# "THE HERRERO-VILLAR APPROACH TO CITATION IMPACT"

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## Abstract

This paper focuses on the evaluation of research units in a scientific field in terms of size-independent indicators of citation impact when size is measured by the number of publications. There are well-known procedures in this context that evaluate each research unit based upon a partition of the field citations into a set of ordered categories, and an external weighting system that determines the relative importance of each category. These conventional procedures are seen to share a common additive structure. We introduce here a new ranking procedure –the *HV* procedure, after Herrero & Villar (2013)– and compare it within a common setting to a number of additive evaluation rules currently used in practice. Given a set of ordered categories, the *HV* procedure measures the performance of the different research units in terms of the relative probability of getting a greater citation impact. The *HV* method provides a complete, transitive and cardinal evaluation without recurring to any external weighting scheme. Using a large dataset of publications in 22 scientific fields assigned to 40 countries, we compare the performance of several additive evaluation rules –the Relative Citation Rate, four percentile-based ranking procedures, and two average-based high-impact indicators– and the corresponding *HV* procedures under the same set of ordered categories. Comparisons take into account re-rankings, and differences in the outcome variability measured by the coefficient of variation, the range, and the ratio between the maximum and minimum index values.

# I. INTRODUCTION

In a globalized and highly interconnected world comparative exercises have become more and more frequent in many aspects of life. Research is no exception and there seems to be growing interest in the evaluation of the scientific influence. Citation analysis has become one of the key tools for evaluating the scientific performance of research units (individual authors, research groups, departments, universities, countries, etc.). Citation impact indicators differ depending on the evaluation approach, the motivation, and the way of transforming citations into specific evaluation formulae. In this paper, we contribute to the literature of citation analysis that focuses on the *ranking of research units* by *size-independent measures of citation impact* when size is measured by the number of publications, i.e. measures that take the relative citation frequencies as the basis for the evaluation (see, among many others, Bornmann *et al.*, 2012, Fairclough & Thelwall, 2015, and Glänzel *et al.*, 2014). We propose a new procedure that evaluates the citation impact of a set of research units according to the criterion pioneered in Herrero & Villar (2013) (*HV* in the sequel).

This new evaluation protocol can be thought of as a two-step procedure in which we first define a partition of the range of citations into a series of categories that gather publications of similar merit, and then evaluate the research units' relative citations distributions embedded in these categories. The key informational item to compare research units is, therefore, the shares of the publications into the different categories. The comparison of these distributions is made in terms of the following principle: each research unit will be compared with all others in terms of the probability of getting a greater citation impact. We shall see that this procedure can also be formulated in terms of a series of tournaments in which each research unit is confronted with all others repeatedly.[1]

There are well-established evaluation procedures that also rely on the assessment of the research units' relative citations distributions by categories using different principles. We shall consider here three types of these indicators that will be used as reference for

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[1] The recourse to tournaments as an evaluation procedure has been applied in related contexts, such as the Google Page Rank algorithm to rank web pages (Page *et al.*, 1998, and Altman & Tennenholtz, 2005), as well as the invariant method (Palacios Huerta & Volij, 2004), the Eigenfactor (Bergstrom, 2007, and West *et al.*, 2010), and the recent paper by Kóczy & Nichifor (2013) that have been used to rank scientific journals. The closest contribution to ours is Carayol & Lahatte (2014), which uses the idea of tournaments for ranking research units when citation impact and quantity both matter.

comparison with the *HV* evaluations. The first type is the *Relative Citation Rate, RCR* (Schubert & Braun, 1986, and Vinkler, 1986). The second type, promoted since 2010 by a group of highly qualified professional leaders in scientometrics, corresponds to what Bornmann & Mutz (2011) call the *percentile rank approach*.[2] The third type consists of the FGT family of high-impact indicators, introduced in Albarrán *et al.* (2011a), which are real valued functions defined over the subset of publications with citations above a *critical citation line* (CCL), and whose properties are inherited from a class of economic poverty indicators introduced by Foster, Greer & Thorbecke (1984).[3]

All these evaluation procedures have in common an additive structure, as shown in Section II. That is, the evaluation of the different research units is given by a weighted sum of the relative citations distribution by categories, where the weights measure the importance of each category. They can be described as implementing the following protocol. First, publications are distributed into a set of categories that gather those publications regarded as being of similar merit. Second, each of those categories is given a weight that determines the rate of substitution between the corresponding categories. And third, the evaluation of each research unit is obtained as a weighted sum of its relative frequencies aggregated by categories.

The additive structure of these evaluation procedures is very appealing because it provides a relatively simple construct that is easy to interpret and rather immediate to compute. The main shortcoming of these indicators is that the evaluation turns out to depend critically on the choice of the weights with which we ponder the publications. Quite often there is no good reason to choose a particular weighting system, which makes the evaluation exercise somehow arbitrary because both the evaluation of the individual units and their ranking depend on those weights. The new evaluation approach presented in this paper avoids this inconvenience because no weighting of categories is involved and still provides a complete, transitive and cardinal evaluation.

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[2] See also the Integrated Impact, or the *I3* indicator in Leydesdorff *et al.* (2011), Leydesdorff and Bormann (2011), Leydesdorff (2012), Wagner & Leydesdorff (2012), and Rousseau (2012). In their search for standards for applying bibliometric methods in the evaluation of research institutes or individuals, Bornmann & Williams (2013), as well as Bornmann, Marx, and co-authors point to the percentile rank approach as the obvious choice (Bornman & Marx, 2013, 2014, and Bornmann *et al.*, 2008, 2014).

[3] For empirical applications of members of the FGT family, see Albarrán *et al.* (2011b, c), Herranz & Ruiz-Castillo (2012, 2013), and Perianes-Rodriguez & Ruiz-Castillo (2016).

Any comparison between alternative ranking procedures should involve not only their rationale and their properties but also the empirical differences they give rise to in applications. Following this idea, we consider here an empirical analysis based on a dataset indexed by Thomson Scientific, and consisting of 4.4 million articles published in 1998-2003, and the citations they receive during a five-year citation window for each year in that period. Articles are classified into the 20 natural sciences and the two social sciences distinguished by this firm. Using these data, we compare the *HV* ranking procedure and the ranks provided by a group of additive procedures in four scientific fields.[4] We compare ranking procedures both from an ordinal point of view (changes in the ranking) and from a cardinal point of view (differences in the spread of the evaluations, as measured by the coefficient of variation, CV, the range, and the ratio between the maximum and minimum). We study a partition of the world into 39 countries and a residual geographical area.

The remainder of this paper is organized into four Sections and an Appendix. Section II presents a selection of additive ranking procedures. Section III describes the alternative approach for the evaluation of research units in a single field by adapting the ideas in Herrero & Villar (2013) to this context. The empirical Section IV develops a comparison between this new ranking procedure and the selected additive procedures in the following fields: Clinical Medicine, Physics, Engineering, and Economics & Business. These fields have been selected endeavoring to ensure diversity and relevance, while keeping the set of empirical comparisons within reasonable limits. Section V contains discussion. The Appendix includes some examples and descriptive statistics. Also, to facilitate reading of the text, some statistical results are relegated to a Supplementary Material section.

## II. THE ADDITIVE APPROACH TO THE EVALUATION OF CITATION IMPACT

### II.1 Framework

Our reference problem is that of evaluating the citation impact of $U$ research units, indexed by $u = 1, \ldots, U$, in a given research field. In this Section we adopt the simplifying assumption that each publication can be attributed to one and only one research unit (this amounts to assuming no co-authorship between people of different units and a single unit affiliation for each author).

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[4] The study has been made for all 22 fields, obtaining similar results. We here report the results for four fields for the sake of parsimony. All remaining results can be obtained from the authors upon request.

We represent a research unit $u$ by a mapping $q_u : \mathbf{N} = \{0, 1, 2, \dots\} \to \mathbf{N}$, where $q_u(r)$ is the number of publications of research unit $u$ with exactly $r$ citations. Hence, a research unit is represented by its publication record as given by $q_u$. For instance, $q_u(0) = 2$, $q_u(5) = 3$ means that this research unit has two publications with zero citations and three publications with five citations. When there is no publication with $r$ citations we have $q_u(r) = 0$. Note that the total number of publications of unit $u$ is given by $\sum_{r \in N} q_u(r)$. Note also that, in the absence of information on the authors that work in a given institution, the notion of productivity recently defended by Abramo & D'Angelo (2016), as well as the joint ranking of scientists and institutions studied in Boyssou and Marchant (2011), are beyond the scope of this paper.

We shall focus here on those evaluation procedures that are size-independent, that is, those that pay attention to the relative frequencies of citations, rather than the absolute ones.[5] This is the case when evaluation procedures satisfy the property of *replication invariance*: replicating any finite number of times the citations of a research unit does not change its evaluation. Then, we define the ***relative citations distribution*** of unit $u$, $D^u : \mathbf{N} \to \mathbf{R}$, where $\mathbf{R}$ stands for the real numbers, as follows

$$D^u(r) = \frac{1}{\sum_{r \in N} q_u(r)} q_u(r).$$

Similarly, we can represent a scientific field as a mapping $Q : \mathbf{N} \to \mathbf{N}$ with $Q(r) = \sum_{u=1}^{U} q_u(r)$, and the corresponding relative citations distribution, $D : \mathbf{N} \to \mathbf{R}$, as

$$D(r) = \frac{1}{\sum_{r \in N} Q(r)} Q(r).$$

An evaluation problem is thus given by $P = \{D^u\}_{u=1}^{U}$. For any problem $P$, our aim is to rank the different research units in terms of their citations by means of a vector valued evaluation function $F$, with $F(P) \in \mathbf{R}^U$, so that $F_u(P) > F_v(P)$ if and only if unit $u$ is considered as better or precedes unit $v$.

## II.2  The additive approach

Let us present now the family of additive evaluation procedures that constitute one of the standard ways of dealing with the evaluation problem in this scenario. This family can be

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[5] The *h*-index introduced by Hirsh (2005) and its many variants, the scoring rules in Marchant (2009), and all ranking procedures in Carayol & Lahatte (2014) are not size-independent. Therefore, they all lie outside the scope of this paper.

described as a two-step procedure defined over the relative citations distributions. In the first step, we define a set of ordered categories $\Theta = \left\{\theta_g\right\}_{g=1}^{G}$, each of which is given a weight, $\omega_g$, in a monotonous way (a better category has associated with it a higher weight). Each category $\theta_g$ gathers all publications that are regarded as of similar merit for evaluation purposes. Second, the relative citations distribution of each research unit is embedded into these categories, as follows. We denote by $c_g^u = \sum_{r \in \theta_g} D^u(r)$ *the* sum of relative frequencies of all publications within category $\theta_g$. That is, $c_g^u$ is the fraction of papers produced by unit $u$ that belong to category $\theta_g$. We can describe the relative citations distribution of unit $u$ embedded in partition $\Theta$, by an array $D_{\Theta}(u) = (c_1^u, \ldots, c_G^u)$. The evaluation formula adopts the following format, for $u$ = 1, 2, …, $U$:

$$F_u(P) = \sum_g \omega_g^F c_g^u \qquad (1)$$

In this formulation, value judgments are introduced in the configuration of the categories, $\Theta = \left\{\theta_g\right\}_{g=1}^{G}$, and the choice of weights, $\omega_g^F$, in the understanding that the higher the merit the higher the weight. Notice that with the same set of categories, different weights give rise to different evaluation rules.

Among the different evaluation procedures that adopt this format, in this paper we consider three different types often found in the literature: (A) The *Relative Citation Rate*, *RCR*, based on the comparison of mean citations; (B) The percentile evaluation procedure, based on the classification of the field publications according to percentiles (or percentile classes), and some associated weights; (C) The FGT family of high-impact indicators, defined over the subset of publications with citations above a critical citation level *CCL*.

**A. Relative Citation Rate indicator**

Given an evaluation problem $P = \{D(u)\}_{u=1}^{U}$, let $\mu_u$ and $\mu$ denote the mean citation of distributions $D^u$ and $D$, respectively. The *RCR* procedure is a citation ranking in terms of the ratio:

$$RCR(u) = \frac{\mu_u}{\mu}. \qquad (2)$$

This corresponds to a particular specification of (1) with $\Theta$=**N**, and $\omega_g^{RCR} = \frac{g}{\mu}$. Here, as any citation level $r$ receives implicitly a different weight, the associated categories correspond to the distinct values in the field relative citations distribution.

## B. Percentile evaluation procedures

In the percentile approach the set of ordered categories, $\Theta = \left\{ \theta_g \right\}_{g=1}^{G}$, is such that $\theta_g$ consists of publications in a certain percentile or percentile class and the *typical* choice of weights is given by $\omega_g^{\pi} = g$. Note that in this case the weights do not change from problem to problem. The evaluation formula is therefore given by:

$$\pi(u) = \sum_g g c_g^u \tag{3}$$

We now present three traditional examples of percentile procedures.

1. The *C100* procedure, where categories correspond to the 100 percentiles in *C*, and the weights range from 1 to 100 for each percentile in ascending order. Thus, $\omega_g^{C100} = g$, for *g* = 1,…,100.

2. The *NSF6* procedure, adopted in the *Science & Engineering Indicators* of the National Science Foundation of the U.S. (National Science Foundation, 2010; see also Leydesdorff *et al.*, 2011, and Schreiber, 2012). This procedure considers six categories, given by: $\theta_1$ = publications in the interval [1, 50th]; $\theta_2$ = publications in the interval (50th, 75h]; $\theta_3$ = publications in the interval (75th, 90th]; $\theta_4$ = publications in the interval (90th, 95th]; $\theta_5$ = publications in the interval (95th, 99th], and $\theta_6$ = publications in the interval (99th, 100th]. Here, again, $\omega_g^{NSF6} = g$, for *g* = 1,…, 6.

3. The *Top k% dichotomous procedure,* where the reference set is partitioned into two categories, $\theta_1$, the top *k%* most cited publications*,* and $\theta_0$, the rest. In this case, $\omega_g^{Topk} = g$, ranks research groups according to the proportion of papers in $\theta_1$.

Dichotomous procedures rely on the idea that only the upper part of the distribution matters and are used in the influential *Leiden Ranking* for universities and the *SCImago Institutions Ranking*.[6] Specifically, the 2015 version of the Leiden Ranking includes the cases *k%* = 50%, 10%, and 1%, while the SCImago's *Excellence Rate* indicator corresponds to *k%* = 10%.

## C. FGT high-impact indicators

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[6] The *Leiden Ranking* (www.leidenranking.com) is a university ranking compiled by the Centre for Science and Technology Studies, Leiden University, The Netherlands, using the Thomson Reuters bibliographic database Web of Science as the source of the publication and citation data. SCImago is a research group from the *Consejo Superior de Investigaciones Científicas*, the University of Granada, Extremadura, Carlos III (Madrid), and Alcalá de Henares in Spain. The *SCImago Institutions Rankings* (SIR; www.scimagoir.com) is a bibliometric ranking of research institutions based on Elsevier's Scopus database. The web-based evaluation tool *InCites* (Thomson Reuters), http//incites.thomsonreuters.com/, also uses the percentile rank approach.

The dichotomous procedure presented above is a particular instance of those evaluation methods that focus on high impact publications and disregard the rest. The latter can be formulated in terms of a CCL *z*, so that any citation below *z* is considered as irrelevant. Thus, only publications with citations over *z* (high impact publications) are considered as important.

For each *z*, the *FGT family* of evaluation procedures, $H^\beta$ with $\beta \geq 0$, is the family of high-impact indicators introduced in Albarrán *et al.* (2011a). It reads as follows:

$$FGT^\beta(u) = \sum_{r>z} c_r^u \left(\frac{r-z}{z}\right)^\beta. \tag{4}$$

This is an additive rule with $\theta_0$ = publications with citations in the interval [0, *z*], $\theta_1$ = publications with (*z* + 1) citations, …, $\theta_v$ = publications with (*z* + *v*) citations, …, i.e., as many categories as distinct citations above *z*, plus one, the category formed by all citations below *z*.[7] Then, $\omega_0^{FGT\beta} = 0$, and $\omega_g^{FGT\beta} = \left(\frac{g-z}{z}\right)^\beta$ for $g \geq 1$.

Given any CCL *z*, let *k*% be the proportion represented by the high-impact publications in citation distribution *D*. Then, for $\beta = 0$, the first member of the FGT family coincides with the *Top k%* indicator. For $\beta = 1$, the second member of the FGT family is called the *Average of the Normalized citation Gaps* (*ANGz* or *ANG k%*) indicator. Note that, following the terminology used in economic poverty analysis, any *Top k%* indicator only captures the *incidence* of the high-impact aspect of a citation distribution, whereas the *ANG k%* indicator captures both *the incidence and the intensity* of this phenomenon.

## III. THE HV EVALUATION PROCEDURE

### III.1. The evaluation formula

Let $\Theta = \left\{\theta_g\right\}_{g=1}^{G}$ be a given partition of the publications, as in the former section. For any unit *u*, let $D_\Theta(u) = (c_1^u, \ldots, c_G^u)$ stand for the vector of publication shares of unit *u* into the different categories. The basic principle of the *HV* procedure to assess the citation impact of a research unit refers to the probability that a representative publication of that unit is in a higher category than a representative publication of another unit. We shall refer to those probabilities as *domination probabilities*. For any pair of units, *u* and *s*, we thus

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[7] The categories above the CCL can be written as $\theta_v$ = publications with (*int(z)* + *v*) citations, where $int(z)$ is the integer part of *z*, to take into account that the percentile defining the CCL can be in practice a non-integer number.

define the scalar $p_{us} \in [0,1]$ as the probability that a publication in unit $u$ belongs to a higher category than a publication in unit $s$. If categories are ordered in an ascending order, we can easily calculate that probability as follows:

$$p_{us} = c_u^G \left( c_s^{G-1} + ... + c_s^1 \right) + c_u^{G-1} \left( c_s^{G-2} + ... + c_s^1 \right) + ... + c_u^2 c_s^1.$$

Similarly, $p_{su}$ denotes the probability that a publication in unit $s$ belongs to a higher category than a publication in unit $u$. By construction, the probability of two publications belonging to the same category is given by $e_{us} = e_{su} = 1 - p_{us} - p_{su}$.

We now define the *relative advantage* of research unit $u$ with respect to unit $s$, $RA_{us}$, as the ratio between the probability that $u$ dominates $s$ and the sum of the probabilities that $u$ is being dominated by some other unit. That is,

$$RA_{us} = \frac{p_{us}}{\sum_{k \neq u} p_{ku}}.$$

Whenever there are only two groups, $RA_{us} = p_{us}/p_{su}$. The *overall relative advantage* of unit $u$, $RA_u$, can thus be described by a weighted average of the relative advantage of $u$ with respect to all other research units. That is,

$$RA_u = \sum_{s \neq u} \lambda_s RA_{us}.$$

Since the weights in this average reflect the relevance of the different units, it is only natural to require choosing them consistently, that is $\lambda_s = RA_s$. In this way, each unit enters the evaluation of the overall relative advantage of any other unit with its own overall relative advantage. That means that the evaluation of a problem $P$ is given by a vector $v \in R_+$, such that:

$$v_u = \sum_{s \neq u} v_s RA_{us} = \frac{\sum_{s \neq u} v_s p_{us}}{\sum_{k \neq u} p_{ku}}, \quad u, s, k = 1, 2, ..., U. \tag{5}$$

Herrero & Villar (2013) show that such a vector, called the **worth**, always exists, and it is strictly positive and unique (up to normalization) under very general conditions.

Notice that the worth vector has a degree of freedom, so that we can freely normalize its values. The easiest (and most natural way) of comparing the performance of the different units among themselves, and with respect to the field as a whole, is by adding to the problem $P = \{D(u)\}_{u=1}^{U}$ the world field citation distribution $D$ as if the field as a whole were an additional unit, and normalize the worth vector of this problem by making the worth of the whole field equal to one. In this way, we are immediately informed not only about the order of the different units, but also whether a certain unit is above or below the "world's average".

Some relevant features of this evaluation procedure are the following:

1. For any given problem, we obtain a *complete ranking* of the units, as well as a *cardinal evaluation* of their relative performance.

2. Given a problem *P,* a unit $u$ is *irrelevant* whenever it happens that for any other unit, $s \neq u$, $p_{us} = 0$. If a unit is irrelevant, then the corresponding component of the worth vector is zero.

3. The worth *is not an additive rule*. That is, we cannot interpret that the worth provides an evaluation in which each category has associated a weight endogenously determined. As shown in Example 1 in the Appendix, in general it is not possible to express the worth as a weighted sum of the different categories. This is due to the multilateral nature of the comparison between individual units.[8]

4. In the case of only two categories, though, the *rankings provided by the HV k% and the Top k% procedures coincide, even if the corresponding cardinal evaluations will do not*. Indeed, without loss of generality, if we have *U* units so that the proportion of publications in the top *k* percentiles are, respectively, $c_1^1 \geq c_1^2 \geq \cdots \geq c_1^U$, the worth vector of these units is given by

$$v_u = \frac{(1-c_1^U)c_1^u}{c_1^U(1-c_1^u)}, for\ all\ u \neq U;\ v_U = 1, \tag{6}$$

so that $v_1 \geq v_2 \geq \cdots \geq v_U$. Thus, both procedures order the units in the same way. Furthermore, under a common normalization, the *components of the worth vector grow faster* than the values attached to the units by the traditional dichotomous procedure, which in this case are

$$Top_u = \frac{c_1^u}{c_1^U},\ \ for\ u \neq U,\ Top_U = 1.$$

It is also interesting to note that the difference between the worth values and the *Top k%* values vanishes when *k* goes to zero. Example 2 in the Appendix illustrates this fact.

**Remark 1:** *The computation of the worth vector can be directly obtained through a friendly and freely available algorithm, hosted in the website of the Instituto Valenciano de Investigaciones Económicas, Ivie ([http://www.ivie.es/valoracion/index.php](http://www.ivie.es/valoracion/index.php)). The worth can be obtained directly from the matrix of relative frequencies of publications by categories and can be plugged into the algorithm as an excel table, thus saving much time and effort. By*

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[8] Note that the weights that appear endogenously in (5) refer to research units and not to categories.

*default the algorithm normalises the worth vector by making the mean value equal to one and requires ordering categories from best to worst.*

Using the categories presented before for the selected additive rules, we find the following examples of the *HV* evaluation procedures:

1. The *RCR* indicator corresponds to the case in which each point in the support of the field citation distribution is considered as a different category. The corresponding partition in the *HV* procedure will be called the *HV max* procedure.

2. The *HV100* procedure considers the categories corresponding to the 100 percentiles in *D,* as in the *C100* procedure*.*

3. The *HVNSF6 procedure* is the counterpart of the *NSF6* procedure.

4. The *HV k%* procedure is the counterpart of the *Top k%* indicator. As mentioned before, the rankings provided by the *HV k%* and the *Top k%* procedures coincide, even though the corresponding evaluations will not.

5. Finally, given a CCL *z*, we had the *ANG k%* evaluation procedure with the following categories: $\theta_0$ = publications with citations in the interval [0, *z*] or in the bottom (100 − *k*) percentiles, $\theta_1$ = publications with (*z* + 1)} citations, …, $\theta_v$ = publications with (*z* + *v*) citations, …, i.e., as many categories as distinct citations above *z*, plus one, the category formed by all citations below *z*. We call *HV k% min-max* the procedure associated to the corresponding set of categories. In the terminology used in Section II.2.C for the FGT indicators, the *HV k%* procedure only compares the *incidence* of the high-impact aspect of the different citation distributions, whereas the *HV k% min-max* procedure compares both *the incidence and the intensity* of the high-impact phenomenon.

Example 3 in the Appendix illustrates the results of applying some of the procedures described in points 1, 4 and 5 above on a given dataset.

### III.2. The HV procedure as a tournament

The worth can also be regarded as the stationary distribution of a Markov process induced by a comparative evaluation of the performance of the different research units in terms of the following tournament. Start by selecting arbitrarily one research unit, say unit *u*. Then select randomly another unit to compete with unit *u*, say unit *s*. Now pick randomly a publication from each of those units and confront them in terms of the category to which

they belong. If the publication of one of those units belongs to a higher category than the other, then that unit remains in the contest while the other one is dismissed. If both publications belong to the same category, then the one initially chosen (unit *u* in this case) remains in the contest, to be confronted with another unit *s* randomly selected. Two new publications are chosen at random from each of those units and are confronted as before.

By repeating indefinitely this process, we find that the probability that unit *u* remains in the contest is given by:

$$\frac{\sum_{s \neq u}\left(p_{us} + e_{us}\right)}{G-1}.$$

That is, the sum of the probability that unit *u* gets better or equal results than all other units times the probability of being chosen at random. Similarly, the probability of unit *u* being beaten by unit *s* is given by:

$$\frac{p_{su}}{G-1}$$

That is, the probability that unit *s* gets a better outcome than unit *u* times the probability of *s* being chosen.

This protocol defines, therefore, a Markov process whose stochastic matrix is:

$$M = \frac{1}{G-1}\begin{pmatrix} \sum_{s \neq 1}\left(p_{1s} + e_{1s}\right) & p_{12} & \dots & p_{1G} \\ p_{21} & \sum_{s \neq 2}\left(p_{2s} + e_{2s}\right) & \dots & p_{2G} \\ \dots & \dots & \dots & \dots \\ p_{G1} & p_{G2} & \dots & \sum_{s \neq G}\left(p_{Gs} + e_{Gs}\right) \end{pmatrix}.$$

This matrix has a positive dominant eigenvector, which corresponds to a stationary distribution, whose *u*-th component is:

$$v_u = \frac{\sum_{s \neq u} p_{us} v_s}{\sum_{s \neq u} p_{su}}.$$

That is, the corresponding worth. This structure explains why the worth is so well behaved and its computation presents no particular difficulty. We can also immediately deduce the uniqueness (and strict positiveness) of the worth vector when matrix *M* is irreducible. A sufficient condition for that to happen is that $p_{us} > 0$ for all *u*, *s*. That is, when there are no irrelevant units.

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In this context the worth tells us the "number of times" that a research unit beats another (more precisely, the fraction of time that, in the long run, each unit will keep competing in the tournament).[9]

## IV. EMPIRICAL RESULTS

### IV.1. Data

The data considered here refer only to research articles or, simply, articles. We begin with a set of 4,472,332 distinct articles published in the period 1998-2003, as well as the citations they receive using a common, five-year citation window for each year in that period. Each of these articles is assigned by Thomson Reuters to one of 22 broad fields. We consider 38 countries that have published at least 10,000 articles in all sciences in the period 1998-2003, plus Luxembourg, which is included in order to cover the 15 countries in the European Union before the accession in 2004, as well as one residual geographical area for the Rest of the World (RW hereafter). Therefore, the total number of research units is $U = 40$.

Articles are assigned to countries according to the institutional affiliation of their authors on the basis of what had been indicated in the by-line of the publications. So far we have assumed that there is no co-authorship, so that each article belongs to a single research unit. However, international cooperation, namely, the existence of articles written by authors belonging to two or more countries poses a technical difficulty that, as is well known, admits different solutions (Waltman & Van Eck, 2015). In this paper, we follow a multiplicative strategy that extends as much as necessary the citation distributions of the research units in our dataset.[10] In this way we arrive at what we call the *geographical extended count* consisting of 5,452,445 articles, a total which is 21.9% larger than the original 4.5 million articles. The distributions of the number of articles by field in the original

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[9] There is a variant of this procedure, called the *balanced worth* (see Herrero & Villar, 2017), in which the probability of remaining in the tournament is equally split when there is a tie. This cancels the extra prize given here to the stronger units, as those winning more often will still have more time competing. Yet we understand that the premium is interesting in this evaluation context.

[10] Perianes-Rodriguez & Ruiz-Castillo (2015) find that a move from the alternative fractional approach to the multiplicative approach does not cause dramatic differences in co-authorship patterns and citation impact values. Nevertheless, *ceteris paribus*, the gainers with a move from the fractional to the multiplicative approach are characterized by (i) a low co-authorship rate for citation distributions as a whole, but a high co-authorship rate in the upper tail of these distributions; (ii) a low citation impact performance, and (iii) a small number of solo articles.

and the geographically extended count are very similar (for details, see Albarrán *et al.*, 2015).

Columns 1 and 2 in Table A in the Appendix include the distribution of the total number of articles by country. The U.S. publishes 26.7% of the total, while the European Union is responsible for approximately one third. The remaining 23 countries and the RW publish about 40% of the total. As indicated in the Introduction, for the sake of parsimony we only present the data for the following four fields: Clinical Medicine, Physics, Engineering, and Economics & Business. Clinical Medicine is the field with the highest number of published articles; Physics and Engineering represent two of the main fields among the natural sciences with different characteristics, and Economics & Business is the only separately identified field among the social sciences. Consequently, columns 3 to 6 in Table A include the distribution by country of the total number of articles in each of these four fields.

In each field, we study the following ranking procedures introduced in Section II.2 and III.3, namely:

(i)     *RCR* and *HV max*;

(ii)    *C100* and *HV100*;

(iii)   *NSF6* and *HVNSF6*;

(iv)    *Top k%* and *HV k%*;

(v)     *ANG k%* and *HV k% min-max*.

Given a field citation distribution and a percentile $k$, we fix the CCL $z$ so that high-impact articles coincide with those above the $k$-th percentile.

**Remark 2.** *The use of percentiles in practice and the construction of the corresponding categories is well known in the literature and is explained in depth, among others, by Waltman and Schreiber (2013). Here we define the percentile categories using the standard statistical approach used by the Science and Engineering Indicators report of the National Science Board (2012). In this approach, the set of, say, top 10% publications is defined such that it includes at most 10% of the publications in a field.*

**IV.2. Results**

As far as ranking procedures are concerned, in groups (iv) and (v) above we consider the values *k%* = 10%, 1%, so that in each of these two groups there are four procedures. Since groups (i) to (iii) involve two procedures each, there are 14 procedures altogether. Index values and country ranks for the aforementioned 14 procedures, within the four fields, are presented in Tables SM1 and SM2 in the Supplementary Material. Country index values are presented relative to the field value, so that the value one can serve as a benchmark for evaluating research units in the usual way.

Comparing alternative evaluation procedures usually involves two key elements: (1) the extent of re-rankings, and (2) the importance of cardinal differences between those evaluations (see *inter alia* Waltman *et al.*, 2012, and Ruiz-Castillo & Waltman, 2015). As a first approximation, the first aspect might be partially revealed by rank correlation coefficients, and also by the Ulam distance between rankings. As discussed by Gordon (1979), the Ulam distance between rankings can be interpreted as the number of elements (countries in our case) that have to be changed in two ranking vectors in order to have full agreement between them.[11] Consequently, the value of the Ulam distance regarding our evaluation problem lies between 0 and 39. Kendall rank correlation coefficients can be found in Table SM3 in the Supplementary Material, while Ulam distances can be found in Table 1.

**Table 1 around here**

Here we are mostly interested in the following questions:

1. How different are the rankings delivered by the additive procedures and the corresponding *HV* evaluations?

2. How different are the rankings as a function of the number of categories (the fineness of the grid) and their associated scores? We are interested, in particular, in comparing indicators of incidence with indicators of incidence and intensity of the high-impact phenomenon.

We find that Kendall correlation coefficients between the *Top k%* and *HV k%* procedures for *k%* = 10%, 1%, are both equal to one in all fields and that the Ulam distance between them is zero, as it should be, since we have already mentioned that they provide identical rankings.

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[11] In order to compute the Ulam distance, we have used several components from the Fortran 90 library SUBSET by John Burkardt (Florida State University), available at his website https://people.sc.fsu.edu/~jburkardt/f_src/subset/subset.html.

There are some other key comparisons characterized by extremely high Kendall coefficients and low Ulam distances, indicating that, in those cases, there are few re-rankings. For instance, among the indicators that look at the whole distribution (*RCR, HV max, C100* and *HV100*), the last three yield extremely similar rankings. Also, the rankings of the *HV k% min-max* are almost identical to the corresponding *Top k%* and *HV k%.* This implies that, in our data, the additional flexibility provided by an extension of the category set in the upper tail of the field citations distribution in the *HV k% min-max* procedure plays a limited role in ranking the countries.

In general, although the rank correlations are relatively high among all procedures, the Ulam distances often show a substantial number of re-rankings, revealing that the latter distinguishes more finely between procedures than the former. Consider the following three cases. Firstly, when comparing indicators that use several categories across the whole distribution (*RCR, C100, NFS6* and the corresponding *HV* indicators) with indicators that focus on the upper tail (*Top k%, ANG k%* and the corresponding *HV* indicators), Ulam distances go from not much more than 10 up to well above 20. This highlights that focusing on the upper part of the field citations distribution has important implications for the evaluation of countries' performance. Secondly, the large differences in Ulam distances between indicators based on the upper 10% or the upper 1% tail imply again that becoming even more selective with countries' performance gives rise to substantial re-rankings. Thirdly, in spite of the similarity of the rankings generated by additive procedures and *HV* indicators when they are based on the same categories, there are a few exceptions worth noting. In particular, there are important differences between the rankings provided by the *NFS6* and the *HVNFS6* procedures. This indicates that the choice of weights in the case of more than two categories can have important consequences.

Finally, the rankings provided by the *RCR* indicator and the *ANG k%* indicators are also very different from their corresponding *HV* indicators: their Ulam distances are around 20 (often above) for the *RCR* indicator, and well above 20 for the *ANG k%* indicators. Notice also that these indicators have another characteristic in common: they are potentially very sensitive to extreme observations. Therefore, they should be treated with caution.[12]

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[12] The case of *ANG 1%* in the field of Economics is particularly informative. While common wisdom in the profession points to the U.S. as the leading country by far, the U.S. would be third in the ranking according the *ANG 1%* (Table SM3 in the Supplementary Material) below Switzerland (first) and, very surprisingly, Mexico (second). Of course, the small country effect and international collaboration can partly explain this, but these

Next, we move to discuss cardinal differences between the units' index values. For all procedures in the four fields, Table 2 presents measures of outcome ***variability***: the range, the ratio Max/Min, and the coefficient of variation (CV).

**Table 2 around here**

Our discussion focuses on three questions.

1. Do the *HV* procedures exhibit a greater variability than the percentile procedures under the same category set? In other words, do we find that variability is ordered as follows:

    *C100 < HV100*?

    *NSF6 < HVNSF6*?

    *Top 10% < HV10%*?

    *Top 1% < HV 1%*?

Consider first the dichotomous case, i.e. the last two rows. As expected, the answer to this key question is in the affirmative in the four fields (rows 7 and 8, and 11 and 12 in Table 2). Note that, as *k* decreases, the difference in variability between the *HV k%* and *Top k%* procedures becomes negligible, as expected (see Example 2 in the Appendix).

On the other hand, when there are more than two categories, *HV* procedures clearly discriminate more than percentile-based procedures (rows 3 and 4, and 5 and 6 in Table 2).

2. Does the variability increase when we move to procedures based on indicators more and more focused on the upper tail of the citation distribution? In other words, do we find the variability ordered as follows:

    *C100 < NSF6 < Top 10% < Top 1%?*          (7)

    *HV 100 < HVNSF6 < HV 10% < HV 1%?*          (8)

    *ANG 10% < ANG 1%?*          (9)

In the first set of scoring rules (sequence 7), the *C100* and *NSF6* procedures are conceptually very different. We find that, contrary to what one may have expected, the variability of the *C100* procedure is greater than that of the *NSF6* procedure. This is due to the effect of the weighting system, which exhibits a much larger spread in the *C100* case (i.e. a ratio of 100/1 in the first case and a ratio of 6/1 in the second). The contrary happens if we

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two issues also potentially affect other indicators. Actually, Mexico goes up a lot in any ranking focusing on the upper 1% tail. But since those indicators are not so extremely sensitive to extreme observations, they deliver more sensible rankings.

compare the *C100* and the *Top 10%* (and the *Top 1%*) procedures in all fields. The increase in the variability, jointly with the relatively low rank correlation and the high Ulam distances discussed before, clearly confirms the existence of differences in this sequence (rows 3, 7, and 11 in Tables 1 and 2).

In the *HV* case (sequence 8), we reach a different result in all fields. Although the *HV100* and the *HVNSF6* rankings are rather similar, the *HVNSF6* procedure has a greater variability than the *HV100* procedure. Thus, sequence 8 is clearly established (rows 4, 6, 8, and 12 in Table 2). Finally, as far as sequence 9 is concerned, the variability also increases as we move towards the very upper tail of citation distributions in all fields (rows 10 and 14 in Table 2).

3. Do the incidence indicators have a smaller variability than the indicators capturing both the incidence and the intensity of the high-impact phenomenon? In other words, do we find that the variability is ordered as follows:

> *Top 10% < ANG 10%?*
>
> *Top 1% < ANG 1%?*
>
> *HV 100 < HV max?*
>
> *HV 10% < HV 10% min max?*
>
> *HV 1% < HV 1% min max*?

We find that the variability is moderately but clearly higher in the *ANG k%* than the *Top k%* indicators. On the contrary, the variability of the *HV100* and *HV max* procedures is indistinguishable (rows 4 and 2 in Table 2), whereas in the two remaining cases the variability of the incidence procedures is even slightly greater than that of the *min-max* alternatives (rows 8 and 9, and 12 and 13 in Table 2). Discriminating between publications with different citations within percentile rank classes in the *HV100*, *HV 10%*, and *HV 1%* procedures has practically no consequences.

## V. DISCUSSION

Based on the ideas presented in Herrero & Villar (2013), in this paper we have introduced a new procedure for the evaluation of research units that can be regarded as an alternative to size-independent additive methods. The *HV* index evaluates the scientific influence of research units in terms of the likelihood of getting publications with higher

citations. The key value judgement is the comparison of any two units in terms of the probability that a random extraction from one of them yields a publication with a higher citation level than one random extraction from the other. The index derives from a consistent application of this notion for the entire set of units participating in the evaluation problem.

A useful way of assessing the interest of a new procedure is to compare it with some relevant alternatives. Here we have selected three types of procedures that also evaluate citations using the relative citations distributions embedded in a set of categories. All those procedures can be described as weighted sums, where the weights correspond to the importance given to each category.

In the previous Section, we have compared from an empirical perspective seven additive procedures representing current practice and the corresponding *HV* alternatives under the same set of categories. Let us now comment from a conceptual viewpoint on the main features that additive and *HV* procedures have in common, and the key aspects that separate them.

All procedures rely on a previous decision –expressing our value judgements–, about the assignment of publications into categories in such a manner that each category includes all publications considered to have the same citation merit. As all publications within a category are indistinguishable, the more generic the category is, the less attention we pay to individual differences (and vice-versa). Our view on how many categories to distinguish and how inclusive they are decisively conditions the evaluation exercise. Changes in the definition of categories affect relative citations frequencies, and hence the final result.

Once the categories have been established, additive procedures and the *HV* evaluation follow different paths. Additive procedures attach a weight to each category, which expresses how important it is, and then obtain the evaluation as a weighted sum of the shares of citations into the different categories. Consequently, once the categories have been defined, the weights fully determine the evaluation. The problem with this approach is that the choice of weights can be rather arbitrary, in which case the same applies to the whole evaluation. To see this, notice that changing the weights of any additive procedure may substantially alter the evaluation (e.g., by continuity, any of the rules in the percentile approach can be approximated arbitrarily from the *C100* by conveniently adjusting the weights).

The *HV* index does not require any external weighting system. Using a different evaluation approach it provides a *relative assessment* of the different research units in terms of the likelihood of getting publications with higher citations (relative here in the sense that the value attached to each unit depends on all the units with which it is compared). The multilateral nature of these comparisons and the evaluation principle lead to a cardinal, complete and transitive ranking, as it is the case in the additive approach.

From the above discussion it follows that the valuation of a unit in the additive methods is independent of the valuation of any other unit, whereas the valuation of a unit by the *HV* method depends on all other units. This type of structural difference appears in different evaluation exercises. Think, for instance, of the way of ranking athletes in a decathlon competition at the Olympic Games, and the way of ordering soccer teams in the European national leagues. In the first case, each of the disciplines is graded separately and the athletes' scores depend on their individual performance. Overall individual scores are obtained by adding up the outcomes of the different disciplines, and the athletes are ordered according to the aggregate outcome. But if a certain athlete disappears from the competition, the score of the remaining athletes does not vary. In the soccer leagues all teams in the same division compete twice with each other and the final ranking takes into account the results of all pairwise matches. The evaluation of a team *vis-a-vis* another depends upon their performance against all the competitors, and upon the competitors' performance. Because of that, if after the league ends a certain team is eliminated for some external reason, the ranking of the remaining teams may vary.

Indeed, the *HV* method solves the evaluation of all research units *simultaneously* instead of unit by unit. One may argue that this makes the evaluation less transparent and harder to compute. This is not the case. On the one hand, the evaluation turns out to be obtained as the dominant eigenvector of a suitable stochastic matrix, so that the solution is well defined and conceptually well grounded. On the other hand, there is a free online algorithm that immediately solves the problem. This algorithm allows interested parties to perform a sensitivity analysis regarding alternative specifications of the categories at no cost.

It might be tempting to think of the *HV* method as providing an endogenous way of attaching weights to the different categories or citations levels, so that the result is actually a

blurred weighted average. This is not the case. Example 1 in the Appendix shows that it might be impossible to recover the *HV* evaluation as a weighted sum.

Let us point out that there is no best ranking procedure for the evaluation of citation impact (for recent discussions, see Boyssou and Marchant, 2014, and Waltman, 2016). Different ways of selecting categories reflect different conceptions of the relevance of citations. Once this has been established, the key question is whether there is a rationale for the choice of weights, or at least a general agreement on why those weights are the proper rates of substitution between categories. When this is the case, additive procedures provide simple and transparent formulae to make the evaluation. Yet many disagreements concerning the ranking of institutions derive, precisely, from the different visions about how publications in different percentiles should be pondered. When there are insufficient reasons to choose a particular weighting system, or when people disagree about the choice of weights, the *HV* method provides a sound alternative that avoids having to decide on how to ponder different categories.

Note that the skewness of citation distributions in all sciences has recently led practitioners towards methods that focus on the upper tail of such distributions. We have confirmed that this focus leads to substantial changes in the evaluation of 40 countries. Yet, what the CCL or the *k%* should be in order to represent excellence in citation impact is not obvious at all. In this situation, the Leiden Ranking has temporarily found an interesting solution: compute *Top k%* indicators for *k% = 10%* and *1%*. One may well consider reasonable to define three categories consisting of the bottom 90 percentiles, the next nine percentiles, and the top last percentile.[13] In this case and, generally, whenever a user believes that based on fundamental value judgments it is best to have more than two categories, we may conclude that the *HV* procedure is a good choice without any *a priori* weighting scheme.

Finally, we address three possible directions for further research. Firstly, we have studied a large dataset but a relatively small number of research units. Before we can give full credit to our empirical conclusions, we must experiment with other large datasets and a

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[13] Another interesting example leading to three categories is Rodriguez-Navarro (2011) who looks for an indicator defined on the very upper tail of citation distributions capable of predicting the number of Nobel Prizes in Chemistry, Physics, and Physiology/Medicine. This author proposes a scoring rule with three categories of percentiles, namely, [0, 99), [99, 99.9) and [99.9, 100] for which, using regression analysis, he suggests weights 0, 1 and 15, respectively.

more extensive list of research units. Secondly, we know that additive indicators might be dominated by a few highly cited publications.[14] Instead, percentiles or percentile rank classes are scarcely affected by extreme observations (see *inter alia* Bornmann and Marx, 2013). It should be noted that *HV* ranking procedures would behave as the corresponding percentile based indicators in this respect. In any case, the robustness of indicators to extreme observations is an empirical matter beyond the scope of this paper. Last, but not least, in this paper we have limited ourselves to the analysis of fields in isolation. The theoretical problem of aggregating fields to provide a joint evaluation of research units (countries) is solved in the case of additive rules, but is still an open question in the case of *HV* indicators. This is also left for further research.

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[14] The case of the University of Göttingen, which was ranked second in the 2011/2012 edition of the Leiden Ranking according to the *MNCS* indicator on the strength of a single highly cited publication, is cited as a good example of this problem (Waltman *et al.*, 2012). For the influence of extreme observations see *inter alia* Li & Ruiz-Castillo (2014).

**APPENDIX**

***Example 1.*** Let us consider three units, each with 18 papers, and three categories. The first unit has 9 papers in category 1 and 9 papers in category 3; Unit 2 has all the papers in category 2, and unit 3 has 6 papers in each category. According to the HV procedure, the three units have the same value (the reason is that, in this example, $p_{ij} = p_{ji}$ for all $i, j = 1, 2, 3$). Thus, if we weight the categories with scores 0, $\alpha, \beta$ we obtain that $\beta = 2\alpha$. Now, take another problem in which again we have three units $a$, $b$, and $c$, and the same three categories as before. The three units have ten papers each. Unit $a$ has five papers in category 1 and five papers in category 3, unit $b$ has 3 papers in category 1 and seven papers in category 2, and unit $c$ has ten papers in category 2. According to the *HV* evaluation, unit $c$ goes first, the next is unit $a$, and the last is unit $b$. But for this to happen with the scores previously obtained, $2\alpha > \beta$, contradicting the previous finding.

***Example 2.*** Consider three units so that for *k = 10%,* present the following distributions:

$$D^1_{10\%} = (0.5, 0.5); \; D^2_{10\%} = (0.9, 0.1); \; D^3_{10\%} = (0.99, 0.001).$$

And for *k=1%,* the citation distributions are as follows:

$$D^1_{1\%} = (0.95, 0.05); \; D^2_{1\%} = (0.99, 0.01); \; D^3_{1\%} = (0.999, 0.001)$$

In both cases, the values of the *Top k%* relative to the third unit are $d_1 = 50; \; d_2 = 10; \; d_3 = 1$. Nonetheless, the *HV* values are as follows:

$$v_1^{10\%} = \frac{0.99}{0.5}50; \; v_2^{10\%} = \frac{0.99}{0.9}10; \; v_3^{10\%} = 1$$

$$v_1^{1\%} = \frac{0.999}{0.95}50; \; v_2^{1\%} = \frac{0.999}{0.99}10; \; v_3^{10\%} = 1.$$

***Example 3.*** Suppose that a field citation distribution is given by

$$Q(1) = Q(3) = Q(4) = Q(5) = Q(14) = Q(15) = Q(20) = Q(25) = Q(40) = Q(50) = Q(100) = 1;$$
$$Q(2) = Q(6) = Q(7) = Q(8) = 2;$$
$$Q(0) = 4,$$
$$Q(r) = 0 \text{ otherwise.}$$

Next, consider the dichotomous case for *k = 25%* with the following two categories:

$$\theta_1 = \{0, 1, 2, 3, 4, 5, 6, 7, 8, 14, 15\};$$
$$\theta_2 = \{20, 25, 40, 45, 50, 100\}.$$

Assume that there are three units (*1, 2, 3*), with the following citations distributions

$$q^1(4) = q^1(6) = q^1(8) = q^1(15) = q^1(20) = q^1(40) = q^1(50) = 1;$$
$$q^2(0) = 2, q^2(2) = q^2(6) = q^2(7) = q^2(14) = q^2(45) = q^2(50) = 1;$$
$$q^3(0) = 2, q^3(1) = q^3(2) = q^3(3) = q^3(5) = q^3(8) = q^3(100) = 1;$$
$$q^j(r) = 0 \text{ otherwise}, j = 1, 2, 3.$$

Panel A in the following table reports the index values (relative to the field index value) for six indicators, grouped in three pairs consisting of one additive rule and the corresponding *HV* indicator. In particular, we report the *Top 25%* and the *HV 25%* (columns 1 and 2), the *RCR* and the *HV max* (columns 3 and 4), and finally

the *ANG 25%* and the *HV 25% min-max* (columns 5 and 6).[15] As indicated in the Introduction, we measure the dispersion of the different procedures by means of three statistics: the range, the ratio Max/Min, and the CV. The results are in Panel B of the following table.

| | Top 25% | HV 25% | RCR | HV max | ANG 25% | HV 25% min-max |
|---|---|---|---|---|---|---|
| | (1) | (2) | (3) | (4) | (5) | (6) |
| **A. Index values** | | | | | | |
| **Unit 1** | 1.50 | 1.80 | 1.02 | 1.87 | 0.60 | 1.33 |
| **Unit 2** | 1.00 | 1.00 | 1.01 | 0.99 | 1.03 | 1.12 |
| **Unit 3** | 0.50 | 0.43 | 0.97 | 0.53 | 1.38 | 0.56 |
| | | | | | | |
| **B. Variability** | | | | | | |
| **Range** | 1.00 | 1.40 | 0.05 | 1.34 | 0.78 | 0.77 |
| **Max/Min** | 3.00 | 4.19 | 1.05 | 3.55 | 2.31 | 2.40 |
| **CV** | 0.50 | 0.64 | 0.03 | 0.60 | 0.39 | 0.40 |

Some comments are in order. Firstly, as we know, the ranking corresponding to the *Top 25%* and the *HV 25%* procedures is the same, but the dispersion of the index values is different. Secondly, we observe that, as expected, the dispersion of the *HV 25%* procedure is greater than that of the *Top 25%* procedure. Finally, let us mention the following interesting observation. Some might believe that for any *z* the corresponding *ANG k%* indicator always has a greater dispersion than the *Top k%* indicator. However, this example provides a counter-example to this conjecture. The reason is that the assignment of the most cited publication to unit *3* offsets the greater share of excellent publications enjoyed by unit 1. This generates a complete re-ranking of the units. The same phenomenon is even more pronounced for *HV* procedures.

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[15] The 75th percentile value turns out to be *z* = 16.25.

**Table A. Distribution of the number of articles by country in the all-sciences case, Clinical Medicine, Physics, Engineering, and Economics & Business**

| Ranking according to (1) | | Total number of articles (1) | % (2) | Percentage of articles in: | | | |
|---|---|---|---|---|---|---|---|
| | | | | Clinical Medicine (3) | Physics (4) | Engineering (5) | Economics & Business (6) |
| 31 | ARGENTINA | 25,939 | 0.5 | 0.3 | 0.5 | 0.2 | 0.2 |
| 12 | AUSTRALIA | 126,072 | 2.3 | 2.4 | 1.2 | 2 | 3.3 |
| 25 | AUSTRIA | 43,009 | 0.8 | 1.2 | 0.8 | 0.6 | 0.6 |
| 21 | BELGIUM | 60,038 | 1.1 | 1.3 | 1 | 1 | 1.3 |
| 18 | BRAZIL | 66,556 | 1.2 | 0.9 | 1.7 | 1 | 0.3 |
| 8 | CANADA | 195,938 | 3.6 | 3.6 | 1.9 | 3.6 | 5 |
| 7 | CHINA | 197,462 | 3.6 | 1.3 | 5.6 | 5.3 | 1.8 |
| 30 | CZECH REPUBLIC | 26,542 | 0.5 | 0.2 | 0.7 | 0.4 | 0.7 |
| 23 | DENMARK | 45,908 | 0.8 | 1 | 0.7 | 0.5 | 0.9 |
| 24 | FINLAND | 43,769 | 0.8 | 1.1 | 0.6 | 0.7 | 0.7 |
| 5 | FRANCE | 282,729 | 5.2 | 5.1 | 6.3 | 4.4 | 3.2 |
| 4 | GERMANY | 390,873 | 7.2 | 7.8 | 9 | 5.8 | 3.6 |
| 27 | GREECE | 30,917 | 0.6 | 0.7 | 0.6 | 0.9 | 0.5 |
| 34 | HUNGARY | 24,398 | 0.4 | 0.3 | 0.5 | 0.4 | 0.1 |
| 14 | INDIA | 107,025 | 2 | 0.8 | 2.2 | 2.3 | 0.5 |
| 39 | IRAN | 9,717 | 0.2 | 0.1 | 0.2 | 0.3 | 0 |
| 38 | IRELAND | 16,005 | 0.3 | 0.3 | 0.2 | 0.3 | 0.4 |
| 22 | ISRAEL | 55,837 | 1 | 1.2 | 1.2 | 0.9 | 1.2 |
| 9 | ITALY | 190,078 | 3.5 | 4.1 | 4.1 | 3.7 | 1.9 |
| 2 | JAPAN | 431,828 | 7.9 | 8.3 | 10.1 | 8.6 | 1.5 |
| 40 | LUXEMBOURG | 584 | 0 | 0 | 0 | 0 | 0 |
| 28 | MEXICO | 29,858 | 0.5 | 0.3 | 0.8 | 0.5 | 0.2 |
| 13 | NETHERLANDS | 111,959 | 2.1 | 2.7 | 1.5 | 1.6 | 3.1 |
| 32 | NEW ZEALAND | 25,437 | 0.5 | 0.4 | 0.2 | 0.3 | 0.7 |
| 29 | NORWAY | 29,511 | 0.5 | 0.7 | 0.3 | 0.4 | 0.8 |
| 20 | POLAND | 61,172 | 1.1 | 0.4 | 2.1 | 1.1 | 0.2 |
| 37 | PORTUGAL | 20,173 | 0.4 | 0.2 | 0.4 | 0.5 | 0.3 |
| 6 | RW | 216,949 | 4 | 3.2 | 4 | 4.5 | 2.1 |
| 10 | RUSSIA | 157,349 | 2.9 | 0.6 | 7.2 | 3.4 | 0.3 |
| 35 | SINGAPORE | 22,834 | 0.4 | 0.3 | 0.5 | 1.3 | 0.6 |
| 36 | SOUTH AFRICA | 21,994 | 0.4 | 0.4 | 0.2 | 0.3 | 0.4 |
| 16 | SOUTH KOREA | 89,445 | 1.6 | 0.9 | 2.4 | 2.9 | 0.8 |
| 11 | SPAIN | 135,317 | 2.5 | 2.3 | 2.3 | 2 | 2 |
| 15 | SWEDEN | 89,902 | 1.6 | 2.2 | 1.3 | 1.2 | 1.5 |
| 17 | SWITZERLAND | 80,669 | 1.5 | 1.7 | 1.8 | 1.2 | 1 |
| 19 | TAIWAN | 62,928 | 1.2 | 1 | 1.3 | 2.8 | 0.8 |
| 26 | TURKEY | 40,018 | 0.7 | 1.3 | 0.4 | 0.9 | 0.4 |
| 3 | UK | 397,488 | 7.3 | 8.5 | 5.3 | 6.8 | 12.2 |
| 33 | UKRAINE | 24,631 | 0.5 | 0 | 1.2 | 0.7 | 0 |
| 1 | UNITED STATES | 1,463,587 | 26.8 | 30.8 | 17.9 | 24.9 | 44.6 |
| | TOTAL | 5,452,445 | 100 | 100 | 100 | 100 | 100 |

Note: Total number of articles in each field: Clinical Medicine = 1,102,367; Physics = 626,304; Engineering = 421,332, and Economics & Business = 75,687

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**Table 1. (Ulam) Distance between rankings according to each procedure.**

**Part A. Clinical Medicine.**

| | RCR | HV max | C100 | HV100 | NSF6 | HVNSF6 | Top 10% | HV 10% | HV10% min-max | ANG 10% | Top 1% | HV 1% | HV1% min-max | ANG 1% |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| | (1) | (2) | (3) | (4) | (5) | (6) | (7) | (8) | (9) | (10) | (11) | (12) | (13) | (14) |
| 1. RCR | 0 | | | | | | | | | | | | | |
| 2. HV max | 17 | 0 | | | | | | | | | | | | |
| 3. C100 | 17 | 3 | 0 | | | | | | | | | | | |
| 4. HV100 | 17 | 0 | 3 | 0 | | | | | | | | | | |
| 5. NSF6 | 13 | 13 | 12 | 13 | 0 | | | | | | | | | |
| 6. HVNSF6 | 17 | 10 | 8 | 10 | 12 | 0 | | | | | | | | |
| 7. Top 10% | 14 | 22 | 22 | 22 | 19 | 20 | 0 | | | | | | | |
| 8. HV10% | 14 | 22 | 22 | 22 | 19 | 20 | 0 | 0 | | | | | | |
| 9. HV10% min-max | 14 | 22 | 22 | 22 | 19 | 20 | 1 | 1 | 0 | | | | | |
| 10. ANG10% | 19 | 22 | 23 | 22 | 22 | 21 | 17 | 17 | 17 | 0 | | | | |
| 11. Top 1% | 22 | 25 | 25 | 25 | 22 | 24 | 21 | 21 | 21 | 15 | 0 | | | |
| 12. HV1% | 22 | 25 | 25 | 25 | 22 | 24 | 21 | 21 | 21 | 15 | 0 | 0 | | |
| 13. HV1% min-max | 22 | 25 | 25 | 25 | 22 | 24 | 21 | 21 | 21 | 15 | 0 | 0 | 0 | |
| 14. ANG1% | 25 | 27 | 27 | 27 | 26 | 24 | 26 | 26 | 25 | 23 | 20 | 20 | 20 | 0 |

**Part B. Economics.**

| | RCR | HV max | C100 | HV100 | NSF6 | HVNSF6 | Top 10% | HV 10% | HV10% min-max | ANG 10% | Top 1% | HV 1% | HV1% min-max | ANG 1% |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| | (1) | (2) | (3) | (4) | (5) | (6) | (7) | (8) | (9) | (10) | (11) | (12) | (13) | (14) |
| 1. RCR | 0 | | | | | | | | | | | | | |
| 2. HV max | 18 | 0 | | | | | | | | | | | | |
| 3. C100 | 18 | 4 | 0 | | | | | | | | | | | |
| 4. HV100 | 18 | 0 | 4 | 0 | | | | | | | | | | |
| 5. NSF6 | 15 | 15 | 14 | 15 | 0 | | | | | | | | | |
| 6. HVNSF6 | 18 | 14 | 12 | 14 | 13 | 0 | | | | | | | | |
| 7. Top 10% | 21 | 22 | 22 | 22 | 22 | 23 | 0 | | | | | | | |
| 8. HV10% | 21 | 22 | 22 | 22 | 22 | 23 | 0 | 0 | | | | | | |
| 9. HV10% min-max | 21 | 21 | 21 | 21 | 22 | 22 | 2 | 2 | 0 | | | | | |
| 10. ANG10% | 22 | 25 | 25 | 25 | 25 | 24 | 23 | 23 | 23 | 0 | | | | |
| 11. Top 1% | 25 | 26 | 26 | 26 | 25 | 27 | 25 | 25 | 25 | 22 | 0 | | | |
| 12. HV1% | 25 | 26 | 26 | 26 | 25 | 27 | 25 | 25 | 25 | 22 | 0 | 0 | | |
| 13. HV1% min-max | 25 | 26 | 26 | 26 | 25 | 27 | 25 | 25 | 25 | 22 | 0 | 0 | 0 | |
| 14. ANG1% | 27 | 28 | 29 | 28 | 27 | 28 | 30 | 30 | 30 | 29 | 16 | 16 | 16 | 0 |

**Part C. Engineering.**

|  | RCR | HV max | C100 | HV100 | NSF6 | HVNSF6 | Top 10% | HV 10% | HV10% min-max | ANG 10% | Top 1% | HV 1% | HV1% min-max | ANG 1% |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
|  | (1) | (2) | (3) | (4) | (5) | (6) | (7) | (8) | (9) | (10) | (11) | (12) | (13) | (14) |
| 1. RCR | 0 |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 2. HV max | 19 | 0 |  |  |  |  |  |  |  |  |  |  |  |  |
| 3. C100 | 20 | 3 | 0 |  |  |  |  |  |  |  |  |  |  |  |
| 4. HV100 | 19 | 0 | 3 | 0 |  |  |  |  |  |  |  |  |  |  |
| 5. NSF6 | 14 | 16 | 17 | 16 | 0 |  |  |  |  |  |  |  |  |  |
| 6. HVNSF6 | 18 | 9 | 10 | 9 | 16 | 0 |  |  |  |  |  |  |  |  |
| 7. Top 10% | 12 | 21 | 21 | 21 | 17 | 21 | 0 |  |  |  |  |  |  |  |
| 8. HV10% | 12 | 21 | 21 | 21 | 17 | 21 | 0 | 0 |  |  |  |  |  |  |
| 9. HV10% min-max | 12 | 21 | 21 | 21 | 17 | 21 | 4 | 4 | 0 |  |  |  |  |  |
| 10. ANG10% | 21 | 25 | 25 | 25 | 23 | 23 | 18 | 18 | 17 | 0 |  |  |  |  |
| 11. Top 1% | 22 | 23 | 22 | 23 | 20 | 22 | 22 | 22 | 22 | 18 | 0 |  |  |  |
| 12. HV1% | 22 | 23 | 22 | 23 | 20 | 22 | 22 | 22 | 22 | 18 | 0 | 0 |  |  |
| 13. HV1% min-max | 22 | 23 | 22 | 23 | 20 | 22 | 22 | 22 | 22 | 18 | 1 | 1 | 0 |  |
| 14. ANG1% | 26 | 29 | 29 | 29 | 28 | 29 | 29 | 29 | 28 | 26 | 24 | 24 | 24 | 0 |

**Part D. Physics.**

|  | RCR | HV max | C100 | HV100 | NSF6 | HVNSF6 | Top 10% | HV 10% | HV10% min-max | ANG 10% | Top 1% | HV 1% | HV1% min-max | ANG 1% |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
|  | (1) | (2) | (3) | (4) | (5) | (6) | (7) | (8) | (9) | (10) | (11) | (12) | (13) | (14) |
| 1. RCR | 0 |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 2. HV max | 23 | 0 |  |  |  |  |  |  |  |  |  |  |  |  |
| 3. C100 | 23 | 0 | 0 |  |  |  |  |  |  |  |  |  |  |  |
| 4. HV100 | 23 | 0 | 0 | 0 |  |  |  |  |  |  |  |  |  |  |
| 5. NSF6 | 17 | 13 | 13 | 13 | 0 |  |  |  |  |  |  |  |  |  |
| 6. HVNSF6 | 23 | 5 | 5 | 5 | 14 | 0 |  |  |  |  |  |  |  |  |
| 7. Top 10% | 17 | 22 | 22 | 22 | 17 | 22 | 0 |  |  |  |  |  |  |  |
| 8. HV10% | 17 | 22 | 22 | 22 | 17 | 22 | 0 | 0 |  |  |  |  |  |  |
| 9. HV10% min-max | 16 | 23 | 23 | 23 | 19 | 23 | 3 | 3 | 0 |  |  |  |  |  |
| 10. ANG10% | 22 | 25 | 25 | 25 | 25 | 25 | 20 | 20 | 20 | 0 |  |  |  |  |
| 11. Top 1% | 22 | 24 | 24 | 24 | 23 | 24 | 22 | 22 | 21 | 20 | 0 |  |  |  |
| 12. HV1% | 22 | 24 | 24 | 24 | 23 | 24 | 22 | 22 | 21 | 20 | 0 | 0 |  |  |
| 13. HV1% min-max | 22 | 24 | 24 | 24 | 23 | 24 | 22 | 22 | 21 | 20 | 0 | 0 | 0 |  |
| 14. ANG1% | 23 | 27 | 27 | 27 | 25 | 26 | 25 | 25 | 24 | 22 | 21 | 21 | 21 | 0 |

**Table 2. The variability of the 14 procedures in terms of the range, the ratio Max/Min, and the coefficient of Variation (CV). Selected scientific fields**

| | Clinical Medicine | | | Physics | | | Engineering | | | Economics & Business | | |
|---|---|---|---|---|---|---|---|---|---|---|---|---|
| | Range | Max./Min. | CV | Range | Max./Min. | CV | Range | Max./Min. | CV | Range | Max./Min. | CV |
| **1. RCR** | 1.06 | 5.43 | 0.334 | 1.12 | 3.55 | 0.264 | 0.99 | 2.84 | 0.217 | 1.11 | 9.39 | 0.335 |
| **2. HV max** | 1.26 | 8.48 | 0.331 | 0.99 | 2.92 | 0.243 | 1.08 | 3.26 | 0.212 | 1.08 | 9.40 | 0.330 |
| **3. C100** | 0.79 | 3.15 | 0.184 | 0.47 | 1.65 | 0.116 | 0.47 | 1.65 | 0.095 | 0.67 | 2.62 | 0.167 |
| **4. HV100** | 1.26 | 8.49 | 0.331 | 0.99 | 2.93 | 0.243 | 1.08 | 3.26 | 0.212 | 1.08 | 9.40 | 0.331 |
| **5. NSF6** | 0.51 | 1.81 | 0.141 | 0.46 | 1.62 | 0.113 | 0.44 | 1.56 | 0.094 | 0.52 | 1.92 | 0.129 |
| **6. HVNSF6** | 1.34 | 9.43 | 0.398 | 1.22 | 3.92 | 0.301 | 1.20 | 3.65 | 0.243 | 1.16 | 13.79 | 0.374 |
| **7. Top 10%** | 1.27 | 11.03 | 0.469 | 1.85 | * | 0.443 | 1.51 | 5.17 | 0.352 | 1.38 | * | 0.496 |
| **8. HV10%** | 1.34 | 12.62 | 0.499 | 2.03 | * | 0.480 | 1.70 | 5.98 | 0.387 | 1.44 | * | 0.522 |
| **9. HV10% min-max** | 1.31 | 11.96 | 0.485 | 1.96 | * | 0.464 | 1.63 | 5.68 | 0.374 | 1.42 | * | 0.514 |
| ***10. ANG10%*** | 1.45 | 34.26 | 0.519 | 2.14 | * | 0.509 | 1.65 | 5.69 | 0.436 | 1.50 | * | 0.664 |
| ***11. Top 1%*** | 1.58 | * | 0.578 | 2.43 | * | 0.565 | 2.35 | * | 0.587 | 1.61 | * | 1.062 |
| **12. HV1%** | 1.58 | * | 0.581 | 2.46 | * | 0.570 | 2.38 | * | 0.593 | 1.62 | * | 1.066 |
| **13. HV1% min-max** | 1.58 | * | 0.579 | 2.44 | * | 0.567 | 2.37 | * | 0.591 | 1.61 | * | 1.065 |
| **14. ANG1%** | 1.76 | * | 0.604 | 2.37 | * | 0.692 | 2.09 | * | 0.600 | 2.96 | * | 1.440 |

\* Since the minimum value is zero, the ratio Max/Min becomes infinite.

**Table SM1. Evaluation results for the 14 procedures.**

**Part A. Clinical Medicine**

| COUNTRY | RCR | HV max | C100 | HV100 | NSF6 | HVNSF6 | Top 10% |
|---|---|---|---|---|---|---|---|
| | (1) | (2) | (3) | (4) | (5) | (6) | (7) |
| ARGENTINA | 0.75 | 0.68 | 0.83 | 0.68 | 0.85 | 0.60 | 0.58 |
| AUSTRALIA | 1.04 | 1.07 | 1.03 | 1.07 | 1.01 | 1.06 | 1.00 |
| AUSTRIA | 0.92 | 0.98 | 0.99 | 0.98 | 0.98 | 0.98 | 0.86 |
| BELGIUM | 1.21 | 1.14 | 1.06 | 1.14 | 1.07 | 1.18 | 1.28 |
| BRAZIL | 0.66 | 0.72 | 0.85 | 0.72 | 0.83 | 0.61 | 0.45 |
| CANADA | 1.23 | 1.27 | 1.11 | 1.27 | 1.10 | 1.32 | 1.26 |
| CHINA | 0.76 | 0.81 | 0.90 | 0.81 | 0.90 | 0.76 | 0.64 |
| CZECH REPUBLIC | 0.82 | 0.76 | 0.87 | 0.76 | 0.90 | 0.73 | 0.71 |
| DENMARK | 1.27 | 1.37 | 1.14 | 1.37 | 1.12 | 1.42 | 1.32 |
| FINLAND | 1.26 | 1.36 | 1.14 | 1.36 | 1.11 | 1.41 | 1.23 |
| FRANCE | 0.89 | 0.76 | 0.88 | 0.76 | 0.93 | 0.76 | 0.90 |
| GERMANY | 0.89 | 0.85 | 0.93 | 0.85 | 0.95 | 0.85 | 0.89 |
| GREECE | 0.68 | 0.78 | 0.88 | 0.78 | 0.87 | 0.69 | 0.53 |
| HUNGARY | 0.87 | 0.86 | 0.93 | 0.86 | 0.92 | 0.78 | 0.73 |
| INDIA | 0.40 | 0.50 | 0.70 | 0.50 | 0.73 | 0.38 | 0.18 |
| IRAN | 0.41 | 0.54 | 0.72 | 0.54 | 0.74 | 0.41 | 0.17 |
| IRELAND | 0.93 | 0.93 | 0.97 | 0.93 | 0.96 | 0.91 | 0.86 |
| ISRAEL | 0.79 | 0.81 | 0.90 | 0.81 | 0.90 | 0.74 | 0.66 |
| ITALY | 1.03 | 1.06 | 1.02 | 1.06 | 1.01 | 1.06 | 1.01 |
| JAPAN | 0.72 | 0.82 | 0.91 | 0.82 | 0.89 | 0.75 | 0.60 |
| LUXEMBOURG | 0.89 | 1.07 | 1.03 | 1.07 | 1.02 | 1.12 | 0.83 |
| MEXICO | 0.67 | 0.65 | 0.80 | 0.65 | 0.82 | 0.56 | 0.49 |
| NETHERLANDS | 1.30 | 1.43 | 1.16 | 1.43 | 1.14 | 1.50 | 1.39 |
| NEW ZEALAND | 0.97 | 0.97 | 0.98 | 0.97 | 0.97 | 0.93 | 0.87 |
| NORWAY | 1.16 | 1.28 | 1.11 | 1.28 | 1.07 | 1.28 | 1.04 |
| POLAND | 0.77 | 0.75 | 0.87 | 0.74 | 0.88 | 0.68 | 0.64 |
| PORTUGAL | 1.03 | 1.01 | 1.00 | 1.01 | 1.01 | 1.02 | 1.04 |
| RW | 0.56 | 0.58 | 0.76 | 0.58 | 0.80 | 0.50 | 0.41 |
| RUSSIA | 0.24 | 0.17 | 0.37 | 0.17 | 0.63 | 0.16 | 0.22 |
| SINGAPORE | 0.77 | 0.82 | 0.91 | 0.82 | 0.89 | 0.73 | 0.55 |
| SOUTH AFRICA | 0.74 | 0.71 | 0.85 | 0.71 | 0.86 | 0.64 | 0.56 |
| SOUTH KOREA | 0.67 | 0.83 | 0.91 | 0.83 | 0.88 | 0.74 | 0.56 |
| SPAIN | 0.82 | 0.76 | 0.87 | 0.76 | 0.90 | 0.72 | 0.76 |
| SWEDEN | 1.15 | 1.31 | 1.12 | 1.31 | 1.08 | 1.32 | 1.10 |
| SWITZERLAND | 1.21 | 1.11 | 1.05 | 1.11 | 1.06 | 1.16 | 1.26 |
| TAIWAN | 0.64 | 0.76 | 0.88 | 0.76 | 0.85 | 0.66 | 0.42 |
| TURKEY | 0.36 | 0.48 | 0.68 | 0.48 | 0.70 | 0.33 | 0.13 |
| UK | 1.04 | 1.05 | 1.02 | 1.05 | 1.02 | 1.06 | 1.05 |
| UKRAINE | 0.24 | 0.26 | 0.48 | 0.26 | 0.64 | 0.21 | 0.13 |
| UNITED STATES | 1.19 | 1.24 | 1.10 | 1.24 | 1.09 | 1.29 | 1.30 |

**Table SM1.I. Evaluation results for the 14 procedures.**
**Part A. Clinical Medicine (cont'd.)**

| COUNTRY | HV10% | HV10% min-max | ANG10% | Top 1% | HV1% | HV1% min- max | ANG1% |
|---|---|---|---|---|---|---|---|
| | (8) | (9) | (10) | (11) | (12) | (13) | (14) |
| ARGENTINA | 0.56 | 0.57 | 0.84 | 0.92 | 0.92 | 0.92 | 1.33 |
| AUSTRALIA | 1.00 | 1.00 | 1.05 | 1.00 | 1.00 | 1.00 | 1.18 |
| AUSTRIA | 0.85 | 0.85 | 0.77 | 0.79 | 0.78 | 0.78 | 0.64 |
| BELGIUM | 1.33 | 1.31 | 1.47 | 1.55 | 1.56 | 1.56 | 1.75 |
| BRAZIL | 0.42 | 0.44 | 0.54 | 0.57 | 0.57 | 0.57 | 0.77 |
| CANADA | 1.30 | 1.29 | 1.41 | 1.51 | 1.52 | 1.52 | 1.61 |
| CHINA | 0.61 | 0.62 | 0.60 | 0.58 | 0.58 | 0.58 | 0.62 |
| CZECH REPUBLIC | 0.69 | 0.70 | 0.85 | 0.98 | 0.98 | 0.98 | 1.04 |
| DENMARK | 1.37 | 1.34 | 1.42 | 1.36 | 1.37 | 1.37 | 1.76 |
| FINLAND | 1.26 | 1.25 | 1.40 | 1.35 | 1.36 | 1.35 | 1.72 |
| FRANCE | 0.89 | 0.90 | 0.97 | 0.92 | 0.92 | 0.92 | 1.08 |
| GERMANY | 0.88 | 0.89 | 0.86 | 0.83 | 0.83 | 0.83 | 0.83 |
| GREECE | 0.50 | 0.51 | 0.45 | 0.42 | 0.42 | 0.42 | 0.33 |
| HUNGARY | 0.71 | 0.72 | 0.90 | 1.17 | 1.18 | 1.18 | 1.23 |
| INDIA | 0.16 | 0.17 | 0.14 | 0.15 | 0.15 | 0.15 | 0.12 |
| IRAN | 0.15 | 0.16 | 0.10 | 0.10 | 0.10 | 0.10 | 0.04 |
| IRELAND | 0.84 | 0.85 | 0.93 | 0.91 | 0.91 | 0.91 | 1.18 |
| ISRAEL | 0.64 | 0.65 | 0.72 | 0.80 | 0.80 | 0.80 | 0.82 |
| ITALY | 1.01 | 1.01 | 1.02 | 1.05 | 1.05 | 1.05 | 1.03 |
| JAPAN | 0.58 | 0.59 | 0.45 | 0.39 | 0.39 | 0.39 | 0.28 |
| LUXEMBOURG | 0.81 | 0.82 | 0.52 | 0.00 | 0.00 | 0.00 | 0.00 |
| MEXICO | 0.46 | 0.47 | 0.62 | 0.44 | 0.44 | 0.44 | 1.04 |
| NETHERLANDS | 1.46 | 1.43 | 1.43 | 1.49 | 1.50 | 1.49 | 1.46 |
| NEW ZEALAND | 0.85 | 0.86 | 1.03 | 1.21 | 1.22 | 1.21 | 1.26 |
| NORWAY | 1.04 | 1.04 | 1.23 | 1.14 | 1.14 | 1.14 | 1.60 |
| POLAND | 0.62 | 0.63 | 0.76 | 0.83 | 0.83 | 0.83 | 0.86 |
| PORTUGAL | 1.04 | 1.05 | 1.06 | 1.36 | 1.36 | 1.36 | 0.75 |
| RW | 0.38 | 0.39 | 0.39 | 0.42 | 0.42 | 0.42 | 0.37 |
| RUSSIA | 0.20 | 0.21 | 0.21 | 0.23 | 0.23 | 0.23 | 0.18 |
| SINGAPORE | 0.52 | 0.53 | 0.70 | 0.60 | 0.59 | 0.60 | 1.06 |
| SOUTH AFRICA | 0.54 | 0.55 | 0.74 | 0.91 | 0.91 | 0.91 | 1.01 |
| SOUTH KOREA | 0.54 | 0.54 | 0.31 | 0.16 | 0.16 | 0.16 | 0.11 |
| SPAIN | 0.75 | 0.75 | 0.82 | 0.75 | 0.75 | 0.75 | 1.00 |
| SWEDEN | 1.11 | 1.10 | 1.14 | 1.13 | 1.14 | 1.14 | 1.25 |
| SWITZERLAND | 1.30 | 1.29 | 1.49 | 1.58 | 1.59 | 1.58 | 1.68 |
| TAIWAN | 0.39 | 0.40 | 0.36 | 0.32 | 0.32 | 0.32 | 0.37 |
| TURKEY | 0.12 | 0.12 | 0.08 | 0.06 | 0.06 | 0.06 | 0.05 |
| UK | 1.06 | 1.05 | 1.06 | 1.08 | 1.08 | 1.08 | 1.08 |
| UKRAINE | 0.12 | 0.12 | 0.04 | 0.00 | 0.00 | 0.00 | 0.00 |
| UNITED STATES | 1.34 | 1.32 | 1.27 | 1.27 | 1.27 | 1.27 | 1.17 |

**Table SM1. Evaluation results for the 14 procedures.**
**Part B. Physics**

| COUNTRY | RCR | HV max | C100 | HV100 | NSF6 | HVNSF6 | Top 10% |
|---|---|---|---|---|---|---|---|
| | (1) | (2) | (3) | (4) | (5) | (6) | (7) |
| ARGENTINA | 0.81 | 0.93 | 0.97 | 0.93 | 0.94 | 0.87 | 0.70 |
| AUSTRALIA | 0.97 | 1.11 | 1.05 | 1.11 | 1.02 | 1.11 | 1.00 |
| AUSTRIA | 1.23 | 1.22 | 1.09 | 1.22 | 1.10 | 1.27 | 1.32 |
| BELGIUM | 1.01 | 1.15 | 1.06 | 1.15 | 1.04 | 1.15 | 1.05 |
| BRAZIL | 0.76 | 0.87 | 0.94 | 0.87 | 0.90 | 0.79 | 0.59 |
| CANADA | 1.17 | 1.16 | 1.07 | 1.16 | 1.06 | 1.17 | 1.15 |
| CHINA | 0.63 | 0.69 | 0.84 | 0.69 | 0.84 | 0.62 | 0.49 |
| CZECH REPUBLIC | 0.77 | 0.82 | 0.91 | 0.82 | 0.91 | 0.79 | 0.72 |
| DENMARK | 1.37 | 1.50 | 1.19 | 1.50 | 1.19 | 1.64 | 1.66 |
| FINLAND | 1.17 | 1.18 | 1.08 | 1.18 | 1.06 | 1.21 | 1.07 |
| FRANCE | 1.03 | 1.07 | 1.03 | 1.07 | 1.02 | 1.09 | 1.04 |
| GERMANY | 1.15 | 1.24 | 1.10 | 1.24 | 1.09 | 1.29 | 1.26 |
| GREECE | 0.96 | 1.12 | 1.05 | 1.12 | 1.02 | 1.12 | 0.92 |
| HUNGARY | 1.00 | 1.05 | 1.02 | 1.05 | 1.01 | 1.06 | 0.86 |
| INDIA | 0.71 | 0.70 | 0.84 | 0.70 | 0.85 | 0.64 | 0.52 |
| IRAN | 0.71 | 0.79 | 0.90 | 0.79 | 0.88 | 0.72 | 0.56 |
| IRELAND | 1.00 | 1.08 | 1.04 | 1.08 | 1.02 | 1.07 | 1.00 |
| ISRAEL | 1.10 | 1.18 | 1.08 | 1.19 | 1.06 | 1.20 | 1.12 |
| ITALY | 1.07 | 1.08 | 1.03 | 1.08 | 1.03 | 1.10 | 1.09 |
| JAPAN | 0.86 | 0.90 | 0.95 | 0.90 | 0.94 | 0.86 | 0.78 |
| LUXEMBOURG | 0.88 | 1.28 | 1.11 | 1.28 | 1.05 | 1.29 | 0.00 |
| MEXICO | 0.60 | 0.68 | 0.83 | 0.68 | 0.83 | 0.61 | 0.43 |
| NETHERLANDS | 1.20 | 1.27 | 1.11 | 1.27 | 1.11 | 1.34 | 1.33 |
| NEW ZEALAND | 1.08 | 1.08 | 1.03 | 1.08 | 1.03 | 1.08 | 1.11 |
| NORWAY | 1.08 | 1.22 | 1.09 | 1.22 | 1.07 | 1.26 | 1.05 |
| POLAND | 0.85 | 0.80 | 0.90 | 0.80 | 0.91 | 0.75 | 0.73 |
| PORTUGAL | 1.03 | 1.12 | 1.05 | 1.12 | 1.04 | 1.13 | 1.04 |
| RW | 0.62 | 0.68 | 0.83 | 0.68 | 0.83 | 0.60 | 0.50 |
| RUSSIA | 0.62 | 0.61 | 0.78 | 0.61 | 0.81 | 0.54 | 0.50 |
| SINGAPORE | 0.67 | 0.82 | 0.91 | 0.82 | 0.88 | 0.75 | 0.51 |
| SOUTH AFRICA | 0.67 | 0.74 | 0.87 | 0.74 | 0.85 | 0.65 | 0.45 |
| SOUTH KOREA | 0.82 | 0.82 | 0.91 | 0.82 | 0.91 | 0.76 | 0.72 |
| SPAIN | 1.10 | 1.16 | 1.07 | 1.16 | 1.05 | 1.18 | 1.09 |
| SWEDEN | 1.11 | 1.16 | 1.07 | 1.17 | 1.05 | 1.19 | 1.09 |
| SWITZERLAND | 1.55 | 1.45 | 1.17 | 1.45 | 1.21 | 1.59 | 1.85 |
| TAIWAN | 0.74 | 0.76 | 0.88 | 0.76 | 0.88 | 0.70 | 0.60 |
| TURKEY | 0.64 | 0.75 | 0.87 | 0.75 | 0.85 | 0.66 | 0.40 |
| UK | 1.14 | 1.15 | 1.07 | 1.15 | 1.06 | 1.19 | 1.19 |
| UKRAINE | 0.44 | 0.51 | 0.72 | 0.51 | 0.74 | 0.42 | 0.25 |
| UNITED STATES | 1.35 | 1.34 | 1.13 | 1.34 | 1.14 | 1.42 | 1.50 |

**Table SM1. Evaluation results for the 14 procedures.**
**Part B. Physics (cont'd.)**

| COUNTRY | HV10% | HV10% min-max | ANG10% | Top 1% | HV1% | HV1% min-max | ANG1% |
|---|---|---|---|---|---|---|---|
| | (8) | (9) | (10) | (11) | (12) | (13) | (14) |
| ARGENTINA | 0.68 | 0.68 | 0.53 | 0.68 | 0.52 | 0.52 | 0.37 |
| AUSTRALIA | 1.00 | 0.99 | 0.72 | 1.00 | 0.65 | 0.65 | 0.40 |
| AUSTRIA | 1.37 | 1.36 | 1.40 | 1.37 | 1.48 | 1.47 | 1.27 |
| BELGIUM | 1.06 | 1.05 | 0.81 | 1.06 | 0.64 | 0.64 | 0.56 |
| BRAZIL | 0.57 | 0.58 | 0.54 | 0.57 | 0.54 | 0.55 | 0.51 |
| CANADA | 1.17 | 1.16 | 1.37 | 1.17 | 1.32 | 1.31 | 1.79 |
| CHINA | 0.47 | 0.47 | 0.40 | 0.47 | 0.38 | 0.38 | 0.33 |
| CZECH REPUBLIC | 0.70 | 0.71 | 0.53 | 0.70 | 0.41 | 0.41 | 0.25 |
| DENMARK | 1.78 | 1.71 | 1.44 | 1.78 | 1.41 | 1.41 | 1.05 |
| FINLAND | 1.08 | 1.07 | 1.34 | 1.08 | 0.78 | 0.78 | 2.37 |
| FRANCE | 1.05 | 1.04 | 0.96 | 1.05 | 0.86 | 0.86 | 0.88 |
| GERMANY | 1.29 | 1.27 | 1.11 | 1.29 | 1.07 | 1.07 | 0.84 |
| GREECE | 0.91 | 0.91 | 0.70 | 0.91 | 0.67 | 0.67 | 0.40 |
| HUNGARY | 0.85 | 0.86 | 0.96 | 0.85 | 1.16 | 1.16 | 1.03 |
| INDIA | 0.49 | 0.50 | 0.69 | 0.49 | 0.59 | 0.59 | 1.13 |
| IRAN | 0.54 | 0.55 | 0.49 | 0.54 | 0.63 | 0.63 | 0.35 |
| IRELAND | 1.01 | 1.01 | 0.88 | 1.01 | 0.97 | 0.96 | 0.48 |
| ISRAEL | 1.14 | 1.13 | 1.02 | 1.14 | 1.01 | 1.01 | 0.72 |
| ITALY | 1.10 | 1.10 | 1.09 | 1.10 | 1.03 | 1.03 | 1.18 |
| JAPAN | 0.76 | 0.77 | 0.75 | 0.76 | 0.72 | 0.72 | 0.75 |
| LUXEMBOURG | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| MEXICO | 0.41 | 0.42 | 0.33 | 0.41 | 0.35 | 0.35 | 0.12 |
| NETHERLANDS | 1.38 | 1.36 | 1.21 | 1.38 | 1.38 | 1.38 | 0.97 |
| NEW ZEALAND | 1.13 | 1.12 | 1.13 | 1.13 | 0.97 | 0.98 | 1.07 |
| NORWAY | 1.05 | 1.04 | 0.93 | 1.05 | 0.92 | 0.92 | 0.79 |
| POLAND | 0.71 | 0.72 | 0.90 | 0.71 | 0.90 | 0.90 | 1.21 |
| PORTUGAL | 1.04 | 1.04 | 0.91 | 1.04 | 1.27 | 1.27 | 0.61 |
| RW | 0.47 | 0.48 | 0.41 | 0.47 | 0.41 | 0.42 | 0.27 |
| RUSSIA | 0.48 | 0.49 | 0.52 | 0.48 | 0.53 | 0.54 | 0.62 |
| SINGAPORE | 0.48 | 0.49 | 0.27 | 0.48 | 0.07 | 0.07 | 0.01 |
| SOUTH AFRICA | 0.42 | 0.44 | 0.50 | 0.42 | 0.62 | 0.63 | 0.51 |
| SOUTH KOREA | 0.70 | 0.71 | 0.77 | 0.70 | 0.65 | 0.65 | 0.93 |
| SPAIN | 1.10 | 1.09 | 1.09 | 1.10 | 1.00 | 1.00 | 1.22 |
| SWEDEN | 1.10 | 1.08 | 1.13 | 1.10 | 0.90 | 0.90 | 1.53 |
| SWITZERLAND | 2.03 | 1.96 | 2.14 | 2.03 | 2.46 | 2.45 | 2.28 |
| TAIWAN | 0.58 | 0.59 | 0.63 | 0.58 | 0.61 | 0.61 | 0.73 |
| TURKEY | 0.37 | 0.39 | 0.40 | 0.37 | 0.42 | 0.42 | 0.32 |
| UK | 1.21 | 1.20 | 1.22 | 1.21 | 1.23 | 1.23 | 1.28 |
| UKRAINE | 0.23 | 0.24 | 0.17 | 0.23 | 0.12 | 0.12 | 0.08 |
| UNITED STATES | 1.58 | 1.55 | 1.64 | 1.58 | 1.78 | 1.77 | 1.68 |

**Table SM1. Evaluation results for the 14 procedures.**
**Part C. Engineering**

| COUNTRY | RCR | HV max | C100 | HV100 | NSF6 | HVNSF6 | Top 10% |
|---|---|---|---|---|---|---|---|
| | (1) | (2) | (3) | (4) | (5) | (6) | (7) |
| ARGENTINA | 0.96 | 1.08 | 1.03 | 1.08 | 1.00 | 1.06 | 0.91 |
| AUSTRALIA | 1.02 | 1.10 | 1.04 | 1.10 | 1.02 | 1.10 | 1.01 |
| AUSTRIA | 1.11 | 1.14 | 1.05 | 1.14 | 1.06 | 1.15 | 1.21 |
| BELGIUM | 1.30 | 1.34 | 1.13 | 1.34 | 1.13 | 1.39 | 1.50 |
| BRAZIL | 0.92 | 1.02 | 1.01 | 1.02 | 0.98 | 1.00 | 0.79 |
| CANADA | 1.00 | 1.03 | 1.01 | 1.03 | 1.00 | 1.02 | 0.93 |
| CHINA | 0.88 | 0.90 | 0.96 | 0.90 | 0.95 | 0.87 | 0.81 |
| CZECH REPUBLIC | 1.07 | 1.01 | 1.00 | 1.01 | 1.03 | 1.03 | 1.28 |
| DENMARK | 1.48 | 1.49 | 1.17 | 1.49 | 1.20 | 1.60 | 1.80 |
| FINLAND | 1.17 | 1.19 | 1.07 | 1.19 | 1.07 | 1.23 | 1.26 |
| FRANCE | 1.12 | 1.21 | 1.08 | 1.21 | 1.07 | 1.23 | 1.14 |
| GERMANY | 1.14 | 1.11 | 1.04 | 1.11 | 1.06 | 1.14 | 1.25 |
| GREECE | 0.85 | 0.96 | 0.99 | 0.96 | 0.95 | 0.94 | 0.71 |
| HUNGARY | 1.04 | 1.14 | 1.06 | 1.14 | 1.04 | 1.14 | 1.07 |
| INDIA | 0.68 | 0.73 | 0.87 | 0.73 | 0.86 | 0.68 | 0.49 |
| IRAN | 1.08 | 1.08 | 1.03 | 1.08 | 1.04 | 1.07 | 1.24 |
| IRELAND | 1.00 | 0.99 | 1.00 | 0.99 | 1.01 | 1.00 | 1.00 |
| ISRAEL | 1.11 | 1.12 | 1.05 | 1.12 | 1.04 | 1.13 | 1.12 |
| ITALY | 1.06 | 1.16 | 1.06 | 1.16 | 1.04 | 1.16 | 1.07 |
| JAPAN | 0.82 | 0.83 | 0.92 | 0.83 | 0.93 | 0.81 | 0.76 |
| LUXEMBOURG | 1.06 | 1.30 | 1.11 | 1.30 | 1.12 | 1.45 | 1.28 |
| MEXICO | 0.72 | 0.78 | 0.90 | 0.78 | 0.89 | 0.74 | 0.52 |
| NETHERLANDS | 1.19 | 1.23 | 1.09 | 1.23 | 1.09 | 1.26 | 1.30 |
| NEW ZEALAND | 0.89 | 1.01 | 1.00 | 1.01 | 0.97 | 0.97 | 0.74 |
| NORWAY | 1.15 | 1.11 | 1.05 | 1.11 | 1.05 | 1.13 | 1.26 |
| POLAND | 0.89 | 0.96 | 0.98 | 0.96 | 0.96 | 0.93 | 0.74 |
| PORTUGAL | 0.94 | 1.10 | 1.04 | 1.10 | 1.00 | 1.09 | 0.85 |
| RW | 0.65 | 0.70 | 0.86 | 0.70 | 0.85 | 0.66 | 0.48 |
| RUSSIA | 0.53 | 0.48 | 0.72 | 0.48 | 0.78 | 0.45 | 0.45 |
| SINGAPORE | 0.96 | 1.06 | 1.03 | 1.06 | 1.00 | 1.05 | 0.92 |
| SOUTH AFRICA | 0.72 | 0.83 | 0.92 | 0.83 | 0.90 | 0.78 | 0.56 |
| SOUTH KOREA | 0.82 | 0.90 | 0.96 | 0.90 | 0.93 | 0.86 | 0.70 |
| SPAIN | 1.10 | 1.22 | 1.09 | 1.22 | 1.07 | 1.24 | 1.10 |
| SWEDEN | 1.24 | 1.31 | 1.11 | 1.31 | 1.11 | 1.33 | 1.33 |
| SWITZERLAND | 1.52 | 1.56 | 1.19 | 1.56 | 1.21 | 1.65 | 1.87 |
| TAIWAN | 0.85 | 0.94 | 0.98 | 0.94 | 0.94 | 0.90 | 0.68 |
| TURKEY | 0.97 | 1.09 | 1.04 | 1.09 | 1.01 | 1.09 | 0.87 |
| UK | 0.98 | 1.00 | 1.00 | 1.00 | 0.99 | 0.99 | 0.94 |
| UKRAINE | 0.54 | 0.52 | 0.75 | 0.52 | 0.79 | 0.50 | 0.36 |
| UNITED STATES | 1.17 | 1.11 | 1.04 | 1.11 | 1.06 | 1.14 | 1.27 |

**Table SM1. Evaluation results for the 14 procedures.**
**Part C. Engineering (cont'd.)**

| COUNTRY | HV10% | HV10% min-max | ANG10% | Top 1% | HV1% | HV1% min-max | ANG1% |
|---|---|---|---|---|---|---|---|
| | (8) | (9) | (10) | (11) | (12) | (13) | (14) |
| ARGENTINA | 0.90 | 0.90 | 0.77 | 0.88 | 0.87 | 0.87 | 0.36 |
| AUSTRALIA | 1.01 | 1.01 | 0.87 | 0.73 | 0.73 | 0.73 | 0.59 |
| AUSTRIA | 1.23 | 1.22 | 1.12 | 1.15 | 1.15 | 1.15 | 0.84 |
| BELGIUM | 1.57 | 1.55 | 1.50 | 1.52 | 1.53 | 1.53 | 1.23 |
| BRAZIL | 0.77 | 0.78 | 0.72 | 0.67 | 0.66 | 0.66 | 0.62 |
| CANADA | 0.92 | 0.93 | 0.99 | 1.04 | 1.04 | 1.04 | 1.10 |
| CHINA | 0.80 | 0.80 | 0.79 | 0.81 | 0.81 | 0.81 | 0.81 |
| CZECH REPUBLIC | 1.32 | 1.29 | 1.13 | 0.90 | 0.90 | 0.90 | 0.81 |
| DENMARK | 1.95 | 1.89 | 1.96 | 2.35 | 2.38 | 2.37 | 2.09 |
| FINLAND | 1.29 | 1.27 | 1.29 | 1.40 | 1.40 | 1.40 | 1.61 |
| FRANCE | 1.16 | 1.15 | 1.06 | 0.97 | 0.97 | 0.97 | 0.93 |
| GERMANY | 1.28 | 1.26 | 1.26 | 1.30 | 1.30 | 1.30 | 1.25 |
| GREECE | 0.69 | 0.69 | 0.56 | 0.43 | 0.43 | 0.43 | 0.53 |
| HUNGARY | 1.07 | 1.06 | 0.81 | 0.58 | 0.58 | 0.58 | 0.56 |
| INDIA | 0.47 | 0.47 | 0.46 | 0.34 | 0.34 | 0.34 | 0.55 |
| IRAN | 1.27 | 1.26 | 1.12 | 0.78 | 0.78 | 0.78 | 0.34 |
| IRELAND | 1.00 | 1.00 | 0.96 | 0.97 | 0.97 | 0.97 | 0.76 |
| ISRAEL | 1.13 | 1.13 | 1.21 | 1.22 | 1.22 | 1.22 | 1.39 |
| ITALY | 1.07 | 1.07 | 0.94 | 0.92 | 0.92 | 0.92 | 0.63 |
| JAPAN | 0.75 | 0.75 | 0.70 | 0.63 | 0.63 | 0.63 | 0.59 |
| LUXEMBOURG | 1.31 | 1.26 | 0.55 | 0.00 | 0.00 | 0.00 | 0.00 |
| MEXICO | 0.50 | 0.51 | 0.46 | 0.25 | 0.25 | 0.25 | 0.51 |
| NETHERLANDS | 1.34 | 1.32 | 1.25 | 1.43 | 1.44 | 1.43 | 1.04 |
| NEW ZEALAND | 0.72 | 0.73 | 0.59 | 0.66 | 0.66 | 0.66 | 0.20 |
| NORWAY | 1.29 | 1.29 | 1.41 | 1.11 | 1.11 | 1.11 | 1.76 |
| POLAND | 0.73 | 0.73 | 0.77 | 0.65 | 0.64 | 0.65 | 1.04 |
| PORTUGAL | 0.84 | 0.83 | 0.63 | 0.28 | 0.28 | 0.28 | 0.41 |
| RW | 0.46 | 0.46 | 0.36 | 0.30 | 0.30 | 0.30 | 0.23 |
| RUSSIA | 0.42 | 0.43 | 0.46 | 0.39 | 0.38 | 0.38 | 0.57 |
| SINGAPORE | 0.91 | 0.91 | 0.78 | 0.72 | 0.72 | 0.72 | 0.42 |
| SOUTH AFRICA | 0.54 | 0.54 | 0.35 | 0.17 | 0.17 | 0.17 | 0.26 |
| SOUTH KOREA | 0.68 | 0.68 | 0.61 | 0.50 | 0.50 | 0.50 | 0.57 |
| SPAIN | 1.11 | 1.10 | 0.97 | 0.87 | 0.87 | 0.87 | 0.71 |
| SWEDEN | 1.38 | 1.36 | 1.38 | 1.46 | 1.47 | 1.47 | 1.40 |
| SWITZERLAND | 2.04 | 1.97 | 2.01 | 1.99 | 2.01 | 2.00 | 2.03 |
| TAIWAN | 0.66 | 0.67 | 0.63 | 0.55 | 0.55 | 0.55 | 0.68 |
| TURKEY | 0.85 | 0.86 | 0.76 | 0.67 | 0.67 | 0.67 | 0.53 |
| UK | 0.94 | 0.94 | 0.94 | 0.90 | 0.90 | 0.90 | 0.98 |
| UKRAINE | 0.34 | 0.35 | 0.37 | 0.17 | 0.17 | 0.17 | 0.67 |
| UNITED STATES | 1.31 | 1.30 | 1.41 | 1.53 | 1.54 | 1.54 | 1.58 |

**Table SM1. Evaluation results for the 14 procedures.**
**Part D. Economics & Business**

| COUNTRY | RCR | HV max | C100 | HV100 | NSF6 | HVNSF6 | Top 10% |
|---|---|---|---|---|---|---|---|
| | (1) | (2) | (3) | (4) | (5) | (6) | (7) |
| ARGENTINA | 0.32 | 0.31 | 0.59 | 0.31 | 0.69 | 0.31 | 0.12 |
| AUSTRALIA | 0.68 | 0.80 | 0.90 | 0.80 | 0.88 | 0.75 | 0.48 |
| AUSTRIA | 0.72 | 0.81 | 0.91 | 0.81 | 0.89 | 0.76 | 0.59 |
| BELGIUM | 0.95 | 1.02 | 1.01 | 1.02 | 0.99 | 0.99 | 1.04 |
| BRAZIL | 0.56 | 0.59 | 0.79 | 0.59 | 0.80 | 0.50 | 0.55 |
| CANADA | 0.88 | 0.97 | 0.98 | 0.97 | 0.97 | 0.96 | 0.81 |
| CHINA | 0.93 | 1.08 | 1.03 | 1.08 | 1.00 | 1.06 | 0.73 |
| CZECH REPUBLIC | 0.13 | 0.13 | 0.41 | 0.13 | 0.57 | 0.09 | 0.09 |
| DENMARK | 0.83 | 0.90 | 0.95 | 0.90 | 0.95 | 0.91 | 0.79 |
| FINLAND | 0.72 | 0.75 | 0.88 | 0.75 | 0.90 | 0.76 | 0.54 |
| FRANCE | 0.88 | 0.83 | 0.92 | 0.83 | 0.94 | 0.81 | 0.83 |
| GERMANY | 0.71 | 0.73 | 0.87 | 0.73 | 0.88 | 0.70 | 0.57 |
| GREECE | 0.50 | 0.58 | 0.78 | 0.58 | 0.79 | 0.52 | 0.14 |
| HUNGARY | 0.75 | 0.73 | 0.87 | 0.73 | 0.89 | 0.71 | 0.67 |
| INDIA | 0.51 | 0.60 | 0.79 | 0.60 | 0.80 | 0.55 | 0.35 |
| IRAN | 0.56 | 0.63 | 0.80 | 0.63 | 0.74 | 0.34 | 0.79 |
| IRELAND | 0.73 | 0.80 | 0.90 | 0.80 | 0.89 | 0.73 | 0.52 |
| ISRAEL | 0.97 | 1.04 | 1.01 | 1.04 | 0.99 | 1.02 | 0.80 |
| ITALY | 0.82 | 0.87 | 0.94 | 0.87 | 0.93 | 0.84 | 0.74 |
| JAPAN | 0.51 | 0.57 | 0.77 | 0.57 | 0.78 | 0.50 | 0.32 |
| LUXEMBOURG | 0.61 | 0.59 | 0.79 | 0.59 | 0.85 | 0.56 | 0.64 |
| MEXICO | 0.69 | 0.63 | 0.82 | 0.63 | 0.84 | 0.63 | 0.49 |
| NETHERLANDS | 0.94 | 1.08 | 1.03 | 1.08 | 1.01 | 1.08 | 0.92 |
| NEW ZEALAND | 0.64 | 0.76 | 0.88 | 0.76 | 0.86 | 0.69 | 0.44 |
| NORWAY | 0.80 | 1.02 | 1.00 | 1.02 | 0.97 | 1.04 | 0.59 |
| POLAND | 0.44 | 0.57 | 0.77 | 0.57 | 0.78 | 0.53 | 0.18 |
| PORTUGAL | 0.64 | 0.72 | 0.86 | 0.72 | 0.86 | 0.66 | 0.68 |
| RW | 0.49 | 0.50 | 0.73 | 0.50 | 0.77 | 0.46 | 0.30 |
| RUSSIA | 0.48 | 0.40 | 0.67 | 0.40 | 0.76 | 0.40 | 0.48 |
| SINGAPORE | 0.89 | 0.91 | 0.96 | 0.91 | 0.95 | 0.87 | 0.80 |
| SOUTH AFRICA | 0.36 | 0.50 | 0.72 | 0.50 | 0.72 | 0.40 | 0.00 |
| SOUTH KOREA | 0.80 | 0.83 | 0.92 | 0.83 | 0.94 | 0.83 | 0.81 |
| SPAIN | 0.72 | 0.81 | 0.91 | 0.81 | 0.89 | 0.76 | 0.59 |
| SWEDEN | 1.00 | 1.15 | 1.05 | 1.15 | 1.03 | 1.13 | 1.01 |
| SWITZERLAND | 1.08 | 0.97 | 0.99 | 0.97 | 1.00 | 0.95 | 1.05 |
| TAIWAN | 0.57 | 0.66 | 0.82 | 0.66 | 0.81 | 0.58 | 0.31 |
| TURKEY | 0.50 | 0.60 | 0.79 | 0.60 | 0.80 | 0.55 | 0.30 |
| UK | 0.93 | 1.05 | 1.02 | 1.05 | 0.99 | 1.03 | 0.83 |
| UKRAINE | 0.31 | 0.25 | 0.54 | 0.25 | 0.66 | 0.24 | 0.54 |
| UNITED STATES | 1.25 | 1.21 | 1.08 | 1.21 | 1.09 | 1.25 | 1.38 |

**Table SM1. Evaluation results for the 14 procedures.**
**Part D. Economics & Business (cont'd.)**

| COUNTRY | HV10% | HV10% min-max | ANG10% | Top 1% | HV1% | HV1% min-max | ANG1% |
|---|---|---|---|---|---|---|---|
| | (8) | (9) | (10) | (11) | (12) | (13) | (14) |
| ARGENTINA | 0.11 | 0.11 | 0.09 | 0.00 | 0.00 | 0.00 | 0.00 |
| AUSTRALIA | 0.45 | 0.46 | 0.33 | 0.22 | 0.22 | 0.22 | 0.11 |
| AUSTRIA | 0.57 | 0.58 | 0.42 | 0.24 | 0.24 | 0.24 | 0.07 |
| BELGIUM | 1.04 | 1.02 | 0.73 | 0.67 | 0.67 | 0.67 | 0.20 |
| BRAZIL | 0.53 | 0.53 | 0.29 | 0.00 | 0.00 | 0.00 | 0.00 |
| CANADA | 0.79 | 0.79 | 0.66 | 0.52 | 0.52 | 0.52 | 0.27 |
| CHINA | 0.71 | 0.72 | 0.65 | 0.70 | 0.70 | 0.70 | 0.58 |
| CZECH REPUBLIC | 0.09 | 0.09 | 0.04 | 0.00 | 0.00 | 0.00 | 0.00 |
| DENMARK | 0.78 | 0.78 | 0.59 | 0.46 | 0.46 | 0.46 | 0.34 |
| FINLAND | 0.52 | 0.53 | 0.47 | 0.64 | 0.64 | 0.64 | 0.11 |
| FRANCE | 0.82 | 0.83 | 0.87 | 1.08 | 1.08 | 1.08 | 0.94 |
| GERMANY | 0.55 | 0.55 | 0.52 | 0.40 | 0.40 | 0.40 | 0.69 |
| GREECE | 0.12 | 0.13 | 0.19 | 0.29 | 0.29 | 0.29 | 0.24 |
| HUNGARY | 0.64 | 0.65 | 0.48 | 0.00 | 0.00 | 0.00 | 0.00 |
| INDIA | 0.33 | 0.33 | 0.12 | 0.00 | 0.00 | 0.00 | 0.00 |
| IRAN | 0.77 | 0.77 | 0.39 | 0.00 | 0.00 | 0.00 | 0.00 |
| IRELAND | 0.49 | 0.50 | 0.51 | 0.34 | 0.34 | 0.34 | 0.42 |
| ISRAEL | 0.79 | 0.80 | 0.94 | 1.17 | 1.17 | 1.17 | 0.93 |
| ITALY | 0.72 | 0.73 | 0.64 | 0.23 | 0.22 | 0.22 | 0.16 |
| JAPAN | 0.30 | 0.31 | 0.30 | 0.28 | 0.28 | 0.28 | 0.28 |
| LUXEMBOURG | 0.62 | 0.63 | 0.38 | 0.00 | 0.00 | 0.00 | 0.00 |
| MEXICO | 0.46 | 0.46 | 0.63 | 1.15 | 1.16 | 1.16 | 1.88 |
| NETHERLANDS | 0.92 | 0.91 | 0.66 | 0.41 | 0.41 | 0.41 | 0.20 |
| NEW ZEALAND | 0.42 | 0.43 | 0.30 | 0.21 | 0.20 | 0.20 | 0.18 |
| NORWAY | 0.56 | 0.56 | 0.36 | 0.18 | 0.18 | 0.18 | 0.21 |
| POLAND | 0.16 | 0.16 | 0.03 | 0.00 | 0.00 | 0.00 | 0.00 |
| PORTUGAL | 0.65 | 0.65 | 0.37 | 0.00 | 0.00 | 0.00 | 0.00 |
| RW | 0.28 | 0.29 | 0.27 | 0.42 | 0.42 | 0.42 | 0.31 |
| RUSSIA | 0.45 | 0.46 | 0.39 | 0.46 | 0.46 | 0.46 | 0.47 |
| SINGAPORE | 0.78 | 0.79 | 0.84 | 0.68 | 0.68 | 0.69 | 1.11 |
| SOUTH AFRICA | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
| SOUTH KOREA | 0.79 | 0.80 | 0.62 | 0.17 | 0.17 | 0.17 | 0.07 |
| SPAIN | 0.56 | 0.56 | 0.49 | 0.43 | 0.43 | 0.43 | 0.58 |
| SWEDEN | 1.01 | 1.00 | 0.76 | 0.57 | 0.57 | 0.57 | 0.49 |
| SWITZERLAND | 1.06 | 1.06 | 1.40 | 1.49 | 1.49 | 1.50 | 2.96 |
| TAIWAN | 0.29 | 0.30 | 0.30 | 0.18 | 0.18 | 0.18 | 0.64 |
| TURKEY | 0.28 | 0.29 | 0.19 | 0.00 | 0.00 | 0.00 | 0.00 |
| UK | 0.82 | 0.82 | 0.74 | 0.62 | 0.61 | 0.61 | 0.68 |
| UKRAINE | 0.52 | 0.52 | 0.21 | 0.00 | 0.00 | 0.00 | 0.00 |
| UNITED STATES | 1.44 | 1.42 | 1.50 | 1.61 | 1.62 | 1.61 | 1.62 |

**Table SM2. Country ranks according to each procedure.**

**Part A. Clinical Medicine**

| COUNTRY | RCR | HV max | C100 | HV100 | NSF6 | HVNSF6 | Top 10% | HV10% | HV10% min-max | ANG10% | Top 1% | HV1% | HV1% min-max | ANG1% |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| | (1) | (2) | (3) | (4) | (5) | (6) | (7) | (8) | (9) | (10) | (11) | (12) | (13) | (14) |
| ARGENTINA | 27 | 33 | 33 | 33 | 31 | 33 | 27 | 27 | 27 | 20 | 17 | 17 | 17 | 8 |
| AUSTRALIA | 11 | 11 | 11 | 11 | 13 | 11 | 13 | 13 | 13 | 12 | 15 | 15 | 15 | 12 |
| AUSTRIA | 16 | 15 | 15 | 15 | 15 | 15 | 17 | 17 | 17 | 22 | 24 | 24 | 24 | 28 |
| BELGIUM | 5 | 8 | 8 | 8 | 7 | 8 | 4 | 4 | 4 | 2 | 2 | 2 | 2 | 2 |
| BRAZIL | 33 | 31 | 32 | 31 | 33 | 32 | 33 | 33 | 33 | 29 | 28 | 28 | 28 | 26 |
| CANADA | 4 | 6 | 6 | 6 | 4 | 5 | 5 | 5 | 6 | 5 | 3 | 3 | 3 | 5 |
| CHINA | 26 | 23 | 23 | 23 | 21 | 20 | 25 | 25 | 25 | 28 | 27 | 27 | 27 | 29 |
| CZECH REPUBLIC | 22 | 29 | 29 | 29 | 23 | 26 | 22 | 22 | 22 | 19 | 16 | 16 | 16 | 18 |
| DENMARK | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 4 | 5 | 5 | 5 | 1 |
| FINLAND | 3 | 3 | 3 | 3 | 3 | 3 | 7 | 7 | 7 | 6 | 7 | 7 | 7 | 3 |
| FRANCE | 19 | 27 | 26 | 27 | 19 | 21 | 14 | 14 | 14 | 15 | 18 | 18 | 18 | 15 |
| GERMANY | 18 | 19 | 18 | 19 | 18 | 18 | 15 | 15 | 15 | 18 | 21 | 21 | 21 | 24 |
| GREECE | 30 | 25 | 25 | 25 | 29 | 28 | 31 | 31 | 31 | 32 | 31 | 31 | 31 | 32 |
| HUNGARY | 20 | 18 | 19 | 18 | 20 | 19 | 21 | 21 | 21 | 17 | 10 | 10 | 10 | 11 |
| INDIA | 37 | 37 | 37 | 37 | 37 | 37 | 37 | 37 | 37 | 37 | 36 | 36 | 36 | 35 |
| IRAN | 36 | 36 | 36 | 36 | 36 | 36 | 38 | 38 | 38 | 38 | 37 | 37 | 37 | 38 |
| IRELAND | 15 | 17 | 17 | 17 | 17 | 17 | 18 | 18 | 18 | 16 | 19 | 19 | 19 | 13 |
| ISRAEL | 23 | 24 | 24 | 24 | 24 | 23 | 23 | 23 | 23 | 25 | 23 | 23 | 23 | 25 |
| ITALY | 13 | 12 | 12 | 12 | 12 | 12 | 12 | 12 | 12 | 14 | 14 | 14 | 14 | 20 |
| JAPAN | 29 | 21 | 21 | 21 | 25 | 22 | 26 | 26 | 26 | 31 | 32 | 32 | 32 | 33 |
| LUXEMBOURG | 17 | 10 | 10 | 10 | 11 | 10 | 19 | 19 | 19 | 30 | 39 | 39 | 39 | 39 |
| MEXICO | 32 | 34 | 34 | 34 | 34 | 34 | 32 | 32 | 32 | 27 | 29 | 29 | 29 | 19 |
| NETHERLANDS | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 3 | 4 | 4 | 4 | 7 |
| NEW ZEALAND | 14 | 16 | 16 | 16 | 16 | 16 | 16 | 16 | 16 | 13 | 9 | 9 | 9 | 9 |
| NORWAY | 8 | 5 | 5 | 5 | 8 | 7 | 11 | 11 | 11 | 8 | 11 | 11 | 11 | 6 |
| POLAND | 25 | 30 | 30 | 30 | 28 | 29 | 24 | 24 | 24 | 23 | 22 | 22 | 22 | 23 |
| PORTUGAL | 12 | 14 | 14 | 14 | 14 | 14 | 10 | 10 | 10 | 11 | 6 | 6 | 6 | 27 |
| RW | 35 | 35 | 35 | 35 | 35 | 35 | 35 | 35 | 35 | 33 | 30 | 30 | 30 | 30 |
| RUSSIA | 40 | 40 | 40 | 40 | 40 | 40 | 36 | 36 | 36 | 36 | 34 | 34 | 34 | 34 |
| SINGAPORE | 24 | 22 | 22 | 22 | 26 | 25 | 30 | 30 | 30 | 26 | 26 | 26 | 26 | 17 |
| SOUTH AFRICA | 28 | 32 | 31 | 32 | 30 | 31 | 28 | 28 | 28 | 24 | 20 | 20 | 20 | 21 |
| SOUTH KOREA | 31 | 20 | 20 | 20 | 27 | 24 | 29 | 29 | 29 | 35 | 35 | 35 | 35 | 36 |
| SPAIN | 21 | 28 | 28 | 28 | 22 | 27 | 20 | 20 | 20 | 21 | 25 | 25 | 25 | 22 |
| SWEDEN | 9 | 4 | 4 | 4 | 6 | 4 | 8 | 8 | 8 | 9 | 12 | 12 | 12 | 10 |
| SWITZERLAND | 6 | 9 | 9 | 9 | 9 | 9 | 6 | 6 | 5 | 1 | 1 | 1 | 1 | 4 |
| TAIWAN | 34 | 26 | 27 | 26 | 32 | 30 | 34 | 34 | 34 | 34 | 33 | 33 | 33 | 31 |
| TURKEY | 38 | 38 | 38 | 38 | 38 | 38 | 39 | 39 | 39 | 39 | 38 | 38 | 38 | 37 |
| UK | 10 | 13 | 13 | 13 | 10 | 13 | 9 | 9 | 9 | 10 | 13 | 13 | 13 | 16 |
| UKRAINE | 39 | 39 | 39 | 39 | 39 | 39 | 40 | 40 | 40 | 40 | 40 | 40 | 40 | 40 |
| UNITED STATES | 7 | 7 | 7 | 7 | 5 | 6 | 3 | 3 | 3 | 7 | 8 | 8 | 8 | 14 |

**Table SM2. Country ranks according to each procedure.  (cont'd.)**
**Part B. Physics**

| COUNTRY | RCR (1) | HV max (2) | C100 (3) | HV100 (4) | NSF6 (5) | HVNSF6 (6) | Top 10% (7) | HV 10% (8) | HV 10% min-max (9) | ANG 10% (10) | Top 1% (11) | HV 1% (12) | HV 1% min-max (13) | ANG 1% (14) |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| ARGENTINA | 27 | 24 | 24 | 24 | 25 | 24 | 27 | 27 | 27 | 30 | 27 | 32 | 32 | 31 |
| AUSTRALIA | 21 | 18 | 18 | 18 | 20 | 18 | 20 | 20 | 20 | 24 | 20 | 24 | 24 | 29 |
| AUSTRIA | 4 | 7 | 7 | 7 | 5 | 7 | 5 | 5 | 4 | 4 | 5 | 3 | 3 | 7 |
| BELGIUM | 18 | 15 | 15 | 15 | 15 | 15 | 15 | 15 | 15 | 21 | 15 | 25 | 25 | 25 |
| BRAZIL | 29 | 26 | 26 | 26 | 29 | 26 | 29 | 29 | 29 | 28 | 29 | 30 | 30 | 27 |
| CANADA | 7 | 13 | 13 | 13 | 10 | 14 | 8 | 8 | 8 | 5 | 8 | 6 | 6 | 3 |
| CHINA | 36 | 36 | 36 | 36 | 36 | 36 | 35 | 35 | 35 | 35 | 35 | 36 | 36 | 33 |
| CZECH REPUBLIC | 28 | 27 | 27 | 27 | 26 | 27 | 25 | 25 | 26 | 29 | 25 | 35 | 35 | 36 |
| DENMARK | 2 | 1 | 1 | 1 | 2 | 1 | 2 | 2 | 2 | 3 | 2 | 4 | 4 | 13 |
| FINLAND | 6 | 10 | 10 | 10 | 11 | 9 | 14 | 14 | 14 | 6 | 14 | 20 | 20 | 1 |
| FRANCE | 17 | 22 | 22 | 22 | 19 | 20 | 17 | 17 | 17 | 16 | 17 | 19 | 19 | 17 |
| GERMANY | 8 | 6 | 6 | 6 | 6 | 6 | 6 | 6 | 6 | 11 | 6 | 10 | 10 | 18 |
| GREECE | 22 | 17 | 17 | 17 | 21 | 17 | 21 | 21 | 21 | 25 | 21 | 22 | 22 | 30 |
| HUNGARY | 19 | 23 | 23 | 23 | 23 | 23 | 22 | 22 | 22 | 15 | 22 | 9 | 9 | 14 |
| INDIA | 31 | 35 | 35 | 35 | 33 | 35 | 31 | 31 | 31 | 26 | 31 | 29 | 29 | 11 |
| IRAN | 32 | 31 | 31 | 31 | 31 | 31 | 30 | 30 | 30 | 33 | 30 | 26 | 26 | 32 |
| IRELAND | 20 | 19 | 19 | 19 | 22 | 22 | 19 | 19 | 19 | 20 | 19 | 15 | 15 | 28 |
| ISRAEL | 12 | 9 | 9 | 9 | 8 | 10 | 9 | 9 | 9 | 14 | 9 | 12 | 12 | 22 |
| ITALY | 15 | 20 | 20 | 20 | 17 | 19 | 11 | 11 | 11 | 12 | 11 | 11 | 11 | 10 |
| JAPAN | 24 | 25 | 25 | 25 | 24 | 25 | 23 | 23 | 23 | 23 | 23 | 21 | 21 | 20 |
| LUXEMBOURG | 23 | 4 | 4 | 4 | 14 | 5 | 40 | 40 | 40 | 40 | 40 | 40 | 40 | 40 |
| MEXICO | 39 | 37 | 37 | 37 | 38 | 37 | 37 | 37 | 37 | 37 | 37 | 37 | 37 | 37 |
| NETHERLANDS | 5 | 5 | 5 | 5 | 4 | 4 | 4 | 4 | 5 | 8 | 4 | 5 | 5 | 15 |
| NEW ZEALAND | 13 | 21 | 21 | 21 | 18 | 21 | 10 | 10 | 10 | 9 | 10 | 14 | 14 | 12 |
| NORWAY | 14 | 8 | 8 | 8 | 7 | 8 | 16 | 16 | 16 | 17 | 16 | 16 | 16 | 19 |
| POLAND | 25 | 30 | 30 | 30 | 28 | 30 | 24 | 24 | 24 | 19 | 24 | 17 | 17 | 9 |
| PORTUGAL | 16 | 16 | 16 | 16 | 16 | 16 | 18 | 18 | 18 | 18 | 18 | 7 | 7 | 24 |
| RW | 37 | 38 | 38 | 38 | 37 | 38 | 34 | 34 | 34 | 34 | 34 | 34 | 34 | 35 |
| RUSSIA | 38 | 39 | 39 | 39 | 39 | 39 | 33 | 33 | 32 | 31 | 33 | 31 | 31 | 23 |
| SINGAPORE | 33 | 29 | 29 | 29 | 30 | 29 | 32 | 32 | 33 | 38 | 32 | 39 | 39 | 39 |
| SOUTH AFRICA | 34 | 34 | 34 | 34 | 35 | 34 | 36 | 36 | 36 | 32 | 36 | 27 | 27 | 26 |
| SOUTH KOREA | 26 | 28 | 28 | 28 | 27 | 28 | 26 | 26 | 25 | 22 | 26 | 23 | 23 | 16 |
| SPAIN | 11 | 12 | 12 | 12 | 13 | 13 | 12 | 12 | 12 | 13 | 12 | 13 | 13 | 8 |
| SWEDEN | 10 | 11 | 11 | 11 | 12 | 11 | 13 | 13 | 13 | 10 | 13 | 18 | 18 | 5 |
| SWITZERLAND | 1 | 2 | 2 | 2 | 1 | 2 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 2 |
| TAIWAN | 30 | 32 | 32 | 32 | 32 | 32 | 28 | 28 | 28 | 27 | 28 | 28 | 28 | 21 |
| TURKEY | 35 | 33 | 33 | 33 | 34 | 33 | 38 | 38 | 38 | 36 | 38 | 33 | 33 | 34 |
| UK | 9 | 14 | 14 | 14 | 9 | 12 | 7 | 7 | 7 | 7 | 7 | 8 | 8 | 6 |
| UKRAINE | 40 | 40 | 40 | 40 | 40 | 40 | 39 | 39 | 39 | 39 | 39 | 38 | 38 | 38 |
| UNITED STATES | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 3 | 2 | 3 | 2 | 2 | 4 |

**Part C. Engineering**

| COUNTRY | RCR (1) | HV max (2) | C100 (3) | HV100 (4) | NSF6 (5) | HVNSF6 (6) | Top 10% (7) | HV 10% (8) | HV 10% min-max (9) | ANG 10% (10) | Top 1% (11) | HV 1% (12) | HV 1% min-max (13) | ANG 1% (14) |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| ARGENTINA | 25 | 21 | 20 | 21 | 24 | 21 | 24 | 24 | 24 | 24 | 18 | 18 | 19 | 35 |
| AUSTRALIA | 19 | 18 | 19 | 18 | 19 | 17 | 19 | 19 | 19 | 20 | 22 | 22 | 22 | 24 |
| AUSTRIA | 11 | 12 | 12 | 12 | 12 | 11 | 13 | 13 | 13 | 12 | 10 | 10 | 10 | 15 |
| BELGIUM | 3 | 3 | 3 | 3 | 3 | 4 | 3 | 3 | 3 | 3 | 4 | 4 | 4 | 9 |
| BRAZIL | 27 | 24 | 24 | 24 | 27 | 25 | 28 | 28 | 28 | 27 | 25 | 25 | 25 | 23 |
| CANADA | 20 | 23 | 23 | 23 | 25 | 24 | 22 | 22 | 22 | 15 | 12 | 12 | 12 | 10 |
| CHINA | 30 | 33 | 33 | 33 | 31 | 32 | 27 | 27 | 27 | 22 | 20 | 20 | 20 | 16 |
| CZECH REPUBLIC | 15 | 25 | 25 | 25 | 18 | 23 | 6 | 6 | 7 | 11 | 17 | 17 | 17 | 17 |
| DENMARK | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 1 | 1 | 1 | 1 |
| FINLAND | 6 | 9 | 9 | 9 | 7 | 9 | 9 | 9 | 9 | 7 | 7 | 7 | 7 | 4 |
| FRANCE | 10 | 8 | 8 | 8 | 8 | 8 | 14 | 14 | 14 | 14 | 13 | 13 | 13 | 14 |
| GERMANY | 9 | 14 | 15 | 14 | 11 | 12 | 11 | 11 | 11 | 8 | 8 | 8 | 8 | 8 |
| GREECE | 31 | 29 | 29 | 29 | 30 | 29 | 32 | 32 | 32 | 33 | 32 | 32 | 32 | 31 |
| HUNGARY | 18 | 11 | 11 | 11 | 17 | 13 | 18 | 18 | 18 | 21 | 29 | 29 | 29 | 28 |
| INDIA | 37 | 37 | 37 | 37 | 37 | 37 | 37 | 37 | 37 | 36 | 34 | 34 | 34 | 29 |
| IRAN | 14 | 20 | 21 | 20 | 16 | 20 | 12 | 12 | 10 | 13 | 21 | 21 | 21 | 36 |
| IRELAND | 21 | 28 | 28 | 28 | 21 | 26 | 20 | 20 | 20 | 17 | 14 | 14 | 14 | 18 |
| ISRAEL | 12 | 13 | 13 | 13 | 15 | 15 | 15 | 15 | 15 | 10 | 9 | 9 | 9 | 7 |
| ITALY | 16 | 10 | 10 | 10 | 14 | 10 | 17 | 17 | 17 | 18 | 15 | 15 | 15 | 22 |
| JAPAN | 33 | 34 | 34 | 34 | 34 | 34 | 29 | 29 | 29 | 28 | 28 | 28 | 28 | 25 |
| LUXEMBOURG | 17 | 5 | 5 | 5 | 4 | 3 | 7 | 7 | 12 | 34 | 40 | 40 | 40 | 40 |
| MEXICO | 35 | 36 | 36 | 36 | 36 | 36 | 36 | 36 | 36 | 35 | 37 | 37 | 37 | 32 |
| NETHERLANDS | 5 | 6 | 6 | 6 | 6 | 6 | 5 | 5 | 5 | 9 | 6 | 6 | 6 | 11 |
| NEW ZEALAND | 29 | 26 | 26 | 26 | 28 | 28 | 31 | 31 | 31 | 32 | 26 | 26 | 26 | 39 |
| NORWAY | 8 | 15 | 14 | 15 | 13 | 16 | 10 | 10 | 8 | 5 | 11 | 11 | 11 | 3 |
| POLAND | 28 | 30 | 30 | 30 | 29 | 30 | 30 | 30 | 30 | 25 | 27 | 27 | 27 | 12 |
| PORTUGAL | 26 | 17 | 17 | 17 | 22 | 18 | 26 | 26 | 26 | 30 | 36 | 36 | 36 | 34 |
| RW | 38 | 38 | 38 | 38 | 38 | 38 | 38 | 38 | 38 | 39 | 35 | 35 | 35 | 38 |
| RUSSIA | 40 | 40 | 40 | 40 | 40 | 40 | 39 | 39 | 39 | 37 | 33 | 33 | 33 | 26 |
| SINGAPORE | 24 | 22 | 22 | 22 | 23 | 22 | 23 | 23 | 23 | 23 | 23 | 23 | 23 | 33 |
| SOUTH AFRICA | 36 | 35 | 35 | 35 | 35 | 35 | 35 | 35 | 35 | 40 | 38 | 38 | 38 | 37 |
| SOUTH KOREA | 34 | 32 | 32 | 32 | 33 | 33 | 33 | 33 | 33 | 31 | 31 | 31 | 31 | 27 |
| SPAIN | 13 | 7 | 7 | 7 | 9 | 7 | 16 | 16 | 16 | 16 | 19 | 19 | 18 | 19 |
| SWEDEN | 4 | 4 | 4 | 4 | 5 | 5 | 4 | 4 | 4 | 6 | 5 | 5 | 5 | 6 |
| SWITZERLAND | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 2 | 2 | 2 | 2 |
| TAIWAN | 32 | 31 | 31 | 31 | 32 | 31 | 34 | 34 | 34 | 29 | 30 | 30 | 30 | 20 |
| TURKEY | 23 | 19 | 18 | 19 | 20 | 19 | 25 | 25 | 25 | 26 | 24 | 24 | 24 | 30 |
| UK | 22 | 27 | 27 | 27 | 26 | 27 | 21 | 21 | 21 | 19 | 16 | 16 | 16 | 13 |
| UKRAINE | 39 | 39 | 39 | 39 | 39 | 39 | 40 | 40 | 40 | 38 | 39 | 39 | 39 | 21 |
| UNITED STATES | 7 | 16 | 16 | 16 | 10 | 14 | 8 | 8 | 6 | 4 | 3 | 3 | 3 | 5 |

**Part D. Economics & Business**

| COUNTRY | RCR (1) | HV max (2) | C100 (3) | HV100 (4) | NSF6 (5) | HVNSF6 (6) | Top 10% (7) | HV 10% (8) | HV 10% min-max (9) | ANG 10% (10) | Top 1% (11) | HV 1% (12) | HV 1% min-max (13) | ANG 1% (14) |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| ARGENTINA | 38 | 38 | 38 | 38 | 38 | 38 | 38 | 38 | 38 | 37 | 37 | 37 | 37 | 37 |
| AUSTRALIA | 23 | 19 | 19 | 19 | 21 | 19 | 28 | 28 | 28 | 27 | 24 | 24 | 24 | 26 |
| AUSTRIA | 20 | 16 | 16 | 16 | 18 | 17 | 19 | 19 | 19 | 21 | 22 | 22 | 22 | 27 |
| BELGIUM | 5 | 7 | 7 | 7 | 7 | 8 | 3 | 3 | 3 | 8 | 8 | 8 | 8 | 22 |
| BRAZIL | 29 | 30 | 31 | 30 | 29 | 32 | 23 | 23 | 24 | 31 | 33 | 33 | 33 | 33 |
| CANADA | 10 | 10 | 10 | 10 | 9 | 9 | 9 | 9 | 10 | 10 | 12 | 12 | 12 | 18 |
| CHINA | 8 | 3 | 4 | 3 | 5 | 4 | 15 | 15 | 15 | 11 | 6 | 6 | 6 | 11 |
| CZECH REPUBLIC | 40 | 40 | 40 | 40 | 40 | 40 | 39 | 39 | 39 | 38 | 38 | 38 | 38 | 38 |
| DENMARK | 12 | 12 | 12 | 12 | 12 | 11 | 12 | 12 | 12 | 15 | 14 | 14 | 14 | 15 |
| FINLAND | 18 | 21 | 20 | 21 | 16 | 16 | 24 | 24 | 23 | 20 | 9 | 9 | 9 | 25 |
| FRANCE | 11 | 15 | 15 | 15 | 13 | 15 | 6 | 6 | 6 | 4 | 5 | 5 | 5 | 5 |
| GERMANY | 21 | 22 | 23 | 22 | 22 | 22 | 22 | 22 | 22 | 16 | 18 | 18 | 18 | 7 |
| GREECE | 33 | 32 | 32 | 32 | 31 | 31 | 37 | 37 | 37 | 34 | 20 | 20 | 20 | 19 |
| HUNGARY | 16 | 23 | 22 | 23 | 17 | 21 | 17 | 17 | 17 | 19 | 29 | 29 | 29 | 29 |
| INDIA | 31 | 28 | 28 | 28 | 28 | 28 | 31 | 31 | 31 | 36 | 36 | 36 | 36 | 36 |
| IRAN | 28 | 27 | 27 | 27 | 36 | 37 | 13 | 13 | 13 | 23 | 30 | 30 | 30 | 30 |
| IRELAND | 17 | 18 | 18 | 18 | 19 | 20 | 26 | 26 | 26 | 17 | 19 | 19 | 19 | 14 |
| ISRAEL | 4 | 6 | 6 | 6 | 6 | 7 | 10 | 10 | 8 | 3 | 3 | 3 | 3 | 6 |
| ITALY | 13 | 13 | 13 | 13 | 15 | 13 | 14 | 14 | 14 | 12 | 23 | 23 | 23 | 24 |
| JAPAN | 30 | 34 | 34 | 34 | 33 | 33 | 32 | 32 | 32 | 28 | 21 | 21 | 21 | 17 |
| LUXEMBOURG | 26 | 31 | 30 | 31 | 25 | 27 | 18 | 18 | 18 | 24 | 31 | 31 | 31 | 31 |
| MEXICO | 22 | 26 | 26 | 26 | 26 | 25 | 27 | 27 | 27 | 13 | 4 | 4 | 4 | 2 |
| NETHERLANDS | 6 | 4 | 3 | 4 | 3 | 3 | 5 | 5 | 5 | 9 | 17 | 17 | 17 | 21 |
| NEW ZEALAND | 25 | 20 | 21 | 20 | 24 | 23 | 30 | 30 | 30 | 29 | 25 | 25 | 25 | 23 |
| NORWAY | 15 | 8 | 8 | 8 | 10 | 5 | 21 | 21 | 21 | 26 | 27 | 27 | 27 | 20 |
| POLAND | 36 | 33 | 33 | 33 | 32 | 30 | 36 | 36 | 36 | 39 | 39 | 39 | 39 | 39 |
| PORTUGAL | 24 | 24 | 24 | 24 | 23 | 24 | 16 | 16 | 16 | 25 | 32 | 32 | 32 | 32 |
| RW | 34 | 35 | 35 | 35 | 34 | 34 | 34 | 34 | 34 | 32 | 16 | 16 | 16 | 16 |
| RUSSIA | 35 | 37 | 37 | 37 | 35 | 35 | 29 | 29 | 29 | 22 | 13 | 13 | 13 | 13 |
| SINGAPORE | 9 | 11 | 11 | 11 | 11 | 12 | 11 | 11 | 11 | 5 | 7 | 7 | 7 | 4 |
| SOUTH AFRICA | 37 | 36 | 36 | 36 | 37 | 36 | 40 | 40 | 40 | 40 | 40 | 40 | 40 | 40 |
| SOUTH KOREA | 14 | 14 | 14 | 14 | 14 | 14 | 8 | 8 | 9 | 14 | 28 | 28 | 28 | 28 |
| SPAIN | 19 | 17 | 17 | 17 | 20 | 18 | 20 | 20 | 20 | 18 | 15 | 15 | 15 | 10 |
| SWEDEN | 3 | 2 | 2 | 2 | 2 | 2 | 4 | 4 | 4 | 6 | 11 | 11 | 11 | 12 |
| SWITZERLAND | 2 | 9 | 9 | 9 | 4 | 10 | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 1 |
| TAIWAN | 27 | 25 | 25 | 25 | 27 | 26 | 33 | 33 | 33 | 30 | 26 | 26 | 26 | 9 |
| TURKEY | 32 | 29 | 29 | 29 | 30 | 29 | 35 | 35 | 35 | 35 | 35 | 35 | 35 | 35 |
| UK | 7 | 5 | 5 | 5 | 8 | 6 | 7 | 7 | 7 | 7 | 10 | 10 | 10 | 8 |
| UKRAINE | 39 | 39 | 39 | 39 | 39 | 39 | 25 | 25 | 25 | 33 | 34 | 34 | 34 | 34 |
| UNITED STATES | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 3 |

**Table SM3. Kendall (rank) correlation results for the 14 procedures.**

**Part A. Clinical Medicine**

| | RCR | HV max | C100 | HV100 | NSF6 | HVNSF6 | Top 10% | HV 10% | HV10% min-max | ANG 10% | Top 1% | HV 1% | HV1% min-max | ANG 1% |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| **1. RCR** | 1.000 | | | | | | | | | | | | | |
| **2. HV max** | 0.808 | 1.000 | | | | | | | | | | | | |
| **3. C100** | 0.815 | 0.992 | 1.000 | | | | | | | | | | | |
| **4. HV100** | 0.808 | 1.000 | 0.992 | 1.000 | | | | | | | | | | |
| **5. NSF6** | 0.910 | 0.887 | 0.895 | 0.887 | 1.000 | | | | | | | | | |
| **6. HVNSF6** | 0.854 | 0.944 | 0.951 | 0.944 | 0.938 | 1.000 | | | | | | | | |
| **7. Top 10%** | 0.903 | 0.756 | 0.764 | 0.756 | 0.864 | 0.808 | 1.000 | | | | | | | |
| **8. HV10%** | 0.903 | 0.756 | 0.764 | 0.756 | 0.864 | 0.808 | 1.000 | 1.000 | | | | | | |
| **9. HV10% min-max** | 0.900 | 0.754 | 0.762 | 0.754 | 0.862 | 0.805 | 0.997 | 0.997 | 1.000 | | | | | |
| **10. ANG10%** | 0.846 | 0.659 | 0.662 | 0.659 | 0.756 | 0.705 | 0.846 | 0.846 | 0.849 | 1.000 | | | | |
| **11. Top 1%** | 0.730 | 0.558 | 0.561 | 0.558 | 0.650 | 0.604 | 0.740 | 0.740 | 0.743 | 0.874 | 1.000 | | | |
| **12. HV1%** | 0.730 | 0.558 | 0.561 | 0.558 | 0.650 | 0.604 | 0.740 | 0.740 | 0.743 | 0.874 | 1.000 | 1.000 | | |
| **13. HV1% min-max** | 0.730 | 0.558 | 0.561 | 0.558 | 0.650 | 0.604 | 0.740 | 0.740 | 0.743 | 0.874 | 1.000 | 1.000 | 1.000 | |
| **14. ANG1%** | 0.635 | 0.489 | 0.491 | 0.489 | 0.550 | 0.525 | 0.604 | 0.604 | 0.607 | 0.743 | 0.782 | 0.782 | 0.782 | 1.000 |

**Part B. Physics**

| | RCR | HV max | C100 | HV100 | NSF6 | HVNSF6 | Top 10% | HV 10% | HV10% min-max | ANG 10% | Top 1% | HV 1% | HV1% min-max | ANG 1% |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| **1. RCR** | 1.000 | | | | | | | | | | | | | |
| **2. HV max** | 0.790 | 1.000 | | | | | | | | | | | | |
| **3. C100** | 0.790 | 1.000 | 1.000 | | | | | | | | | | | |
| **4. HV100** | 0.790 | 1.000 | 1.000 | 1.000 | | | | | | | | | | |
| **5. NSF6** | 0.869 | 0.905 | 0.905 | 0.905 | 1.000 | | | | | | | | | |
| **6. HVNSF6** | 0.800 | 0.979 | 0.979 | 0.979 | 0.915 | 1.000 | | | | | | | | |
| **7. Top 10%** | 0.854 | 0.710 | 0.710 | 0.710 | 0.805 | 0.721 | 1.000 | | | | | | | |
| **8. HV10%** | 0.854 | 0.710 | 0.710 | 0.710 | 0.805 | 0.721 | 1.000 | 1.000 | | | | | | |
| **9. HV10% min-max** | 0.856 | 0.703 | 0.703 | 0.703 | 0.797 | 0.713 | 0.992 | 0.992 | 1.000 | | | | | |
| **10. ANG10%** | 0.813 | 0.608 | 0.608 | 0.608 | 0.687 | 0.618 | 0.831 | 0.831 | 0.838 | 1.000 | | | | |
| **11. Top 1%** | 0.713 | 0.579 | 0.579 | 0.579 | 0.649 | 0.579 | 0.762 | 0.762 | 0.769 | 0.797 | 1.000 | | | |
| **12. HV1%** | 0.713 | 0.579 | 0.579 | 0.579 | 0.649 | 0.579 | 0.762 | 0.762 | 0.769 | 0.797 | 1.000 | 1.000 | | |
| **13. HV1% min-max** | 0.713 | 0.579 | 0.579 | 0.579 | 0.649 | 0.579 | 0.762 | 0.762 | 0.769 | 0.797 | 1.000 | 1.000 | 1.000 | |
| **14. ANG1%** | 0.595 | 0.405 | 0.405 | 0.405 | 0.474 | 0.415 | 0.577 | 0.577 | 0.585 | 0.741 | 0.636 | 0.636 | 0.636 | 1.000 |

**Table SM3. Kendall (rank) correlation results for the 14 procedures.  (cont'd.)**

**Part C. Engineering**

| | RCR | HV max | C100 | HV100 | NSF6 | HVNSF6 | Top 10% | HV 10% | HV10% min-max | ANG 10% | Top 1% | HV 1% | HV1% min-max | ANG1% |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| **1. RCR** | 1.000 | | | | | | | | | | | | | |
| **2. HV max** | 0.782 | 1.000 | | | | | | | | | | | | |
| **3. C100** | 0.779 | 0.992 | 1.000 | | | | | | | | | | | |
| **4. HV100** | 0.782 | 1.000 | 0.992 | 1.000 | | | | | | | | | | |
| **5. NSF6** | 0.890 | 0.882 | 0.874 | 0.882 | 1.000 | | | | | | | | | |
| **6. HVNSF6** | 0.808 | 0.964 | 0.956 | 0.964 | 0.913 | 1.000 | | | | | | | | |
| **7. Top 10%** | 0.900 | 0.738 | 0.736 | 0.738 | 0.851 | 0.764 | 1.000 | | | | | | | |
| **8. HV10%** | 0.900 | 0.738 | 0.736 | 0.738 | 0.851 | 0.764 | 1.000 | 1.000 | | | | | | |
| **9. HV10% min-max** | 0.910 | 0.723 | 0.721 | 0.723 | 0.836 | 0.749 | 0.979 | 0.979 | 1.000 | | | | | |
| **10. ANG10%** | 0.813 | 0.595 | 0.592 | 0.595 | 0.703 | 0.621 | 0.800 | 0.800 | 0.815 | 1.000 | | | | |
| **11. Top 1%** | 0.733 | 0.556 | 0.554 | 0.556 | 0.649 | 0.577 | 0.695 | 0.695 | 0.705 | 0.833 | 1.000 | | | |
| **12. HV1%** | 0.733 | 0.556 | 0.554 | 0.556 | 0.649 | 0.577 | 0.695 | 0.695 | 0.705 | 0.833 | 1.000 | 1.000 | | |
| **13. HV1% min-max** | 0.736 | 0.559 | 0.556 | 0.559 | 0.651 | 0.579 | 0.697 | 0.697 | 0.708 | 0.836 | 0.997 | 0.997 | 1.000 | |
| **14. ANG1%** | 0.513 | 0.346 | 0.349 | 0.346 | 0.413 | 0.351 | 0.444 | 0.444 | 0.459 | 0.638 | 0.651 | 0.651 | 0.654 | 1.000 |

**Part D. Economics & Business**

| | RCR | HV max | C100 | HV100 | NSF6 | HVNSF6 | Top 10% | HV 10% | HV10% min-max | ANG 10% | Top 1% | HV 1% | HV1% min-max | ANG1% |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| **1. RCR** | 1.000 | | | | | | | | | | | | | |
| **2. HV max** | 0.846 | 1.000 | | | | | | | | | | | | |
| **3. C100** | 0.856 | 0.990 | 1.000 | | | | | | | | | | | |
| **4. HV100** | 0.846 | 1.000 | 0.990 | 1.000 | | | | | | | | | | |
| **5. NSF6** | 0.900 | 0.890 | 0.900 | 0.890 | 1.000 | | | | | | | | | |
| **6. HVNSF6** | 0.833 | 0.915 | 0.926 | 0.915 | 0.923 | 1.000 | | | | | | | | |
| **7. Top 10%** | 0.744 | 0.646 | 0.656 | 0.646 | 0.690 | 0.628 | 1.000 | | | | | | | |
| **8. HV10%** | 0.744 | 0.646 | 0.656 | 0.646 | 0.690 | 0.628 | 1.000 | 1.000 | | | | | | |
| **9. HV10% min-max** | 0.751 | 0.654 | 0.664 | 0.654 | 0.697 | 0.636 | 0.992 | 0.992 | 1.000 | | | | | |
| **10. ANG10%** | 0.782 | 0.659 | 0.664 | 0.659 | 0.687 | 0.636 | 0.741 | 0.741 | 0.749 | 1.000 | | | | |
| **11. Top 1%** | 0.555 | 0.490 | 0.488 | 0.490 | 0.517 | 0.498 | 0.423 | 0.423 | 0.431 | 0.646 | 1.000 | | | |
| **12. HV1%** | 0.555 | 0.490 | 0.488 | 0.490 | 0.517 | 0.498 | 0.423 | 0.423 | 0.431 | 0.646 | 1.000 | 1.000 | | |
| **13. HV1% min-max** | 0.555 | 0.490 | 0.488 | 0.490 | 0.517 | 0.498 | 0.423 | 0.423 | 0.431 | 0.646 | 1.000 | 1.000 | 1.000 | |
| **14. ANG1%** | 0.448 | 0.399 | 0.391 | 0.399 | 0.405 | 0.397 | 0.306 | 0.306 | 0.314 | 0.539 | 0.754 | 0.754 | 0.754 | 1.000 |