Ring Resonators with Sagnac Loops for Photonic Processing in DWDM Backbone Networks

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Abstract – In this paper, optical configurations based on ring resonators (RR) with an internal Sagnac (SG) loop in the feedback path, are analyzed in terms of their amplitude response and dispersive properties for filtering and chromatic dispersion managing in digital transmission systems over amplified single-mode fiber (SMF) spans in DWDM backbone networks. Design issues for the architecture as regards quadratic dispersion and magnitude distortion are provided. The RR+SG compound filter provides frequency tunability of the amplitude and dispersion peaks by adjusting a coupling coefficient of an optical coupler, with no need for using integrated thermo-optic nor current-injection based phase shifters. The configuration can be employed as an additional structure for a general RR-based design and synthesis architecture, allowing bandwidth increase of dispersion compensators and flexibility. The performance of a compound filter consisting of a two RR in series stage and a RR+SG filter are reported as a more compact and effective solution for existing multi-channel SMF backbone links operating at high bit rates. Design guidelines of an integrated ring resonator based on polymer technology for showing feasibility of the proposal is reported.

Keywords – BER, dispersion compensation, ring resonator, Sagnac interferometer, tunable filters.

I. INTRODUCTION

Nowadays ring resonators (RR) are widely used for photonic processing in optical communication systems. RR have applications as routers in Self-Routing Frequency Division Multiple Access (SR-FDMA) networks [1, 2], to inform the destination node that a packet has been transmitted and to which channel to tune its receiver [3], and for performance monitoring. They have also been used as filters [4] in Optical Frequency Division Multiplexing transmission systems (OFDM) [5], or in DWDM (Dense Wavelength Division Multiplexing) systems with carriers spacing of 50 GHz, or less [6]. They have also been used as chromatic dispersion compensating filters in high bit rate digital transmission systems [7], in lasers and in non-linear optical applications such as all-optical switches [8, 9]. Different technologies are reported for filtering and chromatic dispersion compensation, such as Fabry-Perot (FP), Planar lightwave circuits (PLC), Mach-Zehnder interferometers (MZI), arrayed waveguide gratings (AWG), thin-film dielectric interference filters (TTF), and conventional fiber Bragg gratings (FBG). General filter design techniques based on signal processing approaches are reported in [10] using compound lattice architectures with MZI and RR, including all-pass filters for dispersion control applications. More recently, tunable dispersion control with micro-electro-mechanical (MEM) actuated all-pass filter [11] was fabricated.

On the other hand, the analysis of a Sagnac (SG) loop in ring resonators (RR) has been reported as a tuneable optical filter [12-13] with ultra-narrow-bandwidth for use in Dense WDM systems. This proposal allows tunability achievement just by adjusting a coupling coefficient of an optical coupler, with no need for using integrated thermo-optic, nor current-injection based phase shifters.

In this paper, we focus on the filtering and dispersive properties of the RR with SG loop filter, for among others chromatic dispersion managing in digital transmission systems over amplified single-mode fiber (SMF) spans in DWDM backbone networks. In section 2 the transfer function is analyzed and design issues for the architecture are provided, section 3 is devoted to in line response and design issues in polymeric technology are reported in section 4.

II. FILTER ARCHITECTURE

The schematic of a RR with internal SG filter [12] is shown in Fig. 1, being $K_1$, $K_2$ the cross-coupling power factors, $\gamma_1, \gamma_2$ the corresponding power excess losses of the couplers, $T_x, T_y$ the power transmission of the corresponding feedback segments per roundtrip, and $L$ the total feedback loop length. The diagram in Fig. 1(b) shows the mirror

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equivalent model of the filter considering unidirectional propagation of the light, which makes easier the analysis of the structure. Considering this mirror model, the structure can be analyzed as an unidirectional ring resonator with internal transfer function dependent on the Sagnac 2x2 matrix parameters.

\[ g \equiv T_x = T_y \]  

(7)

The Z-transform of the transfer function of the SG with feedback in the mirror model, \( h(z) \), has the following expression:

\[ h(z) = \frac{E_{2f}}{E_{af}} = \frac{FT - (FT^2 - FR^2) \cdot T^* \cdot z^{-1}}{1 - FT \cdot T^* \cdot z^{-1}} \]  

(8)

where:

\[ T^* = g \cdot (1 - \gamma_1)^{\frac{1}{2}} \cdot (1 - K_1)^{\frac{1}{2}} \]  

(9)

A first approach to the transfer function of the compound structure in the Z-Transform domain is the following:

\[ H(z) = \frac{E_3}{E_1} = \frac{\rho - (1 - \gamma_1) \cdot h^*(z) \cdot z^{-1}}{1 - \rho \cdot h^*(z) \cdot z^{-1}} \]  

(10)

being:

\[ \rho = (1 - \gamma_1)^{\frac{1}{2}} \cdot (1 - K_1)^{\frac{1}{2}} \]  

(11)

\[ h^*(z) = g \cdot h(z) \]  

(12)

B. Magnitude response and resonance conditions for filtering

The complete Z-transform of the architecture can be obtained by using (8) and (12) in (10); then the zeros and poles of the transfer function can be obtained by factorizing numerator and denominator of the final expression:

\[ H(z) = \rho \cdot \prod_{i=1}^{2} \frac{(1 - c_i \cdot z^{-1})}{(1 - p_i \cdot z^{-1})} \]  

(13)

obtaining:

\[ c_i = \frac{g \cdot (1 - \gamma_1)^{\frac{1}{2}}}{2 \cdot (1 - K_1)^{\frac{1}{2}}} \cdot \left[ FT \cdot (2 - K_1) + (j)^{2(i-1)} \cdot \sqrt{FT^2 \cdot K_1^2 + 4 \cdot (1 - K_1) \cdot FR^2} \right] \]  

(14)

\[ p_i = g \cdot \left[ (1 - \gamma_1) \cdot (1 - K_1) \right]^{\frac{1}{2}} \cdot \left[ FT + (j)^{2(i-1)} \cdot FR \right] \]  

(15)

For designing a selective or notch tunable filter, complex conjugate poles have to be considered [12] and the conditions to be fulfilled are reported in Table I.
**TABLE I.**

<table>
<thead>
<tr>
<th>Resonance Conditions at $p_f$ for Complex Conjugate Poles</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>RR with SG filter</strong></td>
</tr>
<tr>
<td>Maxima condition</td>
</tr>
<tr>
<td>$g = \frac{1}{(1 - \gamma_1)^{1/2}(1 - \gamma_2)(1 - K_i)e^{-\alpha i}}$</td>
</tr>
<tr>
<td>Maxima frequencies*</td>
</tr>
<tr>
<td>$2\pi k = \frac{2\pi f_{1,2} n_{ef}}{c} L_T \mp \phi_s$</td>
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</tr>
</tbody>
</table>

* $k$ is an integer number, $n_{ef}$ the effective group refractive index of the waveguides.

Those equations are valid for the $K_1$ and $K_2$ values satisfying the equation:

$$K_1 < -1 + \sqrt{1 + 4A}$$  \hspace{1cm} (16)

being:

$$A = \frac{K_2 ((1 - K_2)/(1 - 2 K_2)^2}  \hspace{1cm} (17)$$

Under that condition, the values of the phases are given by:

$$\phi_s = \tan^{-1}\left[\frac{(2 - K_2)\sqrt{K_2(1 - K_2)}}{(1 - K_1)(1 - 2 K_2)^2 - K_1^2 (K_2^2 - K_2^2)}\right]$$  \hspace{1cm} (18)

$$\phi_{sc} = \arctan \left(\frac{\sqrt{-K_1^2(1 - 2 K_2)^2 + 16(1 - K_1)(1 - K_2)K_2}}{2(1 - K_1)(1 - 2 K_2)}\right)$$  \hspace{1cm} (19)

C. Quadratic dispersion and magnitude distortion of the RR+SG filter for chromatic dispersion compensation

From the expression in (13) the normalized group delay of the filter for $z = \exp(j \cdot \Omega)$ can be obtained as follows:

$$\tau_n = \sum_{j=1}^{N} \frac{|p_j| \cdot (\cos(\Omega - \phi_{pj}) - |p_j|)}{1 - 2 |p_j| \cos(\Omega - \phi_{pj}) + |p_j|^2} - \sum_{m=1}^{M} \frac{|c_i| \cdot (\cos(\Omega - \phi_{cj}) - |c_i|)}{1 - 2 |c_i| \cos(\Omega - \phi_{cj}) + |c_i|}$$  \hspace{1cm} (20)

In the latter equation, $|c_i|, |p_j|$ are the modules of the zeros and the poles, and $\phi_{ci}, \phi_{pj}$ are their phases, respectively.

Finally, the absolute quadratic dispersion of the filter can be found using:

$$D = -c \left(\frac{T}{\lambda}\right)^2 \cdot 2\pi \frac{d\tau_n}{d\Omega}$$  \hspace{1cm} (21)

where $c$ is the speed of light, $\lambda$ is the optical carrier’s wavelength and:

$$T = \frac{n_{ef} \cdot L_T}{c}$$  \hspace{1cm} (22)

The filter response is repeated with an spectral periodicity, or free spectral range (FSR), that equals $1/T$. It would be desirable that the RR+SG filter fits the general framework of all-pass filters, in order to approximate an arbitrary phase response with unitary magnitude response, except for non-ideal behaviors of photonic components. Examining equation (13) considering (14) and (15) we find that, unfortunately, the RR with a SG interferometer is not an all-pass filter. The consequence of this is a tradeoff between the quadratic dispersion reached and the magnitude distortion.

In Fig. 2 an example of design is considered for $K_1=0.3$ with a FSR equal to 25 GHz. The magnitude response in logarithmic scale (dB) is shown in Fig. 2(a) versus optical frequency deviation (GHz) with regards to the center frequency of the simulations, which equals 193.1 THz (around 1553nm). In Fig. 2(b) the quadratic dispersion of the filter in ps/\text{nm} is shown versus the same scale of optical frequency. By changing the coupling value $K_2$ the tuning of the filter is achieved, due to the fact that the phases of the conjugate pairs of zeros and poles increase while keeping their distance to the unit circle [14].

![Fig. 2. Magnitude response versus frequency for $K_1=0.3$, $g=0.6$ (a) and quadratic dispersion (b) of a RR+SG filter with FSR=25 GHz.](image-url)
As Fig. 2 shows, the RR+SG filter has a symmetrical magnitude response with regards to the center frequency and anti-symmetrical dispersion shapes in each half of the FSR.

As \( K_2 \) increases, the dispersion lobes separate more from each other, leaving a zero dispersion range with a flat shape in the middle of the FSR, see Fig. 2(b). This quick return from the dispersion peaks to zero is a good property to take advantage from when combining the RR+SG quadratic dispersion to other RR-based filters. Because the zeros and the poles have not inverse magnitudes, as it would happen for an all-pass filter, the design of Fig. 2 shows a magnitude distortion in frequency with maximum insertion loss of 3 dB. For this \( K_2 \) value, in order to have a higher dispersion peak, see Fig. 2(b), it is needed to adjust the roundtrip losses closer to the resonance condition, which results in unwanted higher magnitude distortion.

In order to avoid the effect of the poles and to have a simpler design no optical amplification is considered. Additionally, the design point must be far away from resonance conditions, different for each zero when they are not complex conjugated.

III. RR+SG BASED FILTERS AS DISPERSION COMPENSATION MODULES (DCM)

In addition to the analysis of the quadratic dispersion of filters, there is a need for testing the behaviour of the configurations when noise and digital signals appear at the reception stages. Actually, for a fixed bit error rate in an optical transmission system, there is an inversely proportional relation between the bit rate and the transmission distance. In this section we investigate the effect of including a RR+SG based filter (Fig. 3) at the reception stage of a simplified model of a backbone link.

Fig. 3 shows the group delay and quadratic dispersion of a compound design using a 2-RR in series and a RR+SG filter connected to its output. Two lossless RR in series with coupling factors of 0.84 and 0.68 with relative phase shift of 0.7 rads were considered. The design parameters of the RR+SG configuration are \( K_1=0.3, K_2=0.8, g=0.6 \) and \( \gamma_1 = \gamma_2 = 0.075 \), see Fig. 3. The periodicity of all the stages is 25 GHz, and so is the FSR of the total configuration.

In order to test the performance of RR-based filters in an optical digital transmission system operating at high bit rates, a simplified model of the backbone link has been built using the VPI Photonics™ v. 7.01 software simulation engine. Results reported in [14] shows a power penalty enhancement between 3-4 dB when the filter is emplaced at the reception stage of the link. Comparisons with conventional dispersion compensating fiber DCF, modules have also been reported.
The 2D prototypes consist of μRR with 5 microns radius with slab SiN core waveguides of 0.5 microns width on SiO2 cladding. Using liquid crystals cells as adjusting elements, simulations with commercial software in the 1550 nm band show FSR around 4 THz for LCs with 1μm length.

By increasing the RR radius to 300μm and using the effective refractive indexes of the waveguides corresponding to the polymeric technology [17], such as ncore=1.582 and ncladding=1.409, FSRs around 100 GHz can be obtained, fitting the DWDM spectral grid thus allowing applications for the standard SONET/SDH communications networks.

V. SUMMARY AND CONCLUSION

The optical configuration consisting of a ring resonator with an internal Sagnac loop (RR+SG) has been studied for chromatic dispersion managing in backbone SMF links. A mirror model of the configuration has been considered to obtain closed-form formulae of its transfer function, group delay and quadratic dispersion. We have examined graphically the frequency tuning of the dispersion peaks by changing the coupling factor in the Sagnac loop, with no need for using phase-shifting techniques. The magnitude distortion restriction of the RR+SG configuration has also been analyzed.

Additionally, we have presented results of a RR+SG based filter as a dispersion compensating module (DCM). Simulations have shown a power penalty enhancement between 3-4 dB when the filter is emplaced at the reception stage of the link. Another advantage of the RR-based filters as DCM is the periodicity of the transfer function, thus fitting multi-channel DWDM systems with a large number of optical carriers with maximum change in chromatic dispersion around 300 ps/nm for a 200 km SMF link in the complete C-band (1530-1560nm). Fabrication technology issues have also been considered.

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REFERENCES