A new set of failure criteria to predict composite failure in single lap bolted joints is proposed. The present failure criteria are an extension of Chang Lessard criteria considering a three dimensional stress field and including out of plane failure modes. The advantage with respect to other three dimensional failure criteria is the consideration of non linear shear stress strain relationship. The failure criteria were implemented in a finite element model and validated through comparison with experiments in literature. Stresses were calculated by a non linear finite element model developed in ABAQUS/Standard which considers material and geometric nonlinearities. A progressive damage model was implemented in a USDFLD subroutine. The model predicted the effect of secondary bending and tightening torque showing an excellent agreement with experimental results. Moreover, results were compared with those reported in literature using Hashin failure criteria. In addition, a parametric study was carried out to analyse the influence of friction coefficient and tightening torque.

1. Introduction

Composite structures are used extensively in aircraft structures because of their excellent mechanical properties combined with low density. Fastener joining is the most important method of assembling structural elements in the aerospace industry, due to its facility to assemble, disassemble and repair, and its tolerance to environmental effects.

For high responsibility applications on composite structures bolted joints should be carefully designed. The enhanced stress intensity factor at the surrounding of the hole and the weakness of the composite under out of plane loads, make the designing and assembly process more critical in the case of composite joints than in those based on metallic components. Structural safety should be ensured in aeronautical industry, thus the study of bolted joints in structural composite components have received considerable attention in both scientific literature and aeronautical standards [1 9].

A major goal of composite bolted joint research has been to determine the effect of various bolting parameters on the joint strength. The bolting parameters that have been studied include geometric factors [10], material properties [11], coefficients of friction [12], bolt shape [13], clearance [9], and torque [14,15]. These studies have provided strategies to design composite bolted joints avoiding catastrophic failure. The basic failure modes in bolted fibre reinforced materials are bearing, net tension and shear out failures. From these failure modes only bearing damage produces a progressive failure, thus composite bolted joints are designed to fail under this mode. Bearing failure occurs in the material immediately adjacent to the contacting bolt surface due to primarily compressive stresses and leading to a non linear behaviour of the composite plates [7].

The joint bearing strength depends on different parameters, such as: joint configuration, bolt torque, laminate and bolt materials, laminate lay up, and temperature. The level of torque directly influences on the stress fields in both the bolt and the plates. An increment in the tightening torque has two important effects on the joint performance. The positive effect is the increment of friction forces that lead to increasing bearing strength. As was demonstrated in [14,16] for carbon/epoxy laminates, bearing strength grows when the clamping pressure is increased. On the other hand, the negative effect is that out of plane stresses can lead to a premature failure of the joint [17,18]. In consequence, the maximum value of torque is limited by standards.

Moreover, the effect of tightening torque and the through thickness stress distribution are affected by the secondary bending phenomenon. The eccentric load path in single shear lap joints adds the issue of lateral deflection (or secondary bending) of the joint, which generates a non uniform contact pressure between the fasteners and the hole edge. A stress singularity is also introduced when the bolt is tilted in its hole as the surface contact changes into a line contact [19]. The analyses of the stress field in single lap bolted joints have shown that secondary bending produce non uniform stress distributions through the thickness of composite laminates in the vicinity of the bolt hole [5,20].
The influence of torque and secondary bending on bearing strength has been investigated by several researchers by means of experimental studies, see for example [6,8]. However, due to the large range of different matrices, fibres and lay ups available to the designer, the use of purely empirical design procedures would be prohibitively expensive. It is important that all the aspects of joint design are well understood, the development of theoretical reliable models is required to optimise the prediction of bearing strength considering the effect of torque and secondary bending phenomenon.

The most accurate and general models to predict the onset of damage and ultimate failure of composite structures are based on the implementation of constitutive models developed in the context of continuum damage mechanics in finite element (FE) models. The development of a reliable FE model to predict bearing failure of bolted composite joint requires the implementation of failure criteria, the consideration of non linear stress strain relationship and a degradation procedure to reproduce the damage on the material.

For the sake of simplicity several authors have analysed pin loaded composite plates where tightening torque and secondary bending can be neglected. The most commonly used failure criteria to predict pin joints failure are those based on Chang Chang [21] and Chang Lessard [22] formulations that consider only in plane stresses. Several studies has demonstrated that non linear shear stress strain relationship must be considered to predict pin joints bearing strength [23-26].

Although 2D failure criteria can be applied to pin joint, the bolted joint problem is clearly 3D in nature [3]. Effects such as bolt clamp up and secondary bending are best accounted for by 3D models, while the bearing mode of failure is a 3D phenomenon, involving through thickness cracks and delaminations [2].

Failure criteria that consider out of plane stresses as Hashin [27] have been applied to predict bearing failure in double lap [4,9] and bolted single lap joints [28,29]. These studies have proved the influence of out of plane stresses on bearing strength, however there is a lack of studies that consider both out of plane stresses and non linear shear stress strain relationship. The main goal of this work is the implementation of a new set of failure criteria to predict bearing strength of bolted single lap composite joints. The proposed set of failure criteria is an extension of Chang Chang [21] and Chang Lessard [22] criteria including the effect of out of plane stresses.

The accuracy of failure criteria was validated through comparison with experimental data found in literature [13]. To analyse the influence of non linear shear stress strain relationship in the pre diction of bearing failure, the results were also compared with those obtained by Riccio using 3D Hashin failure criteria [29].

### 2. Failure criteria

Chang Lessard criteria were performed to predict damage in laminated composites subjected to compressive loading. The purpose of the authors was the prediction of the in plane response of the laminates from initial loading to final collapse. Since in bolted single lap composite joints composite laminates are subjected to out of plane stresses due to tightening torque and secondary bending effect, the proposed failure criteria includes the effect of both normal and shear out of plane stresses.

It is well known that the in plane shear deformation of composite plies exhibits non linear behaviour without causing damage. Hahn and Tsai [30] formulated the following non linear shear stress strain relationship using high order elasticity theory:

\[ \gamma_{12} = \frac{1}{G_{12}} (\tau_{12} + x\tau_{12}^2) \]  

where \( G_{12} \), \( \tau_{12} \), and \( x \) are, respectively, the in plane shear modulus, shear stress, and shear strain. \( x \) is a constant parameter which is determined experimentally.

Due to the planar structure of composite laminates, the non linear response is difficult to measure under out of plane out of plane stresses. However, since non linear response of composite is mainly dominated by matrix behaviour, the same assumption can be adopted for out of plane shear deformations:

\[ \gamma_{13} = \frac{1}{G_{13}} (\tau_{13} + x\tau_{13}^2) \]  

\[ \gamma_{23} = \frac{1}{G_{23}} (\tau_{23} + x\tau_{23}^2) \]

where \( G_{13} \) and \( G_{23} \) are the shear moduli, \( \tau_{13} \) and \( \tau_{23} \) the shear stresses, and \( \gamma_{13} \) and \( \gamma_{23} \) the shear strains.

Chang Lessard criteria consider four failure modes: matrix crushing, matrix cracking, fibre matrix shear failure, and fibre failure. The proposed extension of Chang Lessard criteria consists in the inclusion of out of plane shear stresses in the formulations of these four failure criteria, and the consideration of two new failure modes: out of plane matrix crushing and delamination.

#### 2.1. Matrix crushing

Chang Lessard criteria consider matrix crushing failure (\( \sigma_m < 0 \)) due to compressive transverse stress and in plane stress, Eq. (4).

The present failure criterion includes the contribution of out of plane shear stress, Eq. (5).

\[ \frac{\sigma_2}{Y_C} = 1 + \frac{\tau_{12}d_{12}}{Y_{12}} + \frac{\tau_{13}d_{13}}{Y_{13}} + \frac{\tau_{23}d_{23}}{Y_{23}} - 1 \]  

\[ \frac{\sigma_2}{Y_C} = 1 + \frac{\tau_{12}d_{12}}{Y_{12}} + \frac{\tau_{23}d_{23}}{Y_{23}} - 1 \]  

\[ \frac{\sigma_2}{Y_C} = 1 + \frac{\tau_{13}d_{13}}{Y_{13}} + \frac{\tau_{23}d_{23}}{Y_{23}} - 1 \]  

where \( \sigma_m \) is the normal stress in transverse direction, \( Y_C \) is the trans verse compressive strength, and \( \gamma_{12} \) and \( \gamma_{23} \) are the ultimate shear strains.

In any of the elements, when the criterion is satisfied (\( e_m = 1 \)) the composite fails by matrix crushing. By introducing the shear stress strain relationships, Eqs. (1) and (3), into Eq. (5), matrix crushing failure criterion yields:

\[ \frac{\sigma_2}{Y_C} = 1 + \frac{\tau_{12}}{S_{12}} + \frac{\tau_{23}}{S_{23}} - 1 \]  

\[ \frac{\sigma_2}{Y_C} = 1 + \frac{\tau_{13}}{S_{13}} + \frac{\tau_{23}}{S_{23}} - 1 \]  

\[ \frac{\sigma_2}{Y_C} = 1 + \frac{\tau_{12}}{S_{12}} + \frac{\tau_{23}}{S_{23}} - 1 \]  

where \( S_{12} \) and \( S_{23} \) are the in plane and out of plane shear strengths.

For composites with linear elastic behaviour (\( x = 0 \)) it should be notice that Eq. (6) can be reduced to:

\[ \frac{\sigma_2}{Y_C} = 1 + \frac{\tau_{12}}{S_{12}} + \frac{\tau_{23}}{S_{23}} - 1 \]  

Additionally, a matrix crushing failure criterion is added to consider out of plane compressive normal stresses (\( \sigma_2 < 0 \)), Eq. (8).

This failure criterion can take into account the damage produced by tightening torque.

\[ \frac{\sigma_3}{S_{13}} = 1 + \frac{\tau_{12}}{S_{12}} + \frac{\tau_{23}}{S_{23}} - 1 \]  

where \( \sigma_3 \) is the out of plane normal stress, \( Z_s \) is the out of plane compressive strength and \( S_{13} \) is the out of plane shear strength. For linear elastic composites (\( x = 0 \)) Eq. (8) can be reduced to:
\[
\left(\frac{\sigma_1}{X_C}\right)^2 + \left(\frac{\tau_{12}}{X_T}\right)^2 + \left(\frac{\tau_{13}}{X_T}\right)^2 + \left(\frac{\tau_{23}}{X_T}\right)^2 e_{\text{mc3}}^2
\]  

(9)

2.2. Matrix cracking

The Chang Lessard criterion for in plane tensile matrix cracking failure \((\sigma_2 > 0)\) considers normal transverse stress and in plane shear stress. In the present failure criterion the contribution of out of plane shear stress is also considered, Eq. (10).

\[
\left(\frac{\sigma_2}{Y_T}\right)^2 + \frac{\tau_{12}^2}{Z_T^2} + \frac{\tau_{13}^2}{Z_T^2} + \frac{\tau_{23}^2}{Z_T^2} e_{\text{mc3}}^2
\]  

(10)

where \(Y_T\) is the transverse tensile strength.

When the criterion is satisfied \((e_{\text{mc3}} > 1)\) the composite fails by matrix cracking. By introducing the shear stress-strain relationships, Eqs. (1) and (3), into Eq. (10), matrix cracking failure criterion yields:

\[
\left(\frac{\sigma_2}{Y_T}\right)^2 + \left(\frac{\tau_{12}}{Z_T}\right)^2 + \left(\frac{\tau_{13}}{Z_T}\right)^2 + \left(\frac{\tau_{23}}{Z_T}\right)^2 e_{\text{mc3}}^2
\]  

(11)

For linear elastic composites \((\sigma = 0)\) Eq. (11) can be reduced to:

\[
\left(\frac{\sigma_2}{Y_T}\right)^2 + \left(\frac{\tau_{12}}{Z_T}\right)^2 + \left(\frac{\tau_{13}}{Z_T}\right)^2 e_{\text{mc3}}^2
\]  

(12)

Additionally, a matrix cracking failure criterion is added to consider out of plane tensile normal stresses \((\sigma_2 > 0)\), Eq. (13). This failure criterion can be used to predict delamination onset,

\[
\left(\frac{\sigma_2}{Y_T}\right)^2 + \frac{\tau_{12}^2}{Z_T^2} + \frac{\tau_{13}^2}{Z_T^2} + \frac{\tau_{23}^2}{Z_T^2} e_{\text{mc3}}^2
\]  

(13)

where \(Z_T\) is the out of plane tensile strength. For linear elastic composites \((\sigma = 0)\) Eq. (13) can be reduced to:

\[
\left(\frac{\sigma_2}{Y_T}\right)^2 + \left(\frac{\tau_{12}}{Z_T}\right)^2 + \left(\frac{\tau_{13}}{Z_T}\right)^2 e_{\text{mc3}}^2
\]  

(14)

2.3. Fibre matrix shearing failure

For predicting fibre matrix shearing failure \((\sigma_1 < 0)\), Chang Lessard criterion considers the effect of normal stress in fibre direction and in plane shear stress. The present failure criterion includes the contribution of out of plane shear stresses, Eq. (15).

\[
\left(\frac{\sigma_1}{X_C}\right)^2 + \frac{\tau_{12}^2}{Z_T^2} + \frac{\tau_{13}^2}{Z_T^2} + \frac{\tau_{23}^2}{Z_T^2} e_{\text{mc3}}^2
\]  

(15)

where \(\sigma_1\) is the normal stress in fibre direction and \(X_C\) the fibre compressive strength.

By introducing the shear stress-strain relationships, Eqs. (1) and (2), into Eq. (15), the shear fibre matrix failure criterion yields:

\[
\left(\frac{\sigma_1}{X_C}\right)^2 + \left(\frac{\tau_{12}}{Z_T}\right)^2 + \left(\frac{\tau_{13}}{Z_T}\right)^2 e_{\text{mc3}}^2
\]  

(16)

Once again, for composites with linear elastic behaviour \((\sigma = 0)\) Eq. (16) can be reduced to:

\[
\left(\frac{\sigma_1}{X_C}\right)^2 + \left(\frac{\tau_{12}}{Z_T}\right)^2 + \left(\frac{\tau_{13}}{Z_T}\right)^2 e_{\text{mc3}}^2
\]  

(17)

2.4. Fibre failure

Chang Lessard fibre failure criterion considers only compressive loads, thus it is based on the fibre buckling strength, Eq. (18). To consider the possibility of tensile loads, the present model includes a tensile fibre failure criterion based on Chang Lessard failure criteria, Eq. (19).

\[
\left(\frac{\sigma_1}{X_C}\right)^2 + \left(\frac{\tau_{12}}{Z_T}\right)^2 + \left(\frac{\tau_{13}}{Z_T}\right)^2 + \left(\frac{\tau_{23}}{Z_T}\right)^2 e_{\text{mc3}}^2
\]  

(18)

\[
\left(\frac{\sigma_1}{X_C}\right)^2 + \frac{\tau_{12}^2}{Z_T^2} + \frac{\tau_{13}^2}{Z_T^2} + \frac{\tau_{23}^2}{Z_T^2} e_{\text{mc3}}^2
\]  

(19)

where \(X_T\) the fibre tensile strength.

By introducing the shear stress strain relationships, Eqs. (1) and (2), into Eq. (19), the tensile fibre failure criterion yields:

\[
\left(\frac{\sigma_1}{X_C}\right)^2 + \left(\frac{\tau_{12}}{Z_T}\right)^2 + \left(\frac{\tau_{13}}{Z_T}\right)^2 e_{\text{mc3}}^2
\]  

(20)

For composites with linear elastic behaviour \((\sigma = 0)\) Eq. (20) can be reduced to:

\[
\left(\frac{\sigma_1}{X_C}\right)^2 + \left(\frac{\tau_{12}}{Z_T}\right)^2 + \left(\frac{\tau_{13}}{Z_T}\right)^2 e_{\text{mc3}}^2
\]  

(21)

3. Numerical model

A FE numerical model reproducing a bolted single lap joint according to [13] was developed using the ABAQUS/Standard code considering non linear stress calculation due to large displacements and composite material behaviour. In addition, Riccio developed a FE model of these tests including a progressive damage model based on Hashin failure criteria [29]. Therefore, the results predicted by the present model could be compared with those predicted by a classical 3D failure criteria such as Hashin.

Single lap composite to aluminium joints were manufactured by using carbon epoxy composite HTA 7/6376 and aluminium AA7475 T76 for plates and titanium 6Al14VSTA for bolts and nuts. The mechanical properties of these materials are described in Tables 1 and 2. The composite lay up was [(0/±45)/90]s/s, and the geometrical description of the single lap specimen is given in Fig. 1. Bolt, nut and washer were considered as a titanium single solid, and the relative displacements between bolt and nut were implemented through a bolt load available in Abaqus/Standard.

<table>
<thead>
<tr>
<th>Material Property</th>
<th>HTA 7/6376</th>
<th>AA7475 T76</th>
<th>Titanium 6Al14VSTA</th>
</tr>
</thead>
<tbody>
<tr>
<td>Longitudinal modulus, (E_1) (GPa)</td>
<td>145</td>
<td>10.3</td>
<td>5.3</td>
</tr>
<tr>
<td>Transverse modulus, (E_2) (GPa)</td>
<td>11.1</td>
<td>3.95</td>
<td>0.3</td>
</tr>
<tr>
<td>Transverse modulus, (E_3) (GPa)</td>
<td>5.3</td>
<td>5.27</td>
<td>0.5</td>
</tr>
<tr>
<td>In-plane shear modulus, (G_{12}) (GPa)</td>
<td>5.3</td>
<td>5.27</td>
<td>0.5</td>
</tr>
<tr>
<td>Out-of-plane shear modulus, (G_{13}) (GPa)</td>
<td>5.3</td>
<td>5.27</td>
<td>0.5</td>
</tr>
<tr>
<td>Major Poisson’s ratio, (\nu_{12})</td>
<td>0.3</td>
<td>0.5</td>
<td>0.5</td>
</tr>
<tr>
<td>Through thickness Poisson’s ratio, (\nu_{13})</td>
<td>0.5</td>
<td>0.5</td>
<td>0.5</td>
</tr>
<tr>
<td>Longitudinal tensile strength, (X_L) (MPa)</td>
<td>2250</td>
<td>1600</td>
<td>64</td>
</tr>
<tr>
<td>Longitudinal compressive strength, (X_C) (MPa)</td>
<td>300</td>
<td>290</td>
<td>50</td>
</tr>
<tr>
<td>Transverse tensile strength, (Y_T) (MPa)</td>
<td>120</td>
<td>290</td>
<td>50</td>
</tr>
<tr>
<td>Transverse compressive strength, (Y_C) (MPa)</td>
<td>50</td>
<td>50</td>
<td>50</td>
</tr>
<tr>
<td>Longitudinal tensile strength, (Z_1) (MPa)</td>
<td>50</td>
<td>50</td>
<td>50</td>
</tr>
<tr>
<td>Longitudinal compressive strength, (Z_C) (MPa)</td>
<td>50</td>
<td>50</td>
<td>50</td>
</tr>
<tr>
<td>In-plane shear strength, (S_{12}) (MPa)</td>
<td>50</td>
<td>50</td>
<td>50</td>
</tr>
<tr>
<td>In-plane shear strength, (S_{23}) (MPa)</td>
<td>50</td>
<td>50</td>
<td>50</td>
</tr>
<tr>
<td>Out-of-plane shear strength, (S_{13}) (MPa)</td>
<td>50</td>
<td>50</td>
<td>50</td>
</tr>
</tbody>
</table>

Table 1

Mechanical properties of carbon-epoxy composite HTA 7/6376.
Thus three solids were used in the FE model: composite plate, aluminium plate, and the bolt nut washer solid.

3.1. Contact and boundary conditions

Contact interactions were modelled using surface based contact considering the linear penalty method. Five contact interactions were defined between the three solids; the composite plate was in contact with aluminium plate, bolt head and bolt shank; and aluminium plate was in contact with nut surface and bolt shank.

The effect of pressure on friction coefficient was neglected, and a constant value of friction coefficient equal to 0.114 was implemented. This friction coefficient was obtained from the work of Herrington and Sabbaghian [31] where friction coefficients between composite plates and the metallic components of the joint were analysed. This value has been used also by other researchers [8].

The loading path was divided into two steps. In the first step, the free ends of aluminium and composite plates were clamped and tightening torque was applied as a bolt load. The bolt load was implemented in the FE model introducing a pre tension condition. This pre tensioning is simulated in Abaqus/Standard by adding a “cutting surface” in the bolt and subjecting it to a normal load. By modifying the elements on one side of the surface, Abaqus/Standard can automatically adjust the length of the bolt at the pre tension section to achieve the prescribed amount of pre tension. The relation between the applied torque \( \tau \) and the normal pressure \( p_w \) acting on the laminate under the washer is [32]:

\[
p_w = \frac{\tau}{k \cdot d \cdot \frac{\pi}{4} \cdot \left( \frac{D^2}{4} - \frac{d^2}{4} \right)}
\]

where \( d \) is the bolt diameter, \( k \) is the torque coefficient usually taken as 0.2 [33], and \( D \) is the washer diameter. Thus bolt load can be calculated as:

\[
F_{\text{bolt}} = \frac{\tau}{k \cdot d}
\]

In the second step, the free end of aluminium plate remained clamped, bolt length was fixed simulating the conservation of tightening torque, and the tension load was applied at the free end of composite plate. The load was applied by imposing only a longitudinal displacement, thus plates were free to rotate leading to secondary bending phenomenon.

Convergence problems due to the rigid body motions (related to possible initial no contact conditions) have been solved by introducing elastic springs with a very low stiffness between a fixed point in space and the unconstrained subcomponents of the joint, see Fig. 2.

3.2. Mesh

The aim of the model is to analyse not only the force displacement relationship, but also the failure modes. Thus a mesh refinement process was carried out to assure that results are not dependent upon the elements size. Successive space discretizations were compared varying the element size in the surrounding of the hole from 0.15 mm to 0.5 mm. The characteristic element size in the final mesh was 0.26 mm, enough to provide accurate results without an expensive computational cost. A total of 41,850 eight node brick elements with reduced integration (C3D8R in Abaqus) were employed to model the composite joint, Fig. 3. Composite plate was modelled with 30,720 elements, aluminium plate with 5120 elements, and 6010 elements were used to model the bolt and the nut.

3.3. Material model

The proposed failure criteria were used to predict the failure of composite plate. A progressive damage model was implemented using a USDFLD subroutine in Abaqus/Standard which allows material properties to be a direct function of predefined field variables. Stresses are called into the subroutine at the start of the current increment and used to evaluate failure criteria. Once the failure criteria are met, the field variables are updated and used to reduce the elastic properties according to the corresponding failure mode, Table 3.

When material properties are degraded at a point, the load redistributes to other points, which could then fail themselves. It is therefore necessary to iterate at the same load level when material properties change to determine if other material points undergo failure. The accuracy of the results when using USDFLD depends on the size of the time increment. Thus, in this analysis very small load steps were used. On the other hand, isotropic hardening model was used to model the plastic behaviour of the metallic components.

### Table 2

<table>
<thead>
<tr>
<th>Mechanical properties of metallic components.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Material</td>
</tr>
<tr>
<td>---------</td>
</tr>
<tr>
<td>Aluminium AA7475-T76</td>
</tr>
<tr>
<td>Titanium 6Al14VSTA</td>
</tr>
</tbody>
</table>

![Fig. 1. Geometrical description of the single-lap-joint.](image-url)
4. Results and discussion

4.1. Model validation

The obtained numerical results were compared with the experimental data from literature [13] to validate the proposed failure criteria. Moreover, the numerical predictions were compared with those of Riccio [29] who implemented a 3D progressive damage FE model, based on the Hashin failure criteria. In Fig. 4, the comparison between experimental and numerical load displacement curves are shown. An excellent agreement between numerical prediction and experimental data was found in both stiffness and bearing strength. The proposed failure criteria predicted bearing failure for a load of 11,601 N, similar to the experimental results: 10,860 N and 11,230 N. Moreover, the present model can reproduce the non linearity of the load displacement curve and the progressive failure of the joint.

Riccio progressive damage model showed a non linear load displacement relationship due to the degradation of mechanical properties. However, Hashin failure criteria overestimated the stiffness and the bearing strength of the joint. The proposed failure criteria predicted bearing failure for a load of 11,601 N, similar to the experimental results: 10,860 N and 11,230 N. Moreover, the present model can reproduce the non linearity of the load displacement curve and the progressive failure of the joint.

4.2. Damage mechanisms

In addition, FE model was used to analyse the damage mechanisms that produced the failure of the composite plate. The values of the failure criteria in the surroundings of the hole when bearing failure occurs are plot in Figs. 5 and 6. Fig. 5 shows the top surface of the composite plate in contact with the bolt head, while Fig. 6 shows the bottom surface in contact with the aluminium plate. Matrix failure was mainly produced by compressive stresses thus, for sake of simplicity, only matrix crushing failure criterion is plotted. The through the thickness distribution of the failure criteria reveals that the single lap composite joint is a 3D problem in nature.

The maximum values of fibre failure criterion were located at the lower plies of the laminate. Due to the secondary bending effect, the compressive load exerted by the bolt shank was concentrated on lower plies, thus the through thickness distribution of the fibre failure criterion was non uniform. Moreover, plies oriented in the longitudinal direction presented higher values of fibre failure criterion.

The distribution of the matrix failure criterion in transverse direction was dominated by secondary bending too. The compressive load exerted by the bolt shank was concentrated on the lower plies. On the other hand, the top ply was damaged due to the compressive load exerted by the bolt head. This pressure applied by the bolt head was non uniform due to secondary bending.

The field of the matrix failure criterion in direction 3 revealed the weight of the tightening torque. In the surroundings of the hole, the matrix was damaged due to the compressive load applied by the bolt head. Tightening torque produced matrix crushing in the composite plate and a degradation of the mechanical properties. Thus the consideration of the damage induced by the out of plane...
stresses is required to get an accurate prediction of the progressive bearing failure in bolted single lap composite joints.

4.3. Effect of friction coefficient

A parametric study was carried out to verify the capability of the FE model to reproduce the influence of friction coefficient and tightening torque observed in experimental results [28,15]. Fig. 7 shows the load displacement curves for different friction coefficients. It is well known that an increment in friction coefficient between plates increases the joint strength [28]. The numerical FE model can reproduce this effect observed in experimental tests reported in literature. This effect was mainly observed for small displacements because, once the relative displacements are higher than the clearance between bolt and hole, the slope of the load displacement curve is non dependent on the friction coefficient.

4.4. Effect of torque

Figs. 8 and 9 show the load displacement curves for different torque tightening. In Fig. 8 the friction coefficient is equal to 0.1 and load displacement curves show that, with this low value of friction coefficient, the load necessary to produce a relative displacement between plates is very low. In this case, an increment in the tightening torque does not produce a significant increase in friction forces; on the other hand a high torque can induce matrix crushing in the composite plate. Thus for low values of friction coefficient an increment in the tightening torque cannot be used to increase the joint strength.
Fig. 9 shows the load–displacement curves with friction coefficient equal to 0.5. Influence of tightening torque.

5. Conclusions

A new set of failure criteria is proposed to predict composite failure in bolted joints. The present failure criteria include out of plane shear stresses in the formulations of the four failure criteria proposed by Chang Lessard and the consideration of two new failure modes: out of plane matrix cracking and delamination. The advantages of the present failure criteria with respect to Chang Lessard criteria are the consideration of a 3D stress field and the prediction of out of plane failure modes as delamination. The main advantage with respect to others 3D failure criteria as Hashin is the inclusion of non linear shear stress strain relationship. Hashin criteria overestimated the stiffness and the bearing strength of the joint. The analysis of failure mechanisms showed that secondary bending effect leads to a non uniform through the thickness distribution. Fibre bucking, fibre matrix shearing failure and in plane matrix crushing were located at the lower plies producing a progressive failure of the joint. Out of plane matrix crushing was distributed on the surface under bolt head and produced a degradation of mechanical properties. Therefore the consideration of 3D stress field including out of plane stresses is necessary to predict bearing failure in bolted single lap composite joints.

In addition, a parametric study was carried out to analyse the influence of friction coefficient and tightening torque. The study showed that an increment in friction coefficient between plates leads to an increase in friction forces and joint stiffness. The effect of torque depends on the friction coefficient. For low values of friction coefficient the effect of an increment in tightening torque can be harmful. However, for moderate high values of friction coefficient the joint stiffness can be increased by increasing the tightening torque.

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References


