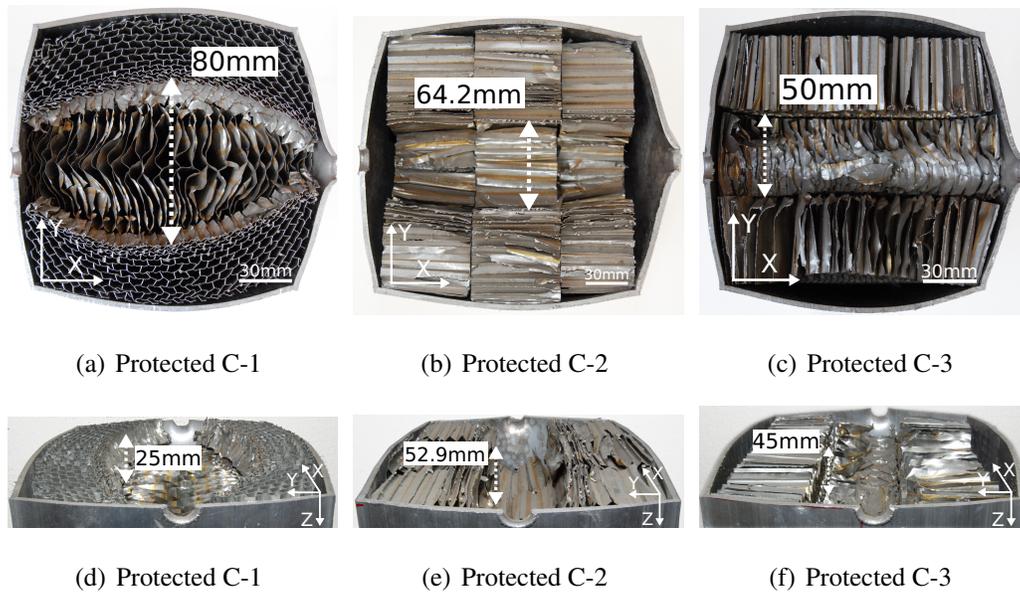


Figure 10: Images of the cut plane of each protected configuration

520 *4.2. Cavity size and tube walls deformation*

521 Finally, it is performed an analysis relating the cavity size and the tube walls
 522 deformation. In the Fig. 12 the volume of the estimated cavity is compared with
 523 the volume generated by the expansion of the tube walls.

524

525 Concerning the volume of the cavity, as it was already commented, the maxi-
526 mum cavity size can be obtained for the non-protected case by means of the high
527 speed camera. As it can be seen in Fig. 11, the cavity geometry is similar to an el-
528 lipsoid and therefore its axes can be obtained from this image. In the upper-lower
529 wall direction (Y axis) the size of the cavity is 120 mm , while in the entry-exit wall
530 direction (X axis) the size is obtained as the final deformed distance between these
531 walls in the projectile trajectory (190 mm). The images does not show the size in
532 the longitudinal tube direction (Z axis), but according to other works [17, 23, 16]
533 in which similar cases have been studied numerically, it can be established that
534 this size is the same as in the upper-lower wall direction (Y axis). In the pro-
535 tected cases, as it has been said previously, the honeycomb panels avoid viewing
536 the inside of the tube. However taking into account the similarity between the
537 shapes of the honeycomb deformation and the expected cavity, it has been made
538 the hypothesis that the maximum expansion of the cavity matches with the max-
539 imum deformation of the honeycomb panel (already detailed in Fig. 10). It has
540 to be mentioned that this hypothesis cannot be made in the honeycomb cell direc-
541 tion since the fluid can flow freely across them and only slight honeycomb cell
542 debonding is observed. In this direction it is expected that the size of the cavity
543 does not show any noticeable alteration with the non-protected case.

544

545 Concerning the volume of the tube walls generated by the expansion of the
546 cavity, the value has been obtained using the expanded displacement shown in
547 Fig. 5. In order to obtain the contour, each wall is divided in 11×75 regions.
548 Therefore, each region represents an area of $13.63 \times 10\text{ mm} \times \text{mm}$, where the av-
549 eraged value of the out of plane residual deformation is obtained. The volume

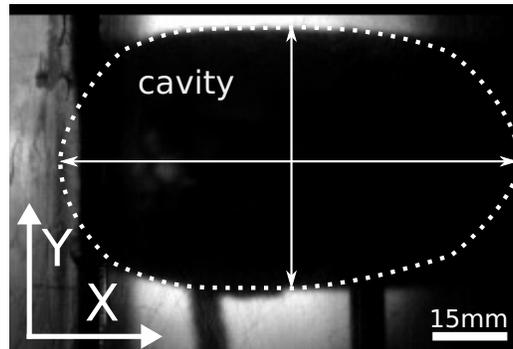


Figure 11: Video images obtained by the high speed camera. Non-protected $t = 472 \mu s$

550 generated has been obtained adding all the region averaged value of the residual
551 deformation and multiplying by the region surface.

552

553 As it can be seen in Fig. 12, there is an adequate correlation between both
554 volumes. This trend confirms the main hypothesis of the work in which the re-
555 duction of cavity expansion by the use of the honeycomb alleviates the loading
556 level of the structure. Moreover, it confirms that the hypothesis made to obtain
557 the volume of the cavity in the protected cases are well established. It can be seen
558 that an important reduction of the wall displacement volume is obtained due to
559 the reduction of the cavity size for all protected configurations. As it can be seen
560 previously, the best performance is exhibited for the configuration C-2, followed
561 by C-1 and finally C-3. C-2 configuration is able to obtain a reduction of a 54%
562 in terms of the expanded volume of the walls produced by a similar reduction of
563 the cavity size.

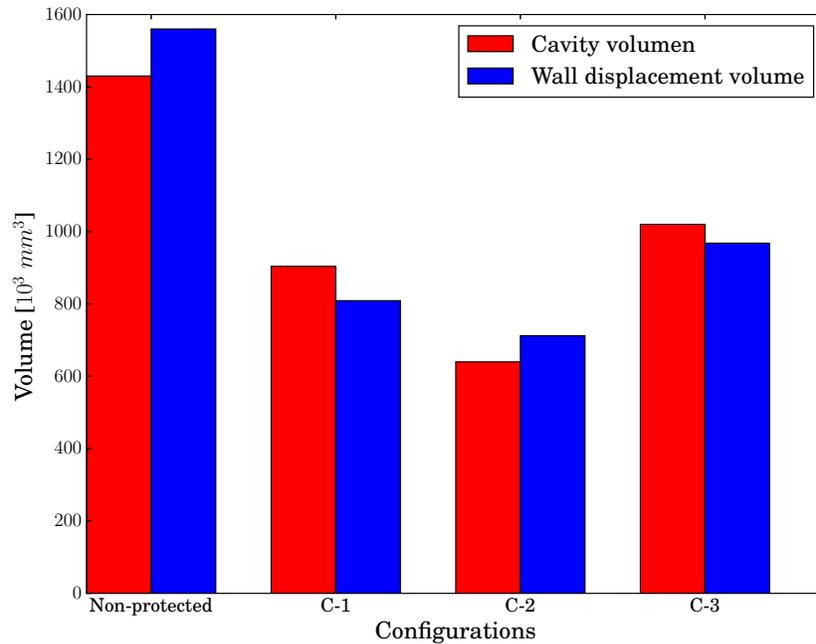


Figure 12: Reduction in the deformation tube walls and in the cavity expansion

564 5. Conclusion

565 In this work a method of HRAM attenuation is proposed. The solution tackles
 566 the expansion of the cavity, which has been shown in previous studies as the most
 567 damaging event of the HRAM phenomenon when the size of the cavity is similar
 568 to the size of the tube. The method consists in placing honeycomb panels inside
 569 the fluid filled structure that is subjected to the HRAM phenomenon . Three dif-
 570 ferent configurations have been studied comparing the results to the non-protected
 571 configuration, leading to the following conclusions.

- 572 • The proposed method does not alter qualitatively the different phases of the
 573 HRAM. It has been shown that the cavity expansion is restricted by this
 574 device and therefore it is obtained smaller residual deformation in the tube,

575 and consequently a less damaging phenomenon.

- 576 • The proposed attenuation method does not counteract the effort in reducing
577 the weight on aircraft structures due to low honeycomb density. Moreover,
578 the honeycomb cell size assures a correct filling and circulation of water
579 inside them.
- 580 • All the protected configurations achieve a negligible deformation far enough
581 from the impacted point, reducing the possible damage that can be produced
582 on adjacent structures.
- 583 • It has been shown that the reduction of cavity expansion matches almost
584 perfectly with the reduction of residual deformation. This fact confirms
585 that for this geometry the cavity is the most damaging phase in the HRAM
586 phenomenon. It has to be remarked that for other structure geometries, in
587 which the tube is much bigger and the cavity expansion is not the most
588 damaging event, other methods have to be studied and compare it with the
589 present one to analyse which is the most efficient one.
- 590 • Once studied the three configurations, it has been seen that the most efficient
591 one is the protected configuration C-2. This is explained because it is the
592 one that is able to restrict the cavity expansion in a more efficient way,
593 limiting it in the two perpendicular direction of projectile trajectory.
- 594 • The orientation of the panel has been proven as the key parameters to op-
595 timize attenuation purposes for these impact conditions. However, as it can
596 be seen for configuration C-1 other variables as the thickness of the panel
597 may have an additional effect on the protection performance.

598 • For the best configuration, it has been obtained up to a 54 % of reduction in
599 the expanded wall displacement volume produced by a similar reduction in
600 the cavity size. Therefore the attenuating effect of the HRAM phenomenon
601 is successfully reached.

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